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