## Sequential and Clocked Circuits; Finite State Machines

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COS 116
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## Sequential Circuits (Recap.)

- Circuits with AND, OR and NOT gates.
- Cycles are allowed.
- Can exhibit "memory".
- May exhibit instabilities (saw last time).


## Recap: D Flip Flop

a.k.a. "Airlock", "Master-Slave"

Basic Memory Block - stores 1 bit.


If we "toggle" the write input (setting it 1 then setting it 0 ) then M acquires the value of $D$.

## Timing Diagram



Time
W


M


Time

## What controls the "Write" signal?

- Often, the system clock!
- "clock" = device that sends out a fluctuating voltage signal that looks like this

Write $=1$

Write $=0$
$\qquad$

## Synchronous Sequential Circuit

(aka Clocked Sequential Circuit)


## Shorthands



## Clock Speeds

| 1974 | Intel 8080 | 2 MHz <br> (Mega $=$ Million) |
| :--- | :--- | :--- |
| Heinrich Hertz <br> $1857-94$ |  |  |
|  | Original IBM PC | 4.77 MHz |
| 1993 | Intel Pentium | 66 MHz |
| 2005 | Pentium 4 | 3.4 GHz <br> (Giga $=$ Billion) |

Distance traveled by light during 1 clock cycle of Pentium 4 4 inches

## What limits clock speed?

## Finite State Machines

## State diagram for automatic door



No Person Detected

## Implementing as synchronous circuit

## INPUT

$$
\begin{aligned}
& 0=\text { No Person Detected } \\
& 1=\text { Person Detected }
\end{aligned}
$$

STATE

$$
\begin{aligned}
& 0=\text { Door Closed } \\
& 1=\text { Open }
\end{aligned}
$$



No Person Detected

| Input | Present State | Next State |
| :---: | :---: | :---: |
| 0 | 0 | 0 |
| 1 | 0 | 1 |
| 0 | 1 | 0 |
| 1 | 1 | 1 |

## Implementation



## Moore FSM (see handout)



K Flip flops allow FSM to have $2^{\mathrm{K}}$ states

## Other examples of FSMs

- Sisyphus

- Brook's Genghis (51 FSMs) (see p. 46 in our text)
- Human Soul a la Aquinas (see Handout)


## Portion of Genghis AFSM Network



## Finally...

 How computers execute programs.
## Scribbler Control Panel Program

## Machine Executable Code



## Meet the little green man..

The Fetch - Decode - Execute FSM


. 0110100000110111101010111.
Program stored in machine memory; each instruction represented by say 64 bits

## Discussion:How would you implement a

Turing-Post program with a digital circuit?
1.PRINT 0
2. GO RIGHT
3. GO TO STEP 1 if 1 SCANNED
4. GO TO STEP 1 if 0 SCANNED
5. STOP

Assume "PRINT" and "SCAN" as basic operations

