COS426 Precept8

Rasterizer (Part 1)

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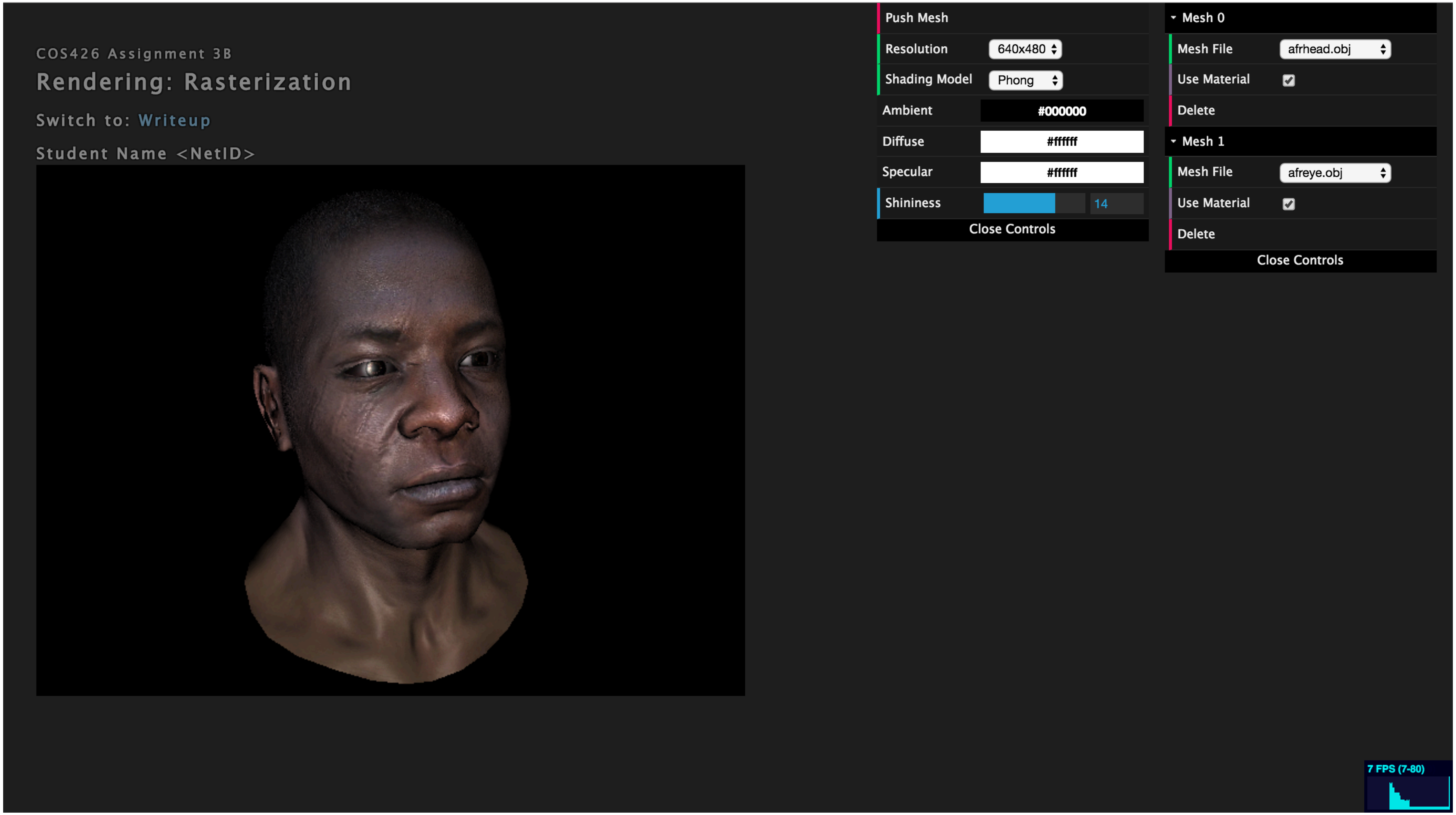
Rasterizer

- Render a lot of triangles in the image plane
  - Projection – orthogonal (naïve) or perspective
  - Which triangles are in the front? (z buffering)
  - How does the triangle react to the light? (reflection model)
  - Meshes are coarse. How to cheat our eyes? (interpolation)
  - How does the material affect the color? (texture mapping)
  - How to add fine details at low cost? (normal mapping)

