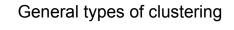


#### Informal goal

- Given set of objects and measure of similarity between them, group similar objects together
- What mean by "similar"?
- · What is good grouping?
- · Computation time / quality tradeoff



- "Soft" versus "hard" clustering – Hard: partition the objects
  - each object in exactly one partition
  - Soft: assign degree to which object in cluster
    - view as probability or score
- flat versus hierarchical clustering

   hierarchical = clusters within clusters



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#### Many

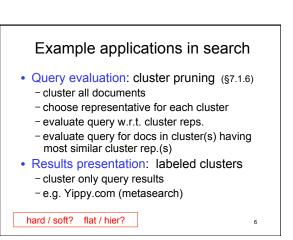
- biology
- astronomy
- computer aided design of circuits
- information organization
- marketing
- -...

## Clustering in information search and analysis

Group information objects

#### ⇒ discover topics

- ? other groupings desirable
- Clustering versus classifying
  - classifying: have pre-determined classes with example members
  - clustering:
    - get groups of similar objects
    - added problem of labeling clusters by topic
       e.g. common terms within cluster of docs.



#### Issues

- What, if any, attributes represent items for clustering purposes?
- What is measure of similarity between items?
  - General objects and matrix of pairwise similaritiesObjects with specific properties that allow other
    - specifications of measure - Most common:
      - Objects are d-dimensional vectors
      - » Euclidean distance
      - » cosine similarity
- · What is measure of similarity between clusters?

#### Issues continued

- Cluster goals?
  - Number of clusters?
  - flat or hierarchical clustering?
  - cohesiveness of clusters?
- How evaluate cluster results?
   relates to measure of closeness between clusters
- Efficiency of clustering algorithms

   large data sets => external storage
- Maintain clusters in dynamic setting?
- Clustering methods? MANY!

## Quality of clustering

- In applications, quality of clustering depends on how well solves problem at hand
- Algorithm uses measure of quality that can be optimized, but that may or may not do a good job of capturing application needs.
- Underlying graph-theoretic problems usually NP-complete

e.g. graph partitioning

Usually algorithm not finding optimal clustering

# General types of clustering methods

- constructive: decide in what cluster each object belongs and don't change
   often faster
- iterative improvement: start with a clustering and move objects around to see if can improve clustering

   often slower but better

### Vector model: K- means algorithm

- Well known, well used
- · Flat clustering
- · Number of clusters picked ahead of time
- Iterative improvement
- · Uses notion of centroid
- · Typically uses Euclidean distance

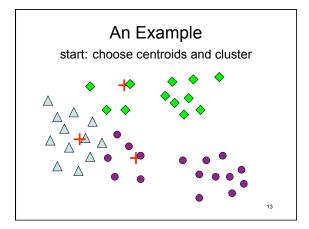
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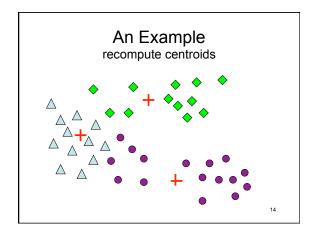
## K-means overview

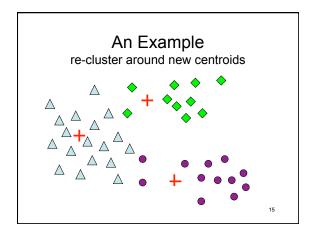
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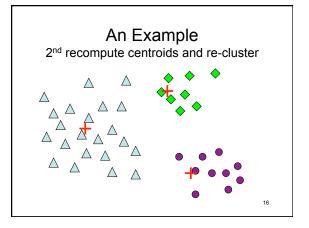
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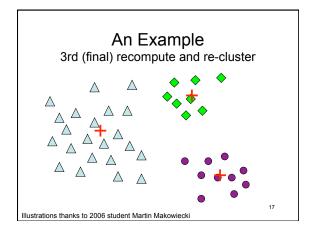
- Choose k points among set to be clustered
   Call them k centroids
  - not required to be in set to be clustered
- For each point not selected, assign it to its closest centroid
  - Assignments give initial clustering
- Until "happy" do:
- Recompute centroids of clusters:
  - centroid of set of vectors  $\{v_i | 1 \le i \le n\} = 1/n * \Sigma_{i=1}^n v_i$ • New centroids may not be points of original set
- Reassign all points to closest centroid
  Updates clusters

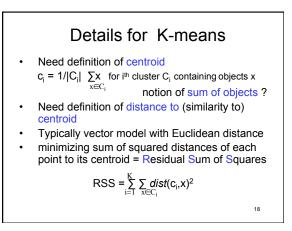


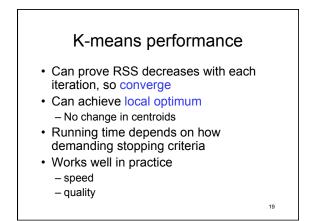


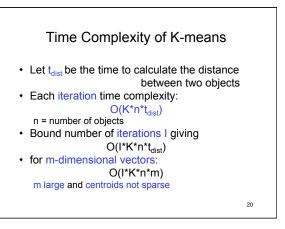


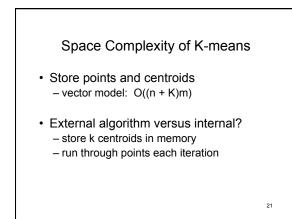


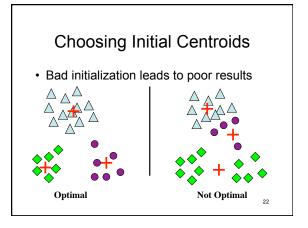


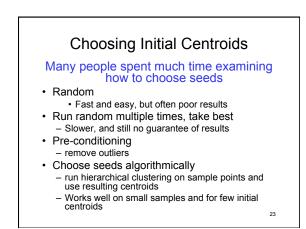


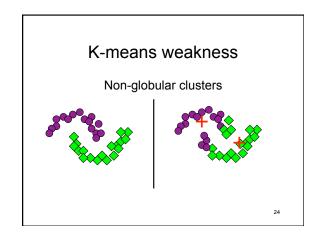


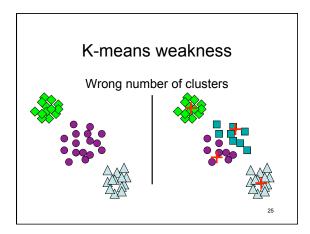


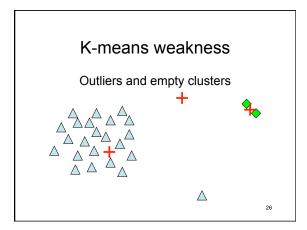












## Real cases tend to be harder

- Different attributes of the feature vector have vastly different sizes

   size of star versus color
- Can weight different features
   how weight greatly affects outcome
- Difficulties can be overcome

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