























	change	next ele	ment w	ith lar	y. ger elei	ments t	to its le	ft, one	-by-on
i	j		1	2	a		-	6	7
6	6	and	had	2 him	his	4 was	you	the	hut
6	5	and	had	him	his	was	the	you	
6	4	and	had	him	his	the	was	you	but
		and	had	him	his	the	was	you	but
	Treestory	g a[6] in	to positi	on by ex	changin	g with la	irger ent	ries to it.	s left



















					me	ging					
ergir	ig. C	omb	oine two p	ore-so	rted I	ists in	to a so	orted	whole.		
ow to	mei	rge (efficient	ly? U	se an a	auxilia	ry arr	ay.	\triangleright		
i	a a										
_	,		dawing	0	1	2	3	4	5	6	7
				and	had	him	was	but	his	the	you
0	4	0	and	and		him	was	but			
1	4	1	but	and	had	him	was	but		the	
1	5	2	had	and	had	him	was	but	his	the	you
2	5	3	him	and	had	him	was		his	the	you
3	5	4	his	and	had	him	was		his	the	you
3	6	5	the	and	had	him	was		his	the	you
-	6	6	was	and	had	him	was	but	his	the	you
3	7	7	you	and	had	him	was		his	the	you
3											











		Mergeso	ort: Lesson			
Lesson. Gre	eat algorith	nms can be m	ore powerful	than superco	mputers.	
	Computer	Compares Per Second	Insertion	Mergesort		
	laptop	107	3 centuries	3 hours		
	super	1012	2 weeks	instant		
		N	= 1 billion			
						3

Longest Repeated Substring	
	34











Longes	t Repeated S	Substring: Ei	npirical Anal	ysis
Input File	Characters	Brute	Suffix Sort	Length
LRS.java	2,162	0.6 sec	0.14 sec	73
Amendments	18,369	37 sec	0.25 sec	216
Aesop's Fables	191,945	3958 sec	1.0 sec	58
Moby Dick	1.2 million	43 hours †	7.6 sec	79
Bible	4.0 million	20 days †	34 sec	11
Chromosome 11	7.1 million	2 months [†]	61 sec	12,567
Pi	10 million	4 months [†]	84 sec	14

Lesson. Sorting to the rescue; enables new research.

Summary

Binary search. Efficient algorithm to search a sorted array.

Mergesort. Efficient algorithm to sort an array.

Applications. Many many applications are enabled by fast sorting and searching.