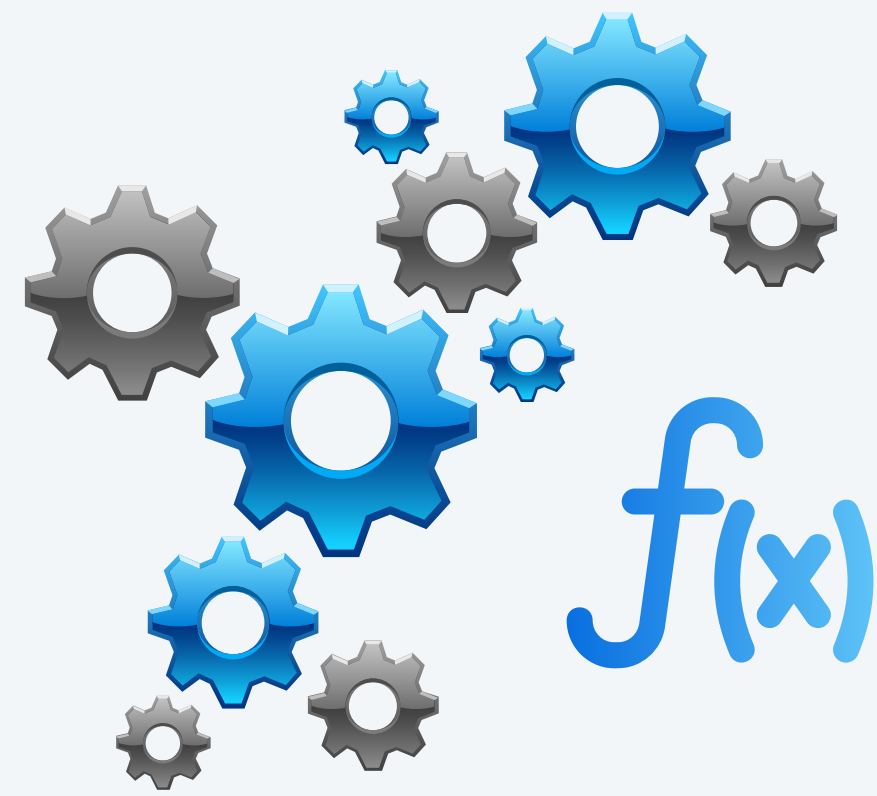


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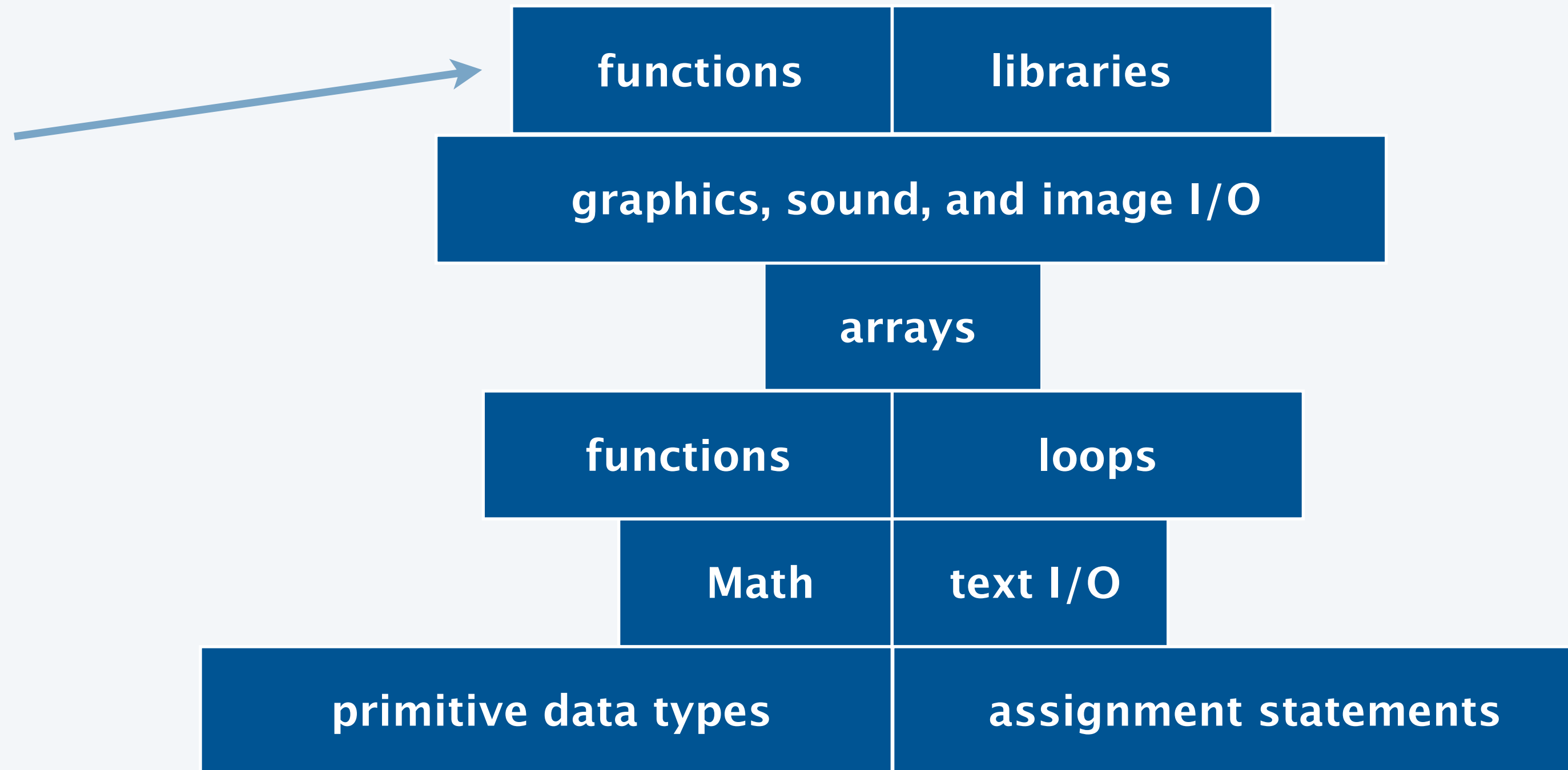
2.1 FUNCTIONS

- ▶ *call by value*
- ▶ *recursion*
- ▶ *what next?*

Basic building blocks for programming



*divide a program
into functions*



Summary

Functions. Provide a fundamental way to change flow of control of program.

- Java evaluates the **arguments** and **passes by value** to function.
- Function initializes **parameter variables** with corresponding argument values.
- Function computes a single **return value** and returns it to caller.