GUI & Demo

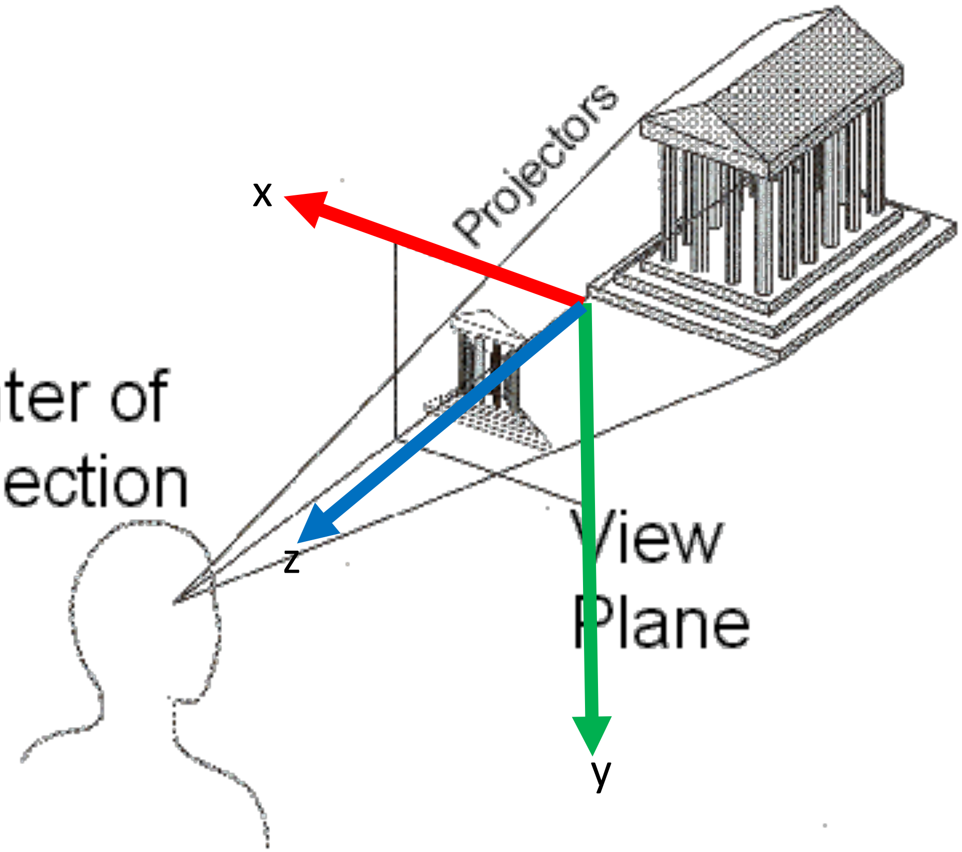

COS426 Assignment 3B
Rendering: Rasterization
Switch to: Writeup
Student Name <NetID>
Push Mesh
Resolution 640x480
Shading Model Phong
Ambient #000000
Diffuse #ffffff
Specular #ffffff
Shininess 14
Close Controls
Mesh 0
Mesh File afrhead.obj
Use Material
Delete
Mesh 1
Mesh File afreye.obj
Use Material
Delete
Close Controls
7 FPS (7-80)

In this precept

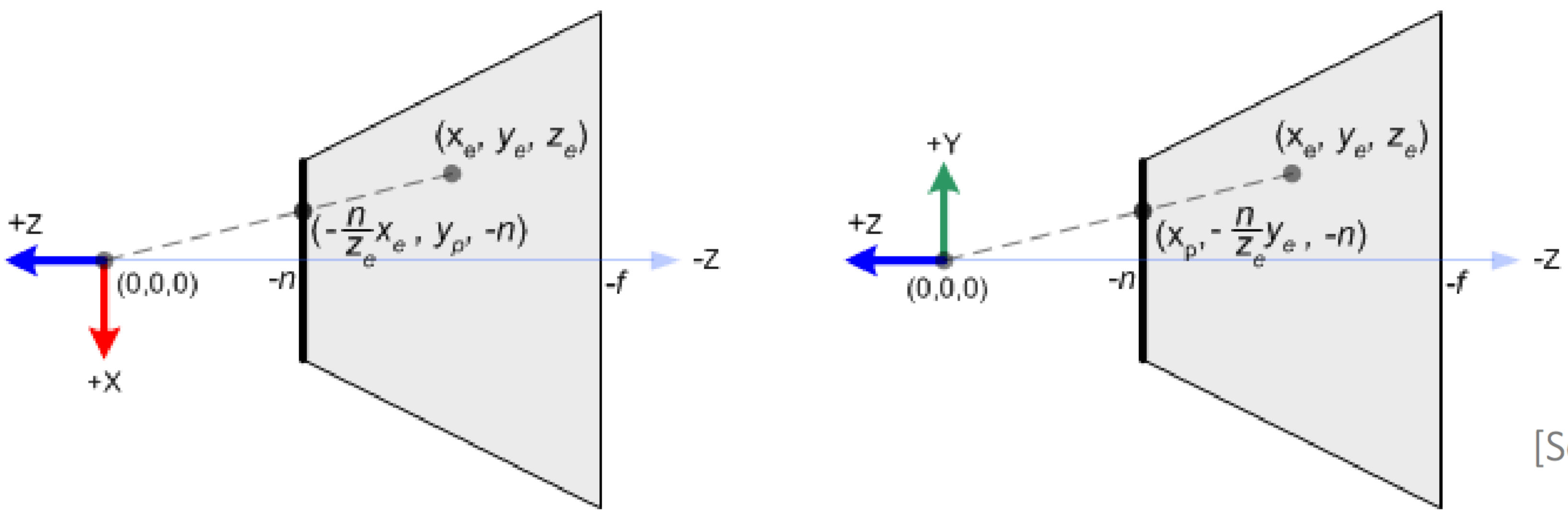
- perspective projection
- barycentric coordinates

