

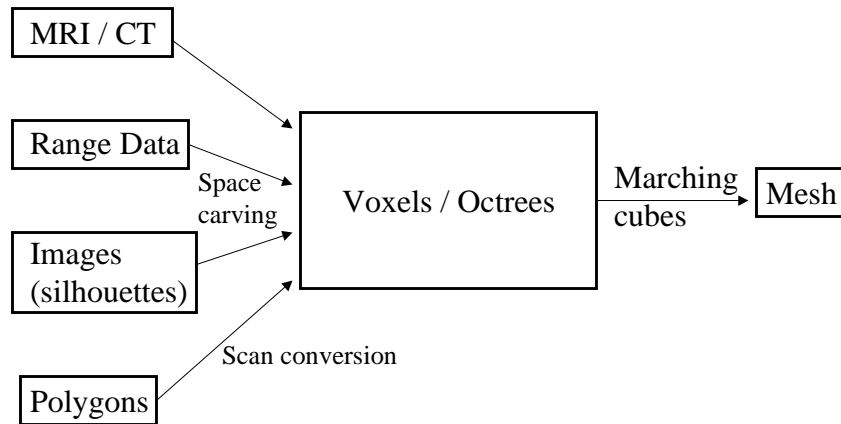
Reconstruction of Voxels from Sensor Data

Geometric Modeling
COS 598d Fall 2000

Volume Representations

- Voxels = uniform, orthogonal grid
 - Binary (empty/full)
 - Float : density / color / distance to surface, etc.
 - 0th (nearest) vs. 1st order (tri-linear) interpolation
 - Can be RLE'd
- Octrees = hierarchical space subdivision
 - cube nodes: black/ white/ gray (split 1-to-8)

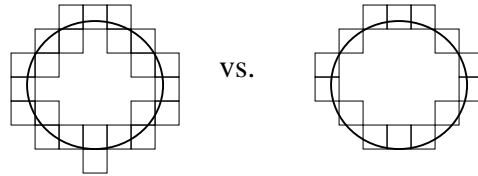
Data acquisition / conversion



3D “Scan-Conversion”

- Binary vs. anti-aliased
- Extension of scanline filling
- Scan-convert boundary, then flood fill

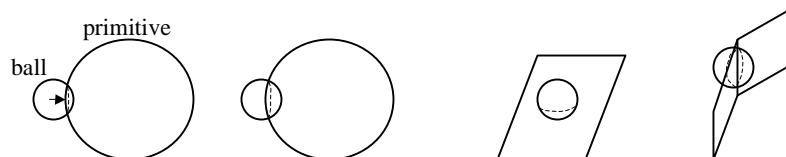
Problems



- “simple” and “separating”
- In 2D: 4/8-adjacency :
neighbors share edges / edges OR vertices
4-connected is 8-separating and vice-versa
- 3D: 6/18/26-adjacency

3D Antialiasing

- [Wang & Kaufman'93]
 - weighted integral of “stuff” inside ball
 - radius 3 voxels => filtering
 - weight function = cone (“hat”)
 - precompute for all primitive types & discrete set of distances



3D Antialiasing

[Oomes et al.'97]

- sample implicit function defined on volume
 - point => gaussian fall-off blob
 - line => “cylinder”, radial e^{-d} fall-off, *erf* for ends
 - triangle =>
$$\frac{\int_0^1 \exp\left(\frac{C^2 - AF + 2s(BF - CD) + s^2(D^2 - EF)}{\sigma^2 F}\right) \left[\operatorname{erf}\left(\frac{-C + sD}{\sigma\sqrt{2F}}\right) - \operatorname{erf}\left(\frac{F - C + s(D - F)}{\sigma\sqrt{2F}}\right) \right] ds}{\int_0^1 \exp\left(\frac{(D^2 - EF)(3s - 1)^2}{18\sigma^2 F}\right) \left[\operatorname{erf}\left(\frac{2F - D + 3s(D - F)}{3\sigma\sqrt{2F}}\right) - \operatorname{erf}\left(\frac{-D - F + 3sD}{3\sigma\sqrt{2F}}\right) \right] ds}$$
- Expensive but solves some problems.

Space Carving

- Done hierarchically using octrees
- Cubes can be “maybe full” / mixed / empty
- Start w/ whole volume presumed full
- “Carve” away portions of “seen” space
- If cube partially empty, subdivide
- Carve 1 level using all views before subdiv.

Octrees from silhouettes

- [Szeliski '93]
 - Map cube to image & see if full
 - Fast test on square bounding box (could use summed area tables too)
 - Subdivide after full rotation
- + Simple & fast
- Result is “line hull”

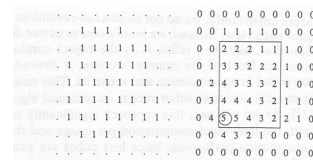
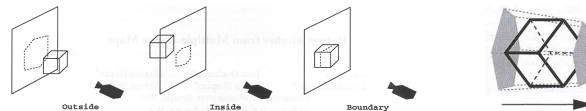


FIG. 2. The half-distance transform and its use in inclusion testing. A sample binary image is shown on the left, and its half-distance transform is on the right. The circled 5 in the distance map indicates that a 5×5 square is the largest square inside the silhouette whose lower left corner is at that pixel.

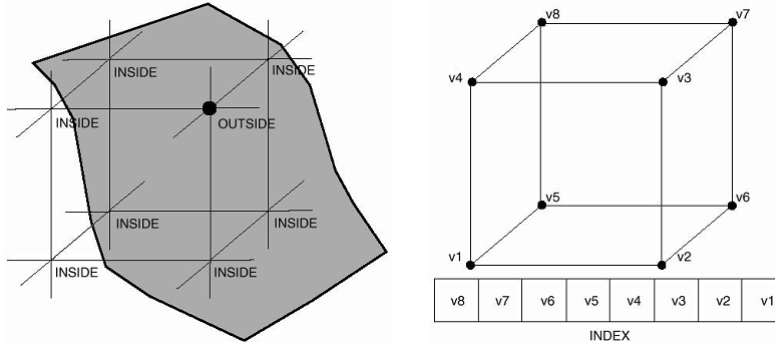
Octrees from range data

- [Pulli et al. '97] Project cubes to depth map

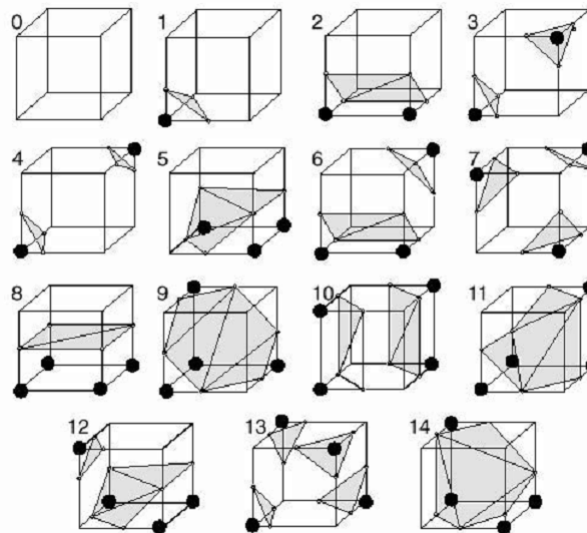


- All points in hex. behind far cube vtx => empty
- If points in hexagon in front => cube inside obj
- Else, cube is boundary (subdivide)
- Can accelerate using 2D min/max quadtrees.
- Hint for voxel grid resolution

Marching Cubes



Cases



Matching up neighboring voxels