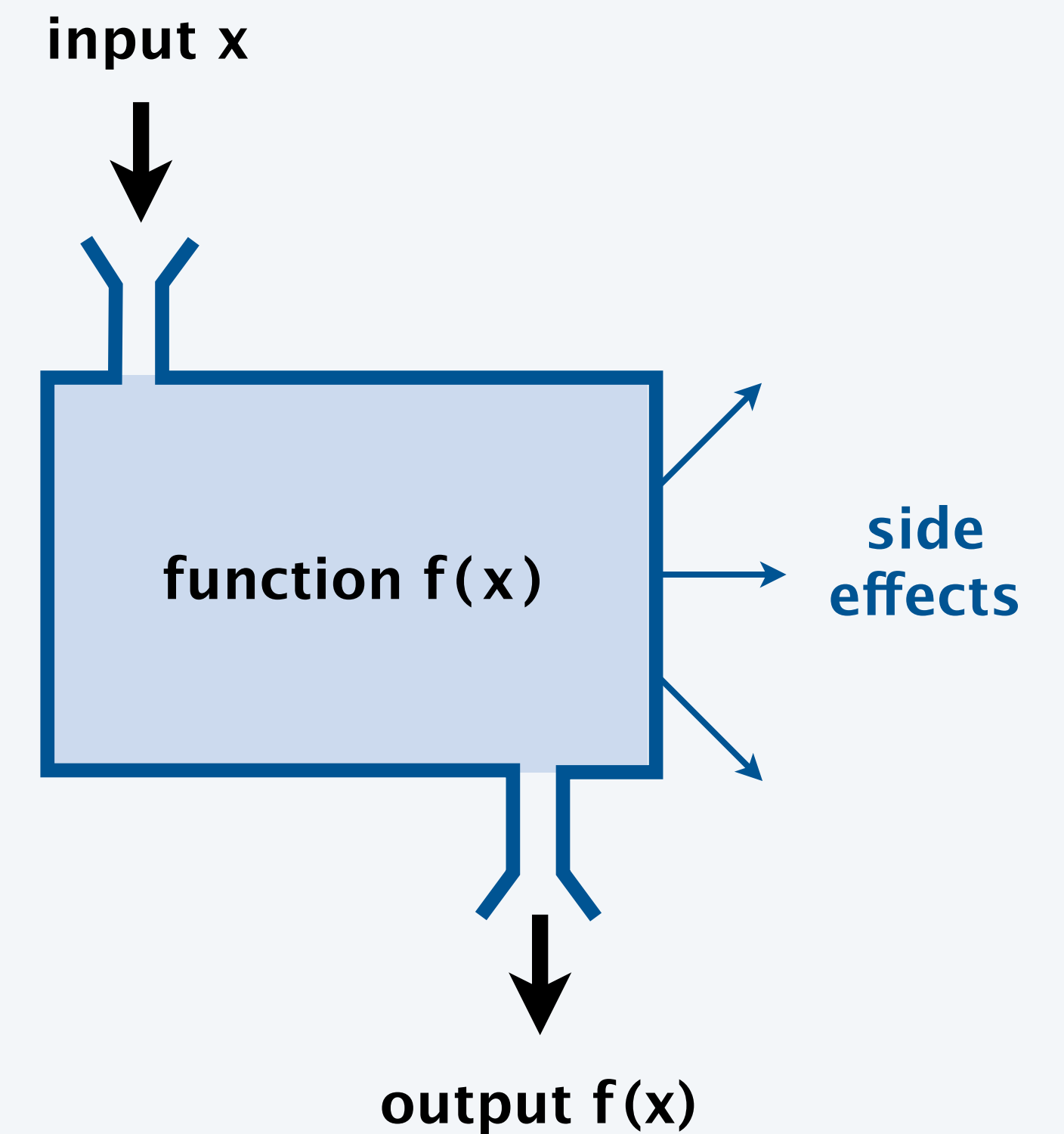
Applications.

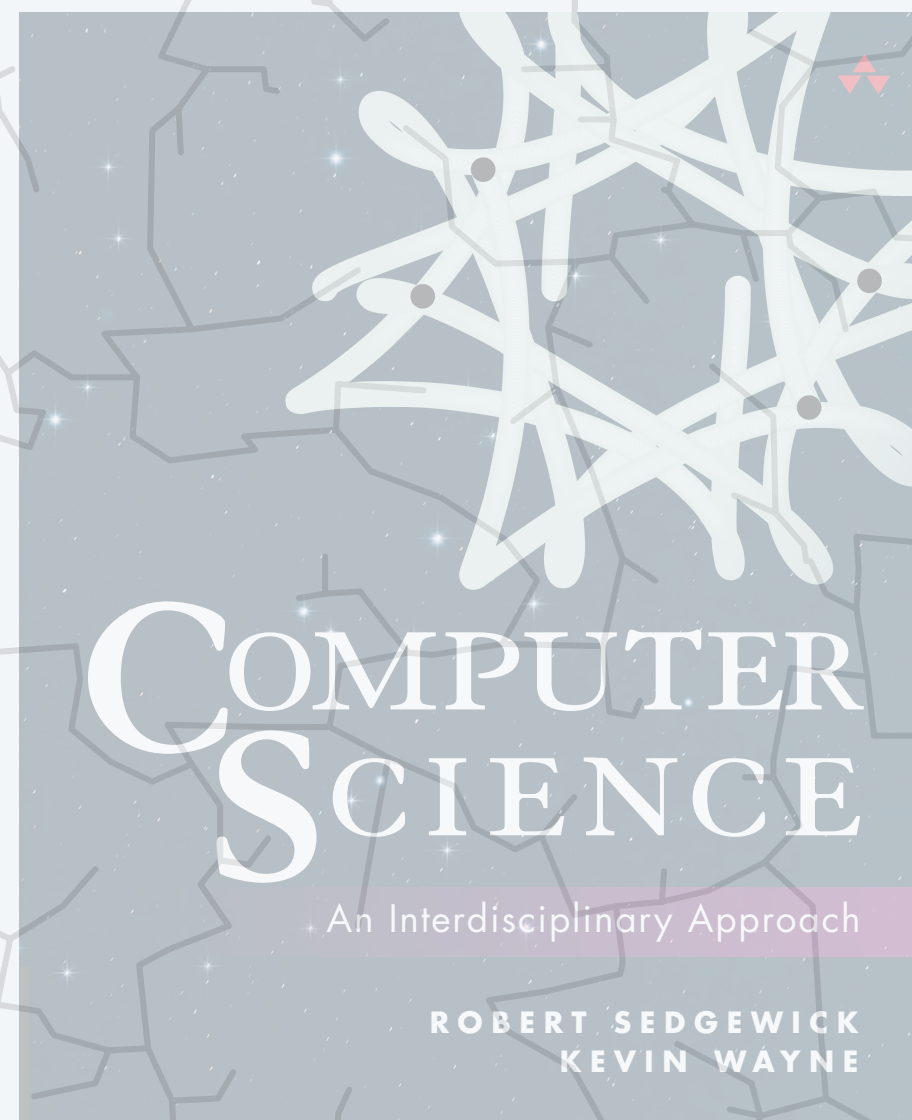
- Scientists use mathematical functions to calculate formulas.
- Programmers use functions to build **modular programs**.
- You use functions for both.