Perspective Projection

objects must be on the negative z axis, otherwise cannot be seen.



Near and Far Planes



[Song Ho Ahn]

n and f are usually positive values. But near plane locates at –n and far plane locates at –f.

Graphics Projection Transform

- Map x-component of a point to (-1, 1)
- Map y-component of a point to (-1, 1)
- Map z-component of a point from (near, far) to (-1, 1)
- Believe it or not, this matrix does the transformation:

$$\begin{pmatrix} \frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & -\frac{f+n}{f-n} & -\frac{2fn}{f-n} \\ 0 & 0 & -1 & 0 \end{pmatrix}$$

Use the Projection Matrix

- What is the fourth dimension?
  - This matrix is in homogeneous form and it should be multiplied with homogeneous coordinates: (x, y, z, 1)^T. Then you get (x', y', z', w).
  - transform it back -> (x'/w, y'/w, z'/w)
  - if z is outside (near, far), don't do the projection because it can't be seen.

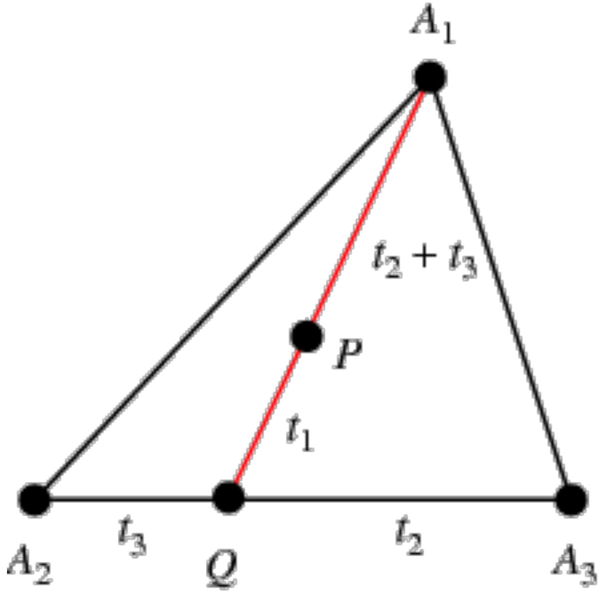
$$\begin{pmatrix} \frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & -\frac{f+n}{f-n} & -\frac{2fn}{f-n} \\ 0 & 0 & -1 & 0 \end{pmatrix}$$

