

Summary of Optimization Material

We've looking at a variety of different analysis techniques and optimization techniques over the last couple of weeks:

- Chapter 17.1-17.3: Data-flow analysis and optimizations
 - Liveness analysis, reaching definition analysis
 - Constant propagation, copy propagation, common sub expression elimination, constant folding,...
- Chapter 18.1-18.3: Dominators, loops, analysis and optimizations
 - Loop invariant analysis and statement hoisting
 - Induction variable analysis, strength reduction and elimination.
- Chapter 19.1, 19.3 (not conditional constant propagation): Static Single Assignment (SSA), a pervasive intermediate representation for advanced optimization

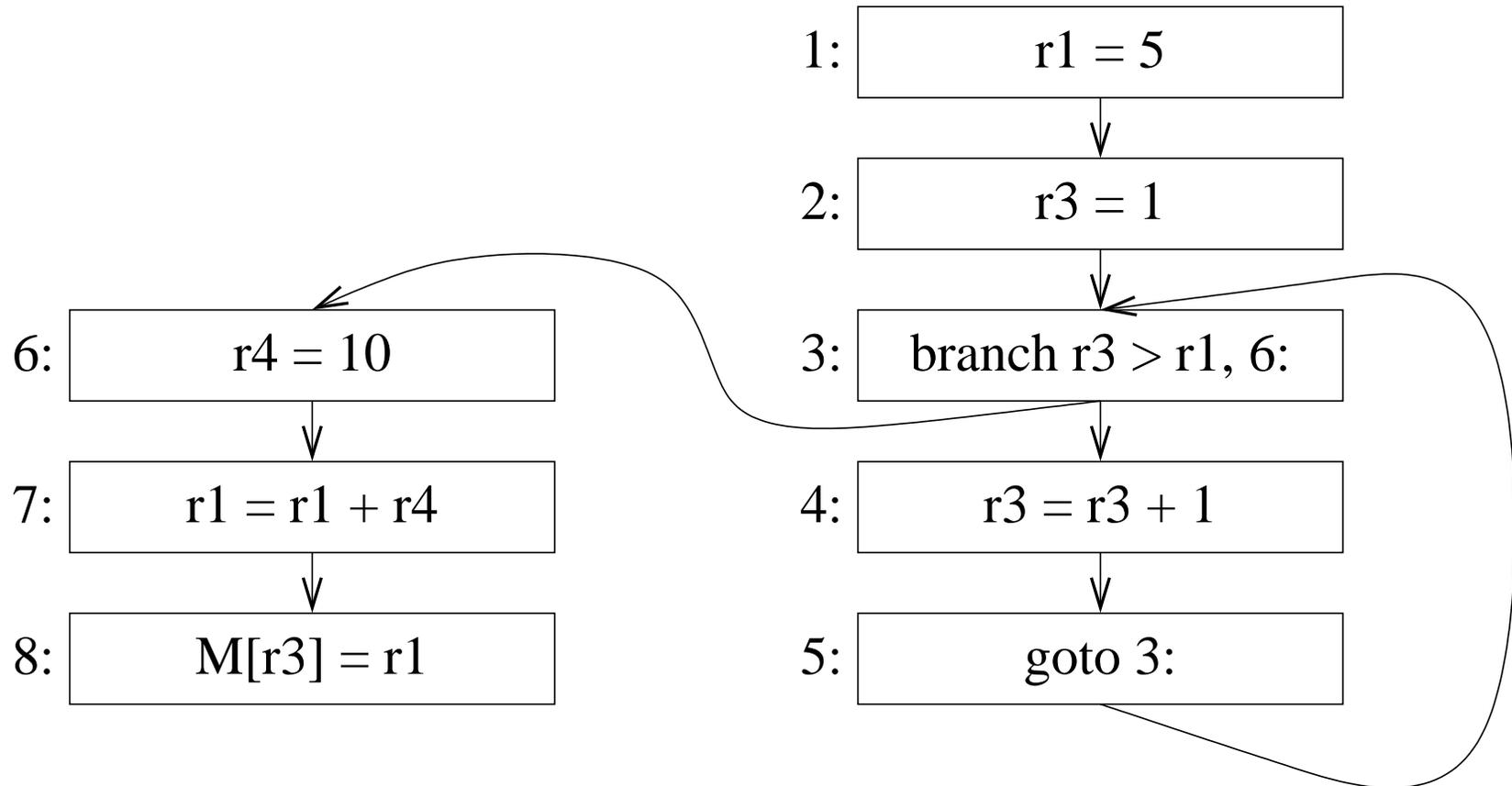


Motivating SSA

- Many optimizations need to find all use-sites for each definition, and all definition-sites for each use.
 - Constant propagation must refer to the definition-site of the unique reaching definition.
 - Copy propagation, common sub-expression elimination...
- Information connecting all use-sites to corresponding definition-sites can be stored as *def-use chains* and/or *use-def chains*.