Last lecture. Write your own functions.

Last precept. Build reusable libraries of functions.

This lecture. How Java passes arguments, and **self-referential functions**.





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2.1 FUNCTIONS

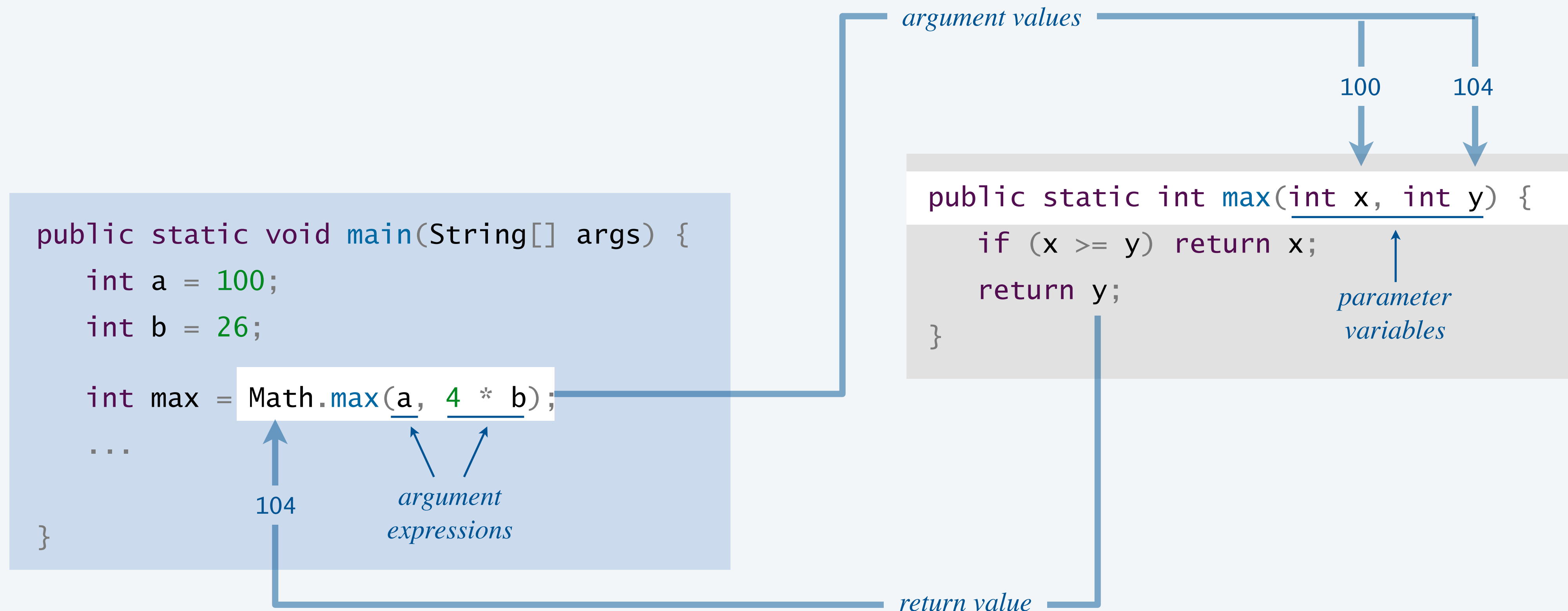
- ▶ *call by value*
- ▶ *recursion*
- ▶ *what next?*

Call by value

Java uses **call by value** to pass arguments to methods.

- Java evaluates each argument expression to produce a **value**.
- Java assigns each value to the corresponding **parameter variable**.

*for primitive types, the value is the data-type value;
for arrays (and other non-primitive types),
the value is an “object reference”*





What does the following program print?

- A. -126
- B. 126
- C. Compile-time error.
- D. Run-time error.

```
public class Mystery {  
    public static void negate(int a) {  
        a = -a;  
    }  
    public static void main(String[] args) {  
        int a = 126;  
        negate(a);  
        StdOut.println(a);  
    }  
}
```



What does the following program print?

- A. 12 6
- B. -12 -6
- C. Compile-time error.
- D. Run-time error.

```
public class AnotherMystery {  
    public static void negate(int[] b) {  
        for (int i = 0; i < b.length; i++)  
            b[i] = -b[i];  
    }  
  
    public static void main(String[] args) {  
        int[] a = { 12, 6 };  
        negate(a);  
        StdOut.println(a[0] + " " + a[1]);  
    }  
}
```

Side effects with arrays

Functions and arrays.

- A function can have the side effect of changing the elements in an argument array. ← *shuffle, reverse, sort, shift, ...*
- But the function cannot change the argument array itself. ← *to refer to a different array (e.g., of a different length or type)*

```
public class Mutate {  
    public static void shuffle(String[] a) {  
        int n = a.length;  
        for (int i = 0; i < n; i++) {  
            int r = (int) (Math.random() * (i + 1));  
            String temp = a[r];  
            a[r] = a[i];  
            a[i] = temp;  
        }  
    }  
    public static void main(String[] args) {  
        shuffle(args);  
        for (int i = 0; i < args.length; i++)  
            StdOut.println(args[i]);  
    }  
}
```

a[] and args[] refer to the same array

swaps a[r] and a[i]

```
~/cos125/functions> java-introcs Mutate A B C D  
C  
A  
B  
D  
  
~/cos125/functions> java-introcs Mutate A B C D  
B  
A  
C  
D  
  
~/cos125/functions> java-introcs Mutate COS 125  
125  
COS
```

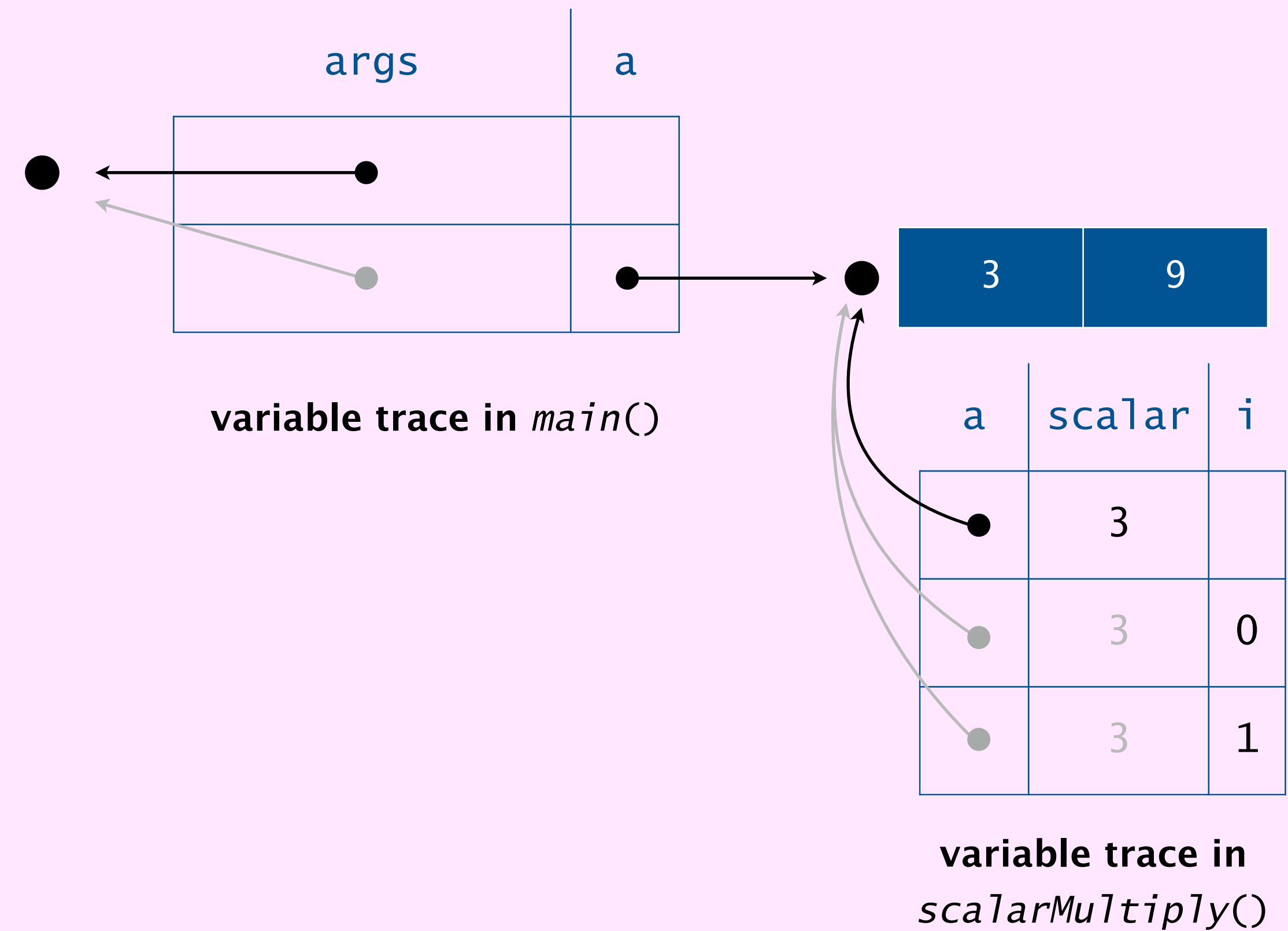

Mechanics of function calls



```
public class Polynomial {
    public static void scalarMultiply(int[] a, int scalar) {
        for (int i = 0; i < a.length; i++)
            a[i] *= scalar;
    }

    public static void main(String[] args) {
        int[] a = { 1, 3 };
        scalarMultiply(a, 3);
        StdOut.println(a[0] + " " + a[1]);
    }
}
```

```
~/cos125/functions> java-introcs Polynomial
3 9
```



Copying an array

Beware of common bugs!

```
public static int[] copy(int[] a) {  
    return a;  
}
```



```
public static void copy(int[] a, int[] b) {  
    b = a;  
}
```



```
public static int[] copy(int[] a) {  
    int[] b = new int[a.length];  
    for (int i = 0; i < a.length; i++)  
        b[i] = a[i];  
    return a;  
}
```



```
public static void copy(int[] a, int[] b) {  
    for (int i = 0; i < a.length; i++)  
        b[i] = a[i];  
}
```



↑
if calling code ran `b = new int[a.length]`

```
public static int[] copy(int[] a) {  
    int[] b = new int[a.length];  
    for (int i = 0; i < a.length; i++)  
        b[i] = a[i];  
    return b;  
}
```



```
public static void copy(int[] a, int[] b) {  
    b = new int[a.length];  
    for (int i = 0; i < a.length; i++)  
        b[i] = a[i];  
}
```



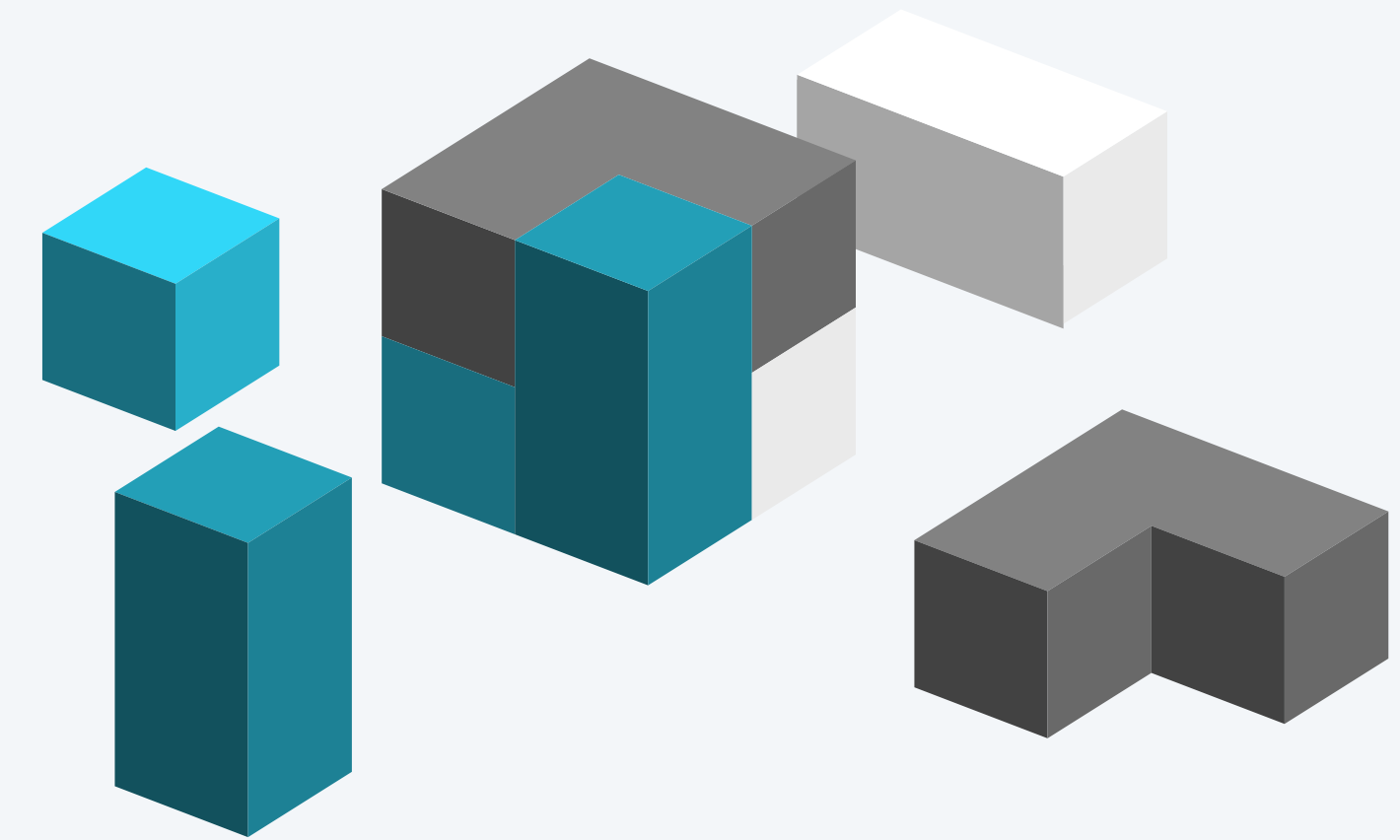
Procedural decomposition

Decomposition. Break up a complex programming problem into smaller functional parts.

Procedural decomposition. Implement each part as a separate **function**.

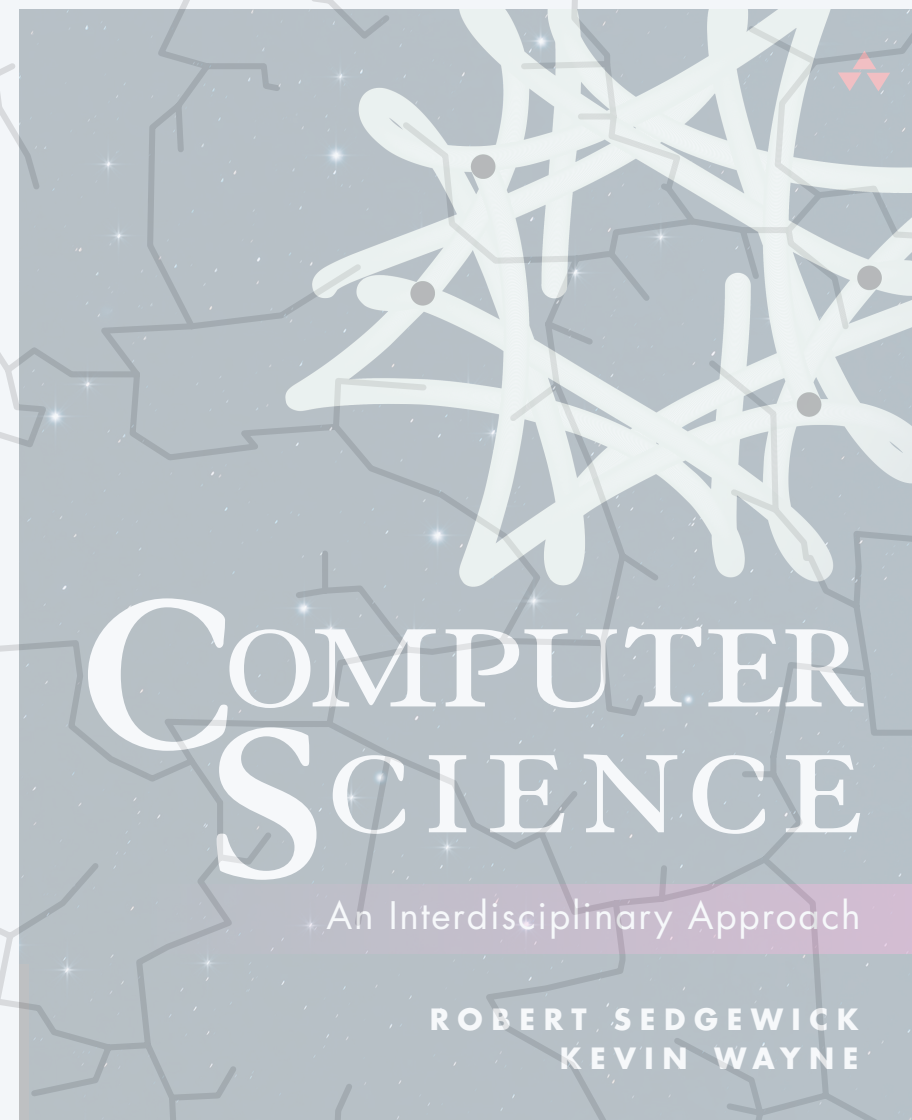
Example. Find the root of a polynomial.

- Approximate until convergence.
- Apply the Newton–Raphson iteration.
- Compute the derivative of a polynomial.
- Evaluate a polynomial at a point.



Benefits. Supports the 3 Rs:

- Readability: understand and reason about code.
- Reliability: test, debug, and maintain code.
- Reusability: reuse and share code.



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2.1 FUNCTIONS

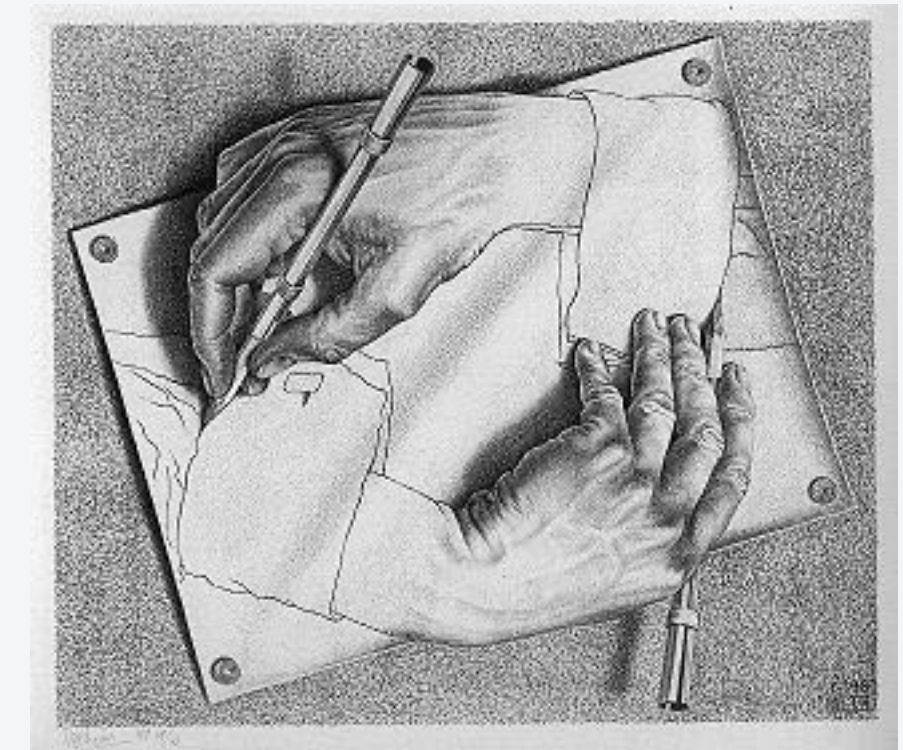
- ▶ *call by value*
- ▶ *recursion*
- ▶ *what next?*

Overview

Recursion is when something is specified in terms of **itself**. ← *self-reference*

Why learn recursion?