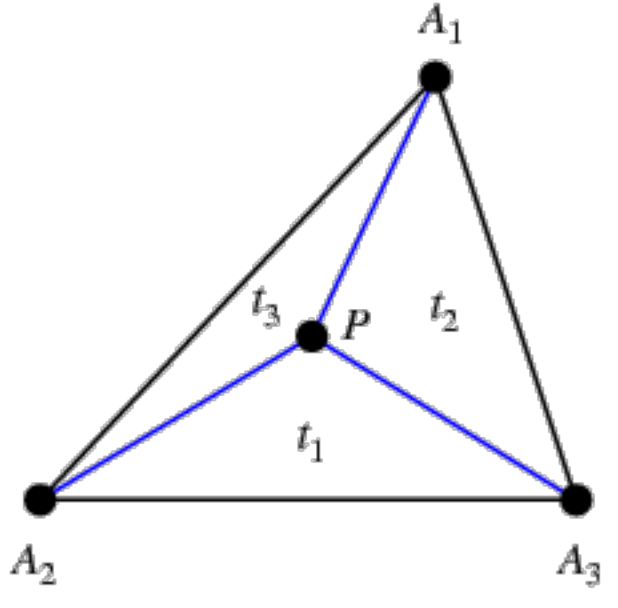
Changing Camera Pose

- This projection matrix can only be directly used when the camera coordinate is perfectly aligned with the world coordinate. What if the camera is moving?
- We represent the pose of the camera in the world space as: [R|t], also in homogeneous form (4x4 matrix). [R|t] transforms a point represented in the camera coordinate system to the world coordinate system.
- But we want to transform a point in the world coordinate system to the camera coordinate system. So we simply use inv([R|t]).
- Concatenate with the previous projection matrix:
  - $\begin{pmatrix} \frac{2n}{r-l} & 0 & \frac{r+l}{r-l} & 0 \\ 0 & \frac{2n}{t-b} & \frac{t+b}{t-b} & 0 \\ 0 & 0 & -\frac{f+n}{f-n} & -\frac{2fn}{f-n} \\ 0 & 0 & -1 & 0 \end{pmatrix}$ x inv([R|t] (given as viewMat in the code)

Barycentric Coordinates

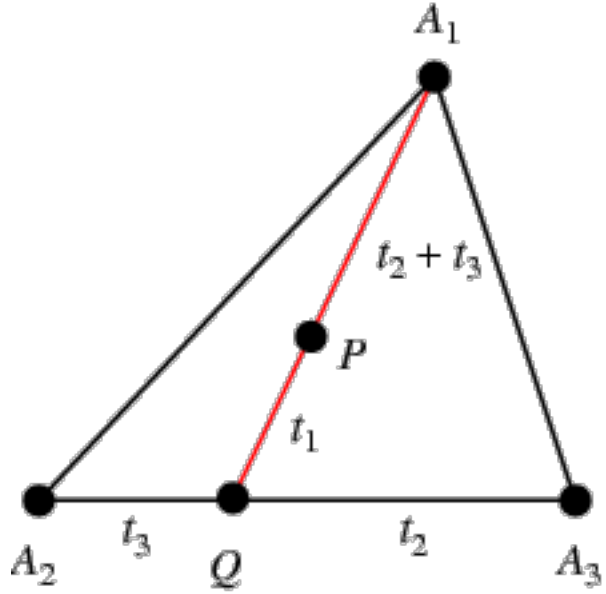
- Any point in the triangle can be represented as a linear combination of the three vertices
  - Q is a linear combination of A2 and A3
  - P is a linear combination of Q and A1

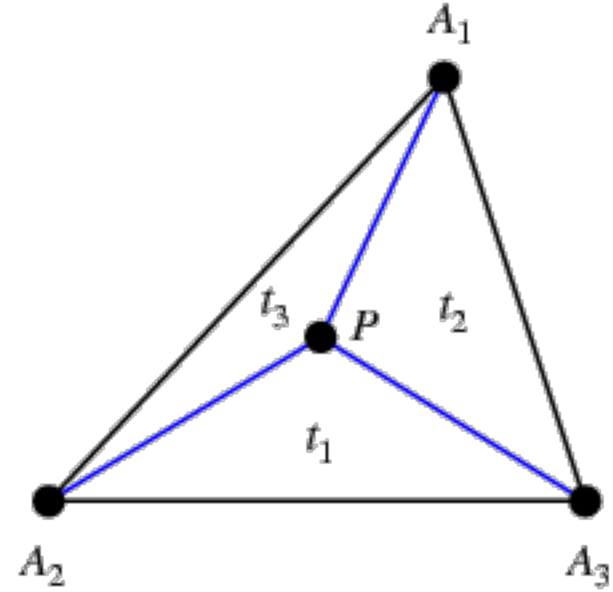




Barycentric Coordinates

- $P = \alpha A_1 + \beta A_2 + \gamma A_3$
- $\alpha + \beta + \gamma = 1$
- if any of $\alpha, \beta, \gamma < 0$, P is not in the triangle.





See this article for detailed computation:
https://fgiesen.wordpress.com/2013/02/06/the-barycentric-conspirac/

Use Barycentric Coordinates

- Weight average of the values on the 3 coordinates
  - Interpolate z coordinate
  - Interpolate color
  - Interpolate normal direction
  - Interpolate texture coordinates

Q&A