- *def-use chains*: for each definition d of r , list of pointers to all uses of r that d reaches.
- *use-def chains*: for each use u of r , list of pointers to all definitions of r that reach u .



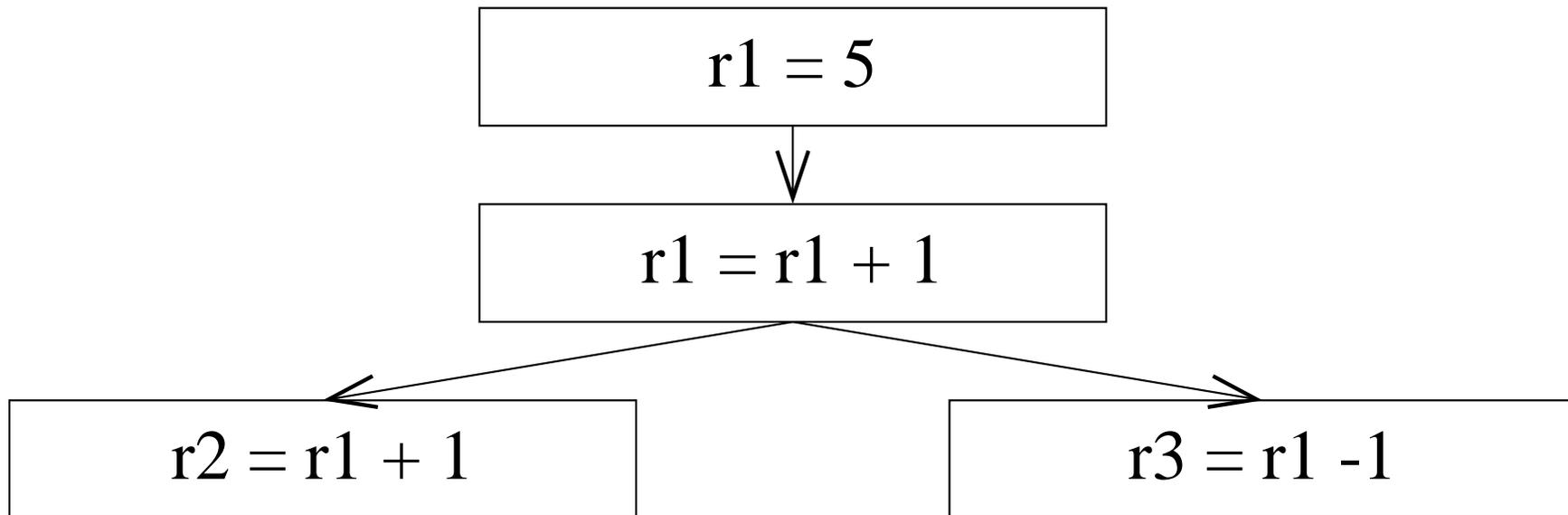
Use-Def Chains, Def-Use Chains Example



Static Single Assignment

Static Single Assignment (SSA):

- improvement on def-use chains
- each temporary has only one definition in program
- for each use u of r , only one definition of r reaches u



Static Single Assignment

Static Single Assignment Advantages:

- Dataflow analysis and code optimization is simplified and made more efficient.
- Less space required to represent def-use chains. Def-use chains require space proportional to uses * defs for each variable.
- Eliminates unnecessary relationships:

```
for i = 1 to N do A[i] = 0
for i = 1 to M do B[i] = 1
```

- No reason why both loops should be forced to use same register to hold index register.
- SSA renames second *i* to a new temporary which may lead to better register allocation/optimization.



Static Single Assignment

```
int f(int i, int j) {
    int x,y;
    switch (i) {
        case 0: x = 3; break;
        case 1: x = 7; break;
        case 2: x = 4; break;
        default: x = 17; break;
    }
    switch (j) {
        case 0: y = x+1; break;
        case 1: y = x+7; break;
        case 2: y = x+3; break;
        default: y = x+33; break;
    }
    return y;
}
```

Building def-use chains costs quadratic space whereas SSA encodes def-use information in linear space.



Conversion to SSA Form

Easy to convert basic blocks into SSA form:

- Each definition modified to define brand-new register, instead of redefining old one.
- Each use of register modified to use most recently defined version.

$$r1 = r3 + r4$$

$$r2 = r1 - 1$$

$$r1 = r4 + r2$$

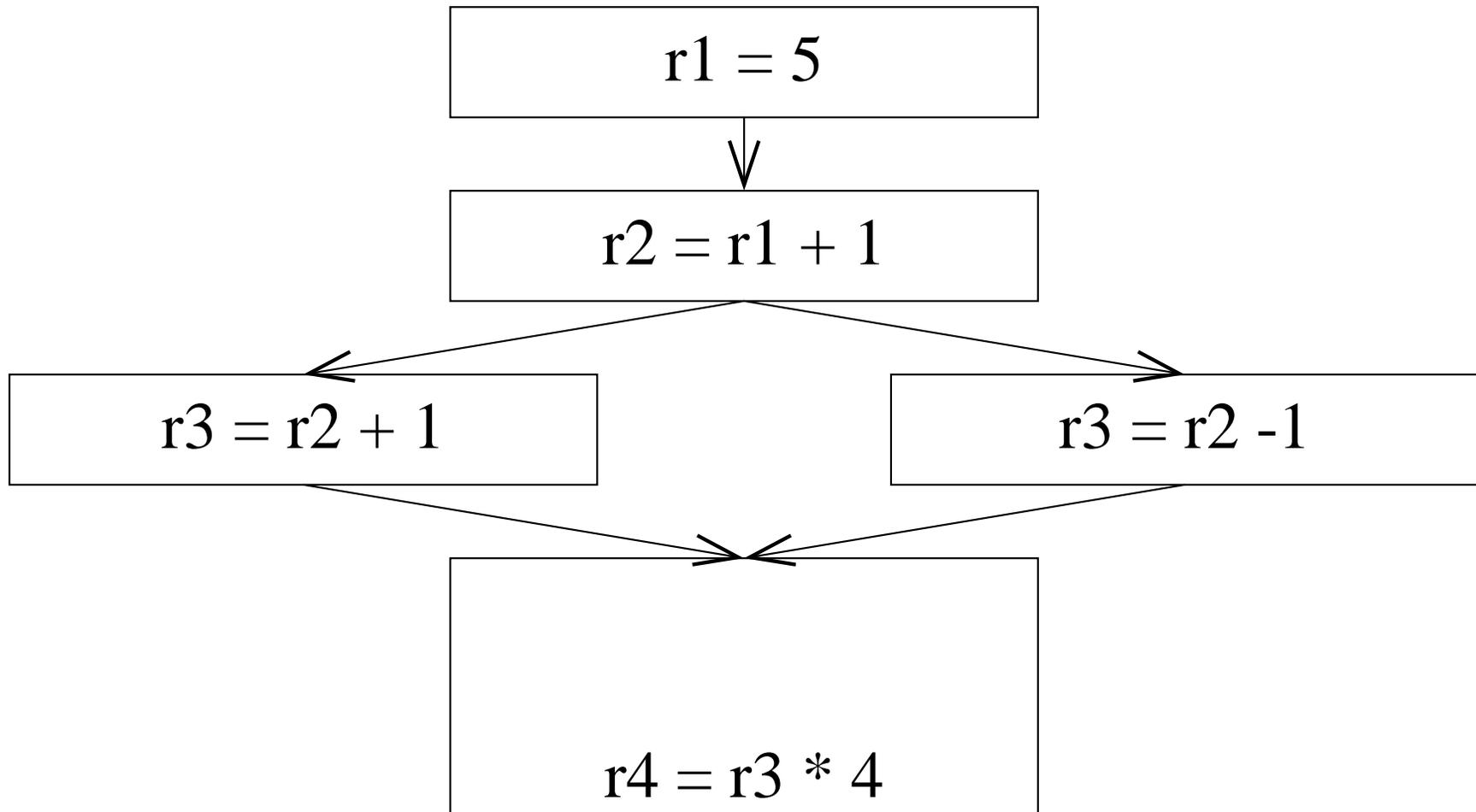
$$r2 = r5 * 4$$

$$r1 = r1 + r2$$

This is easy for straight-line programs but complex control flow introduces problems.



Conversion to SSA Form



Use ϕ functions.



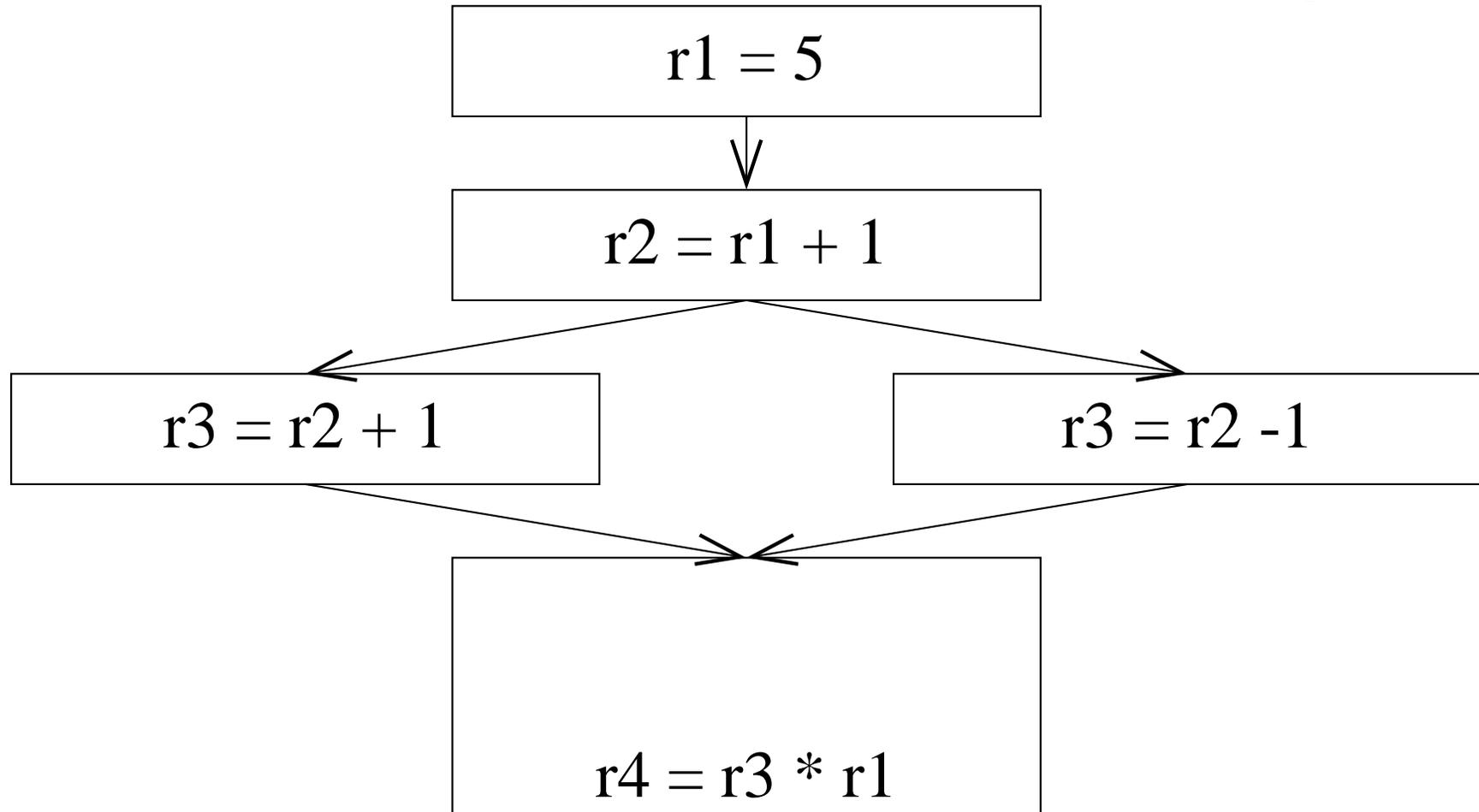
Conversion to SSA Form

- ϕ -functions enable the use of r_3 to be reached by exactly one definition of r_3 .
- $r_3'' = \phi(r_3, r_3')$:
 - $r_3'' = r_3$ if control enters from left
 - $r_3'' = r_3'$ if control enters from right
- Can implement ϕ -functions as set of move operations on each incoming edge.
- In practice, ϕ -functions are just used as notation.



Conversion to SSA Form - Simple Approach

Can insert ϕ -functions for each register at each node with more than two predecessors.



We can do better...



Conversion to SSA Form

Path-Convergence Criterion: Insert a ϕ -function for a register r at node z of the flow graph if ALL of the following are true:

1. There is a block x containing a definition of r .
2. There is a block $y \neq x$ containing a definition of r .
3. There is a non-empty path P_{xz} of edges from x to z .
4. There is a non-empty path P_{yz} of edges from y to z .
5. Paths P_{xz} and P_{yz} do not have any node in common other than z .
6. The node z does not appear within both P_{xz} and P_{yz} prior to the end, though it may appear in one or the other.

Assume CFG entry node contains implicit definition of each register:

- $r =$ actual parameter value
- $r =$ undefined

ϕ -functions are counted as definitions.



Conversion to SSA Form

Solve path-convergence iteratively:

WHILE (there are nodes x, y, z satisfying conditions 1-6) &&
(z does not contain a *phi*-function for r) DO:
insert $r = \phi(r, r, \dots, r)$ (one per predecessor) at node z .

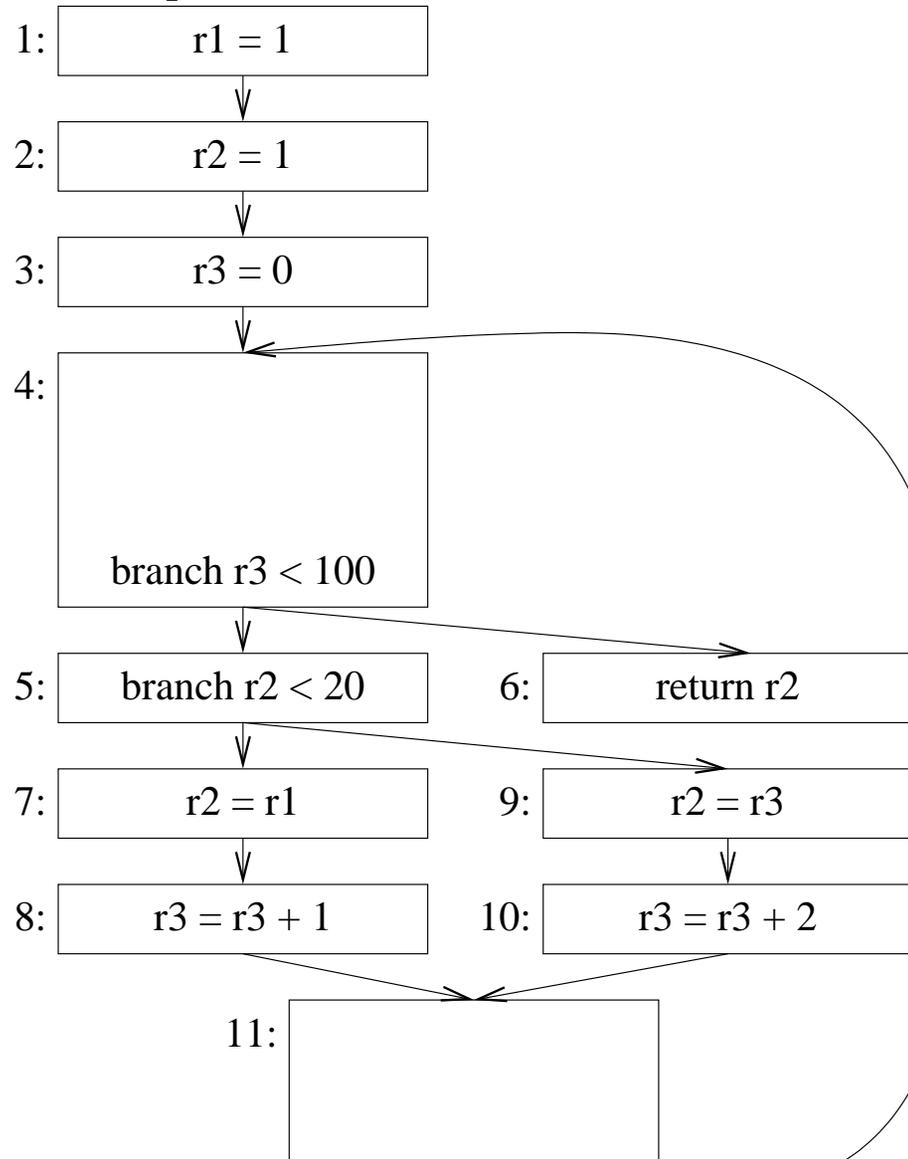
- Costly to compute.
- Since definitions dominate uses, use domination to simplify computation.

Use *Dominance Frontier*...pgs 433,434



Static Single Assignment Example

Insert *phi*-functions:



Static Single Assignment Example

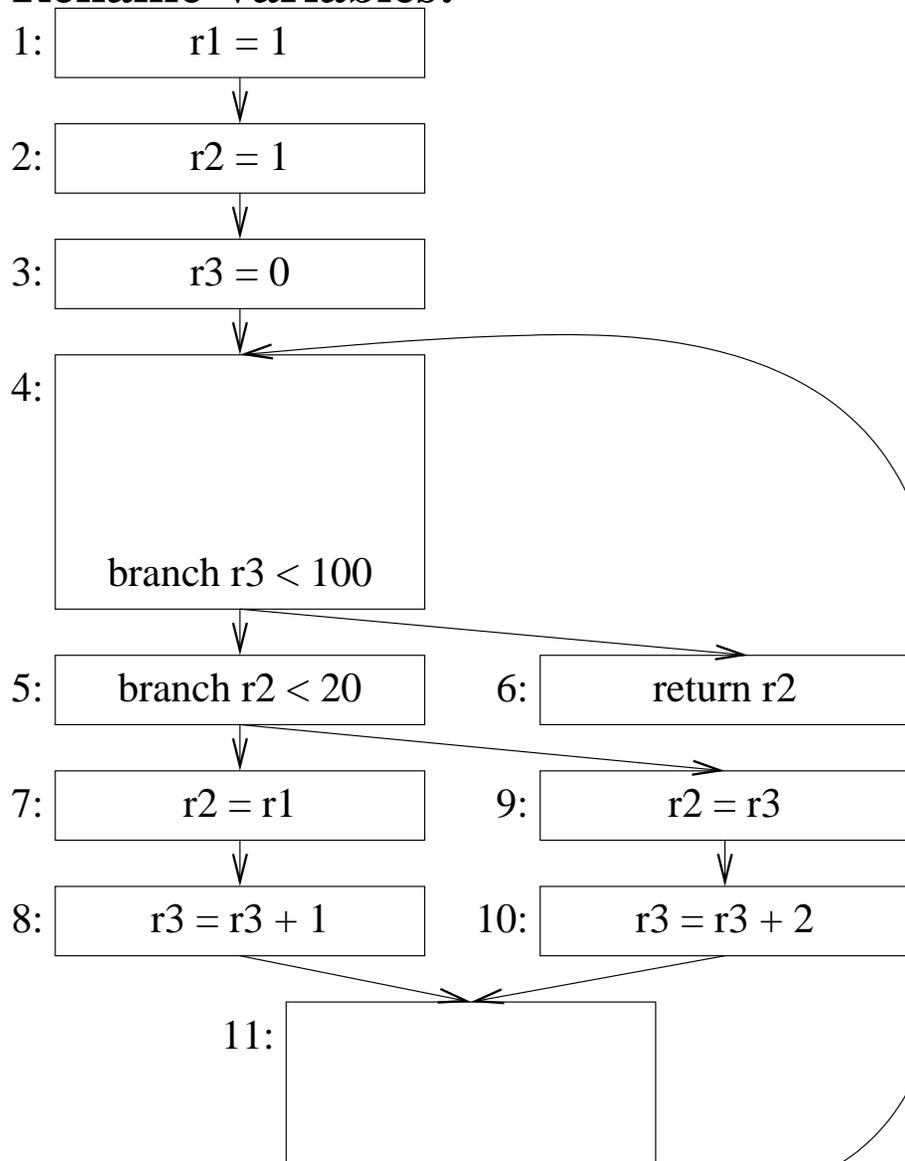
Rename Variables:

1. traverse dominator tree, renaming different definitions of r to $r_1, r_2, r_3 \dots$
2. rename each regular use of r to most recent definition of r
3. rename ϕ -function arguments with each incoming edge's unique definition



Static Single Assignment Example

Rename Variables:



Dominance Property of SSA

Dominance property of SSA form: definitions dominate uses

- If x is i^{th} argument of ϕ -function in node n , then definition of x dominates i^{th} predecessor of n .
- If x is used in non- ϕ statement in node n , then definition of x dominates n .



Dead Code Elimination

Given $d: t = x \text{ op } y$

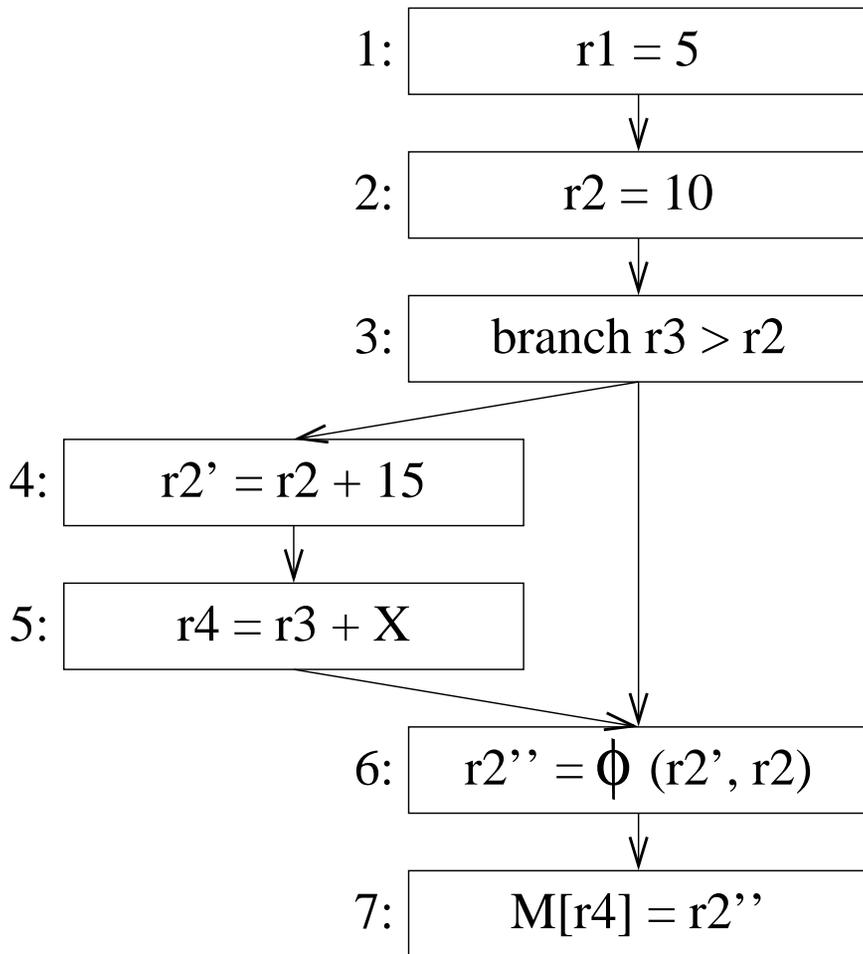
- t is live at end of node d if there exists path from end of d to use of t that does not go through definition of t .
- if program not in SSA form, need to perform liveness analysis to determine if t live at end of d .
- if program is in SSA form:
 - cannot be another definition of t
 - if there exists use of t , then path from end of d to use exists, since definitions dominate uses.
 - * every use has a unique definition
 - * t is live at end of node d if t is used at least once



Dead Code Elimination

Algorithm:

WHILE (for each temporary t with no uses &&
statement defining t has no other side-effects) DO
delete statement definition t



Simple Constant Propagation

Given $d: \tau = c$, c is constant Given $u: x = \tau \text{ op } b$

- if program not in SSA form:
 - need to perform reaching definition analysis
 - use of τ in u may be replaced by c if d reaches u and no other definition of τ reaches u
- if program is in SSA form:
 - d reaches u , since definitions dominate uses, and no other definition of τ exists on path from d to u
 - d is only definition of τ that reaches u , since it is the only definition of τ .
 - * any use of τ can be replaced by c
 - * any ϕ -function of form $v = \phi(c_1, c_2, \dots, c_n)$, where $c_i = c$, can be replaced by $v = c$



Simple Constant Propagation