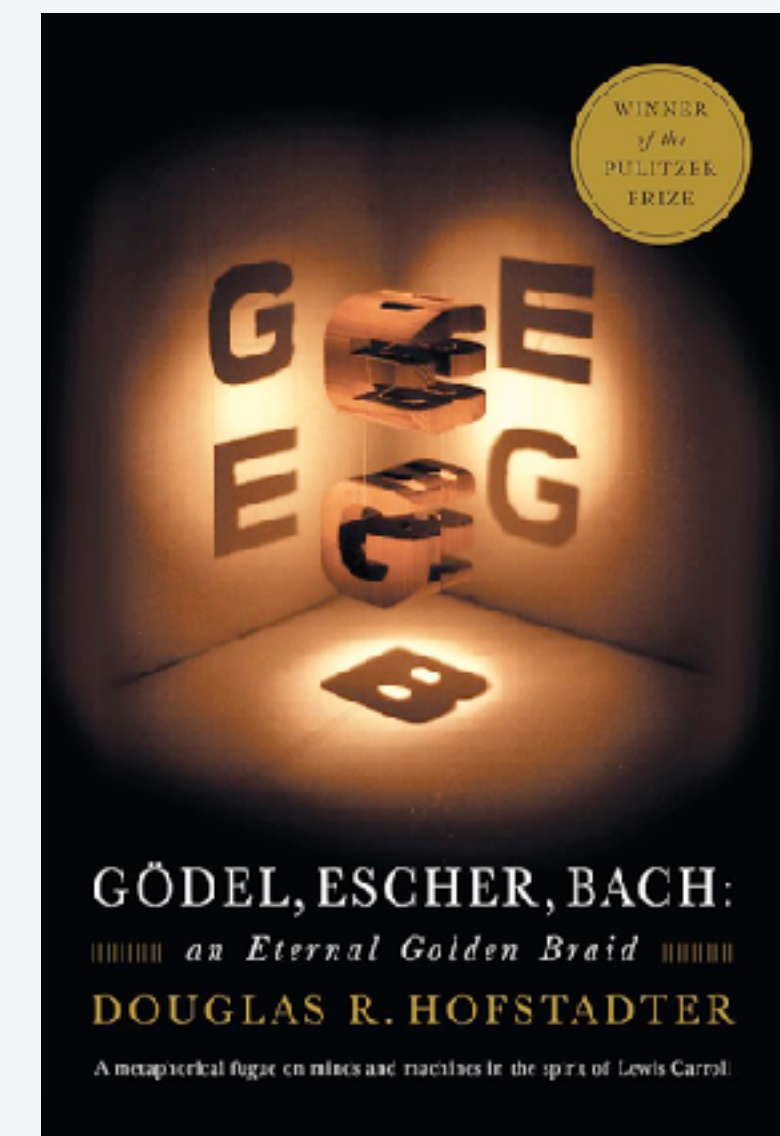
- Powerful programming paradigm.
- Insight into the nature of computation and math. ← *proofs by induction, incompleteness theorems*



Drawing Hands,
by M. C. Escher

Many computational artifacts are naturally self-referential.

- File system with folders containing folders.
- Binary trees.
- Divide-and-conquer algorithms.
- ⋮



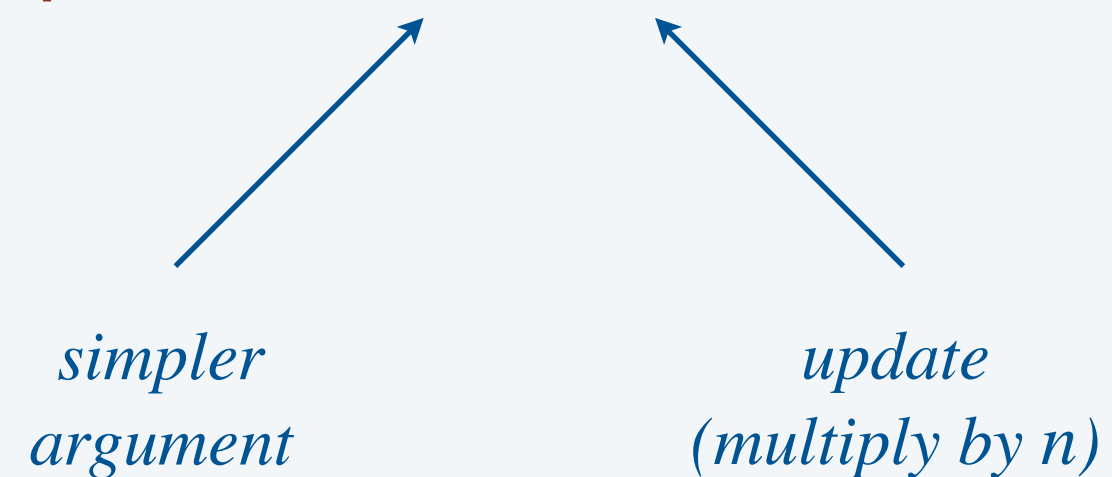
Recursive functions

A recursive function **calls itself**.

- **Base case:** if the argument is “simple,” compute directly.
- **Reduction step:** if the argument is “complicated,” call function on simpler argument and “update.”

Example: Factorial function $n! = n \cdot (n - 1) \cdots 2 \cdot 1$.

- **Base case:** $0! = 1$ (by definition).
- **Reduction step:** $n! = (n - 1)! \cdot n$.



```
public static int factorial(int n) {  
    if (n == 0) return 1;  
    else return n * factorial(n - 1);  
}
```

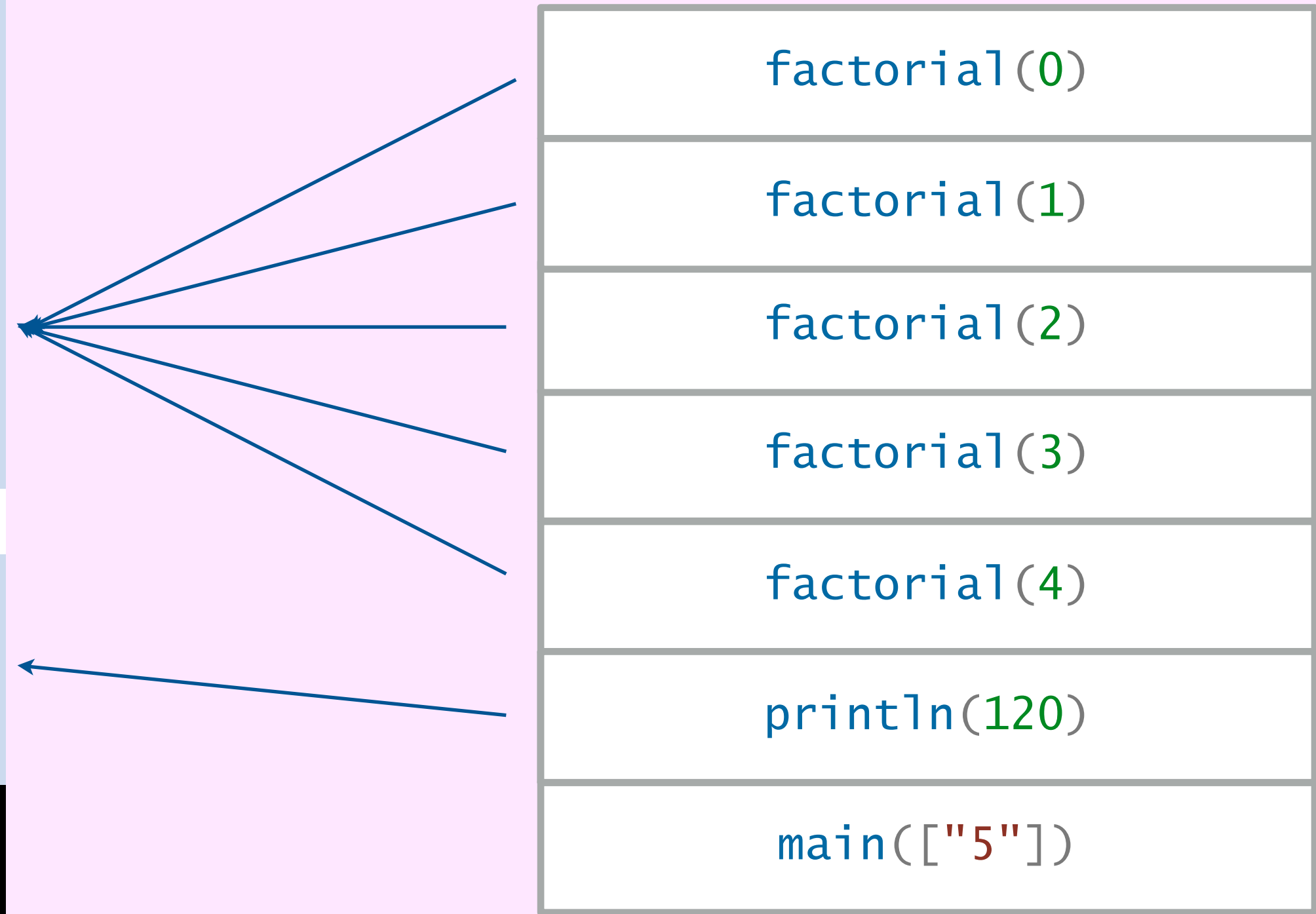
Recursive function calls



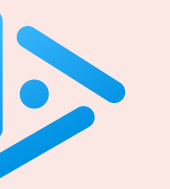
```
public static int factorial(int n) {  
    if (n == 0)  
        return 1;  
    else  
        return n * factorial(n - 1);  
}
```

```
public static void main(String[] args) {  
    int n = Integer.parseInt(args[0]);  
    StdOut.println(factorial(n));  
}
```

```
~/cos125/functions> java-introcs Factorial 5  
120
```



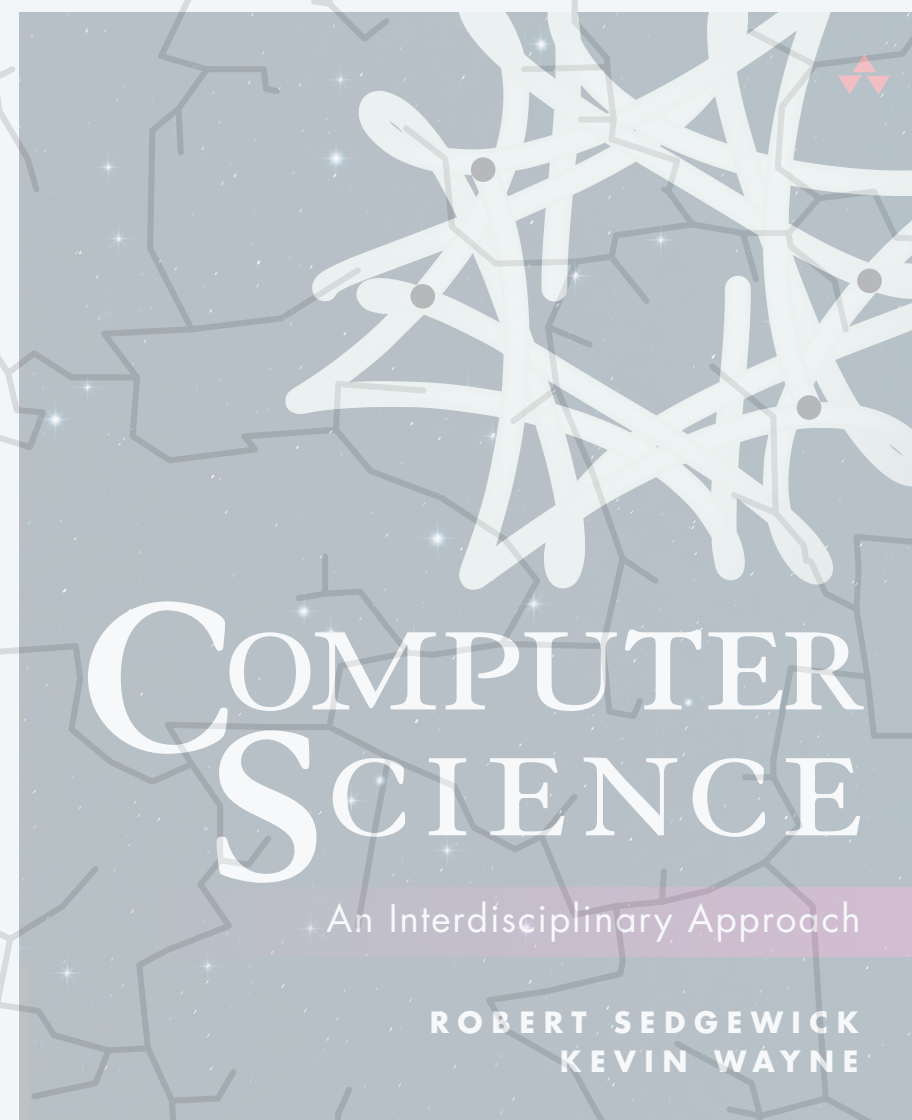
function-call stack



What does the following program print when $n = 4$?

- A. 120
- B. 24
- C. Compile-time error.
- D. Run-time error.

```
public class YetAnotherMystery {  
    public static int factorial(int n) {  
        return n * factorial(n - 1);  
    }  
  
    public static void main(String[] args) {  
        int n = Integer.parseInt(args[0]);  
        StdOut.println(factorial(n));  
    }  
}
```

<https://introcs.cs.princeton.edu>

2.1 FUNCTIONS

- ▶ *call by value*
- ▶ *recursion*
- ▶ *what next?*

Sorting algorithms

Goal. Place numbers of n -integer array in sorted order.

Solution. Mergesort: recursive with $n \log n$ runtime order of growth!

- **Base case:** if array has length 1, return it.
- **Reduction step:** divide array in half; sort both halves then merge.

```
public static void sort(int[] a, int lo, int hi) {  
    if (hi <= lo) return;  
    int mid = (lo + hi) / 2;  
    sort(a, lo, mid);  
    sort(a, mid + 1, hi);  
    merge(a, lo, mid, hi);  
}
```

Object-oriented programming

Data type. A set of values and a set of operations on those values.

Java class. Java's mechanism for defining a new data type.

Object. An instance of a data type that has

- **State:** value from its data type.
- **Behavior:** actions defined by the data type's operations.
- **Identity:** unique identifier (e.g. memory address).



```
public class PrintPoly{
    public static void main(String[] args) {
        Polynomial p = new Polynomial(1.0, 1.0);
        double[] c = new double[] {1.0, -1.0};
        Polynomial q = new Polynomial(c);
        p.multiplyBy(q);
        p.print();
    }
}
```

```
~/cos125/functions> java-introcs PrintPoly
1.0 * X^2 - 1.0
```

Theory of computing

Scenario 1. You just wrote a program that solves Problem A. You're feeling proud (as you should), and think your program is the best.

Can you **prove** it's the best solution for Problem A?



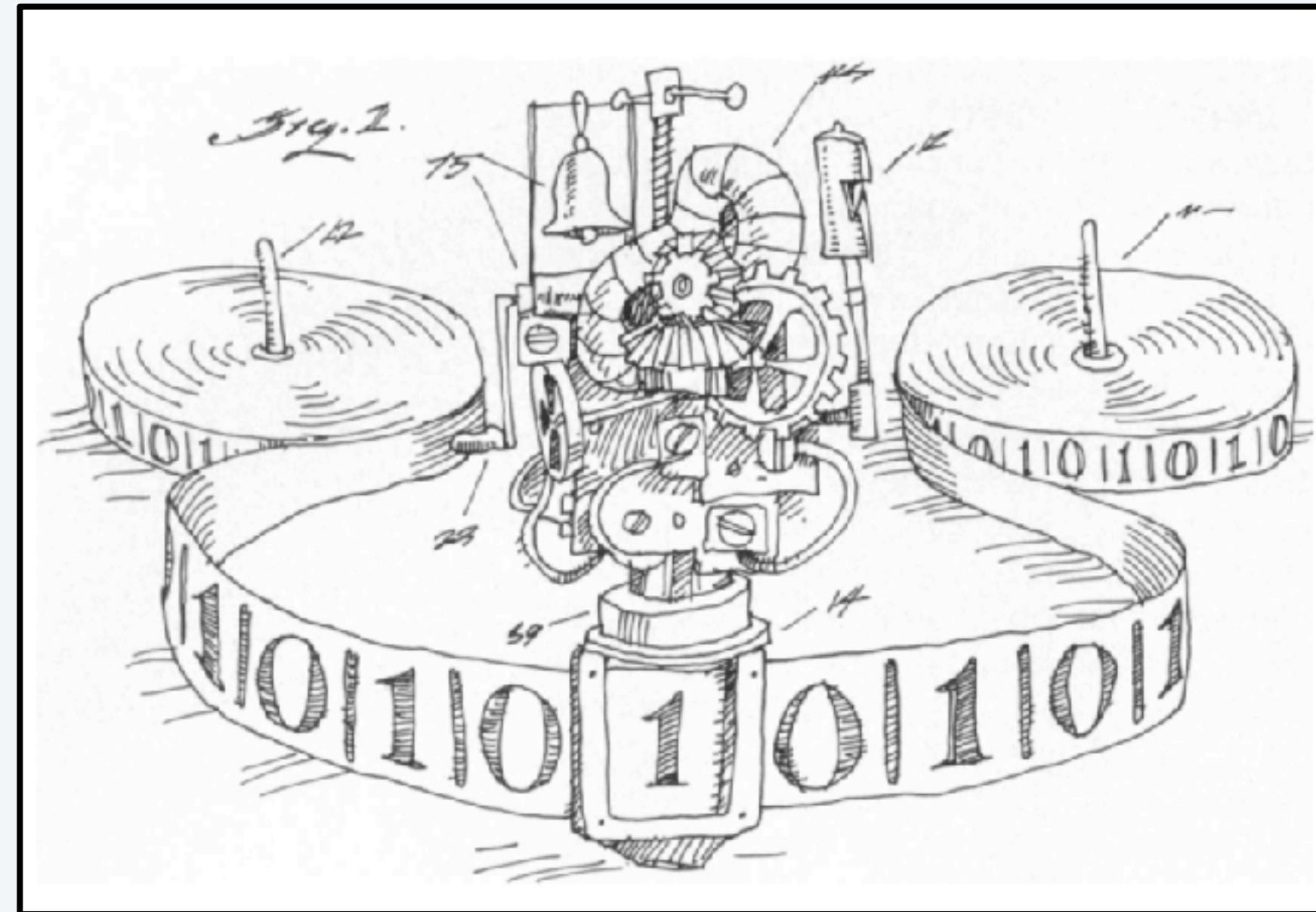
Scenario 2. You spent hours and hours trying to solve Problem B, but didn't get there. You're smart and know it — so Problem B looks like the issue.

Can you **prove** Problem B is really hard to solve?



Fundamental questions

- Q1. What is an **algorithm**?
- Q2. What is an **efficient** algorithm?
- Q3. Which **problems** can be solved efficiently?



A Turing machine

Final exam

Day: August 14th

Place: McDonnell 105

Time: 1:30pm to 2:50pm

8 quiz-type questions (so 10min/question, on average).

Closed book, but can bring “cheatsheet:”

- 8.5-by-11 paper, one side, in your own handwriting.

Study material:

- Review quiz
- Textbook
- Ed

Good luck!

Credits

media	source	license
<i>Gears</i>	<u>Adobe Stock</u>	<u>education license</u>
<i>Function Gradient</i>	<u>Adobe Stock</u>	<u>education license</u>
<i>Function Machine</i>	<u>Wvbailey</u>	<u>public domain</u>
<i>Gödel, Escher, Bach cover</i>	<u>Amazon</u>	
<i>Drawing Hands</i>	<u>Wikipedia</u>	
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<i>Cartoon of Turing Machine</i>	Tom Dunne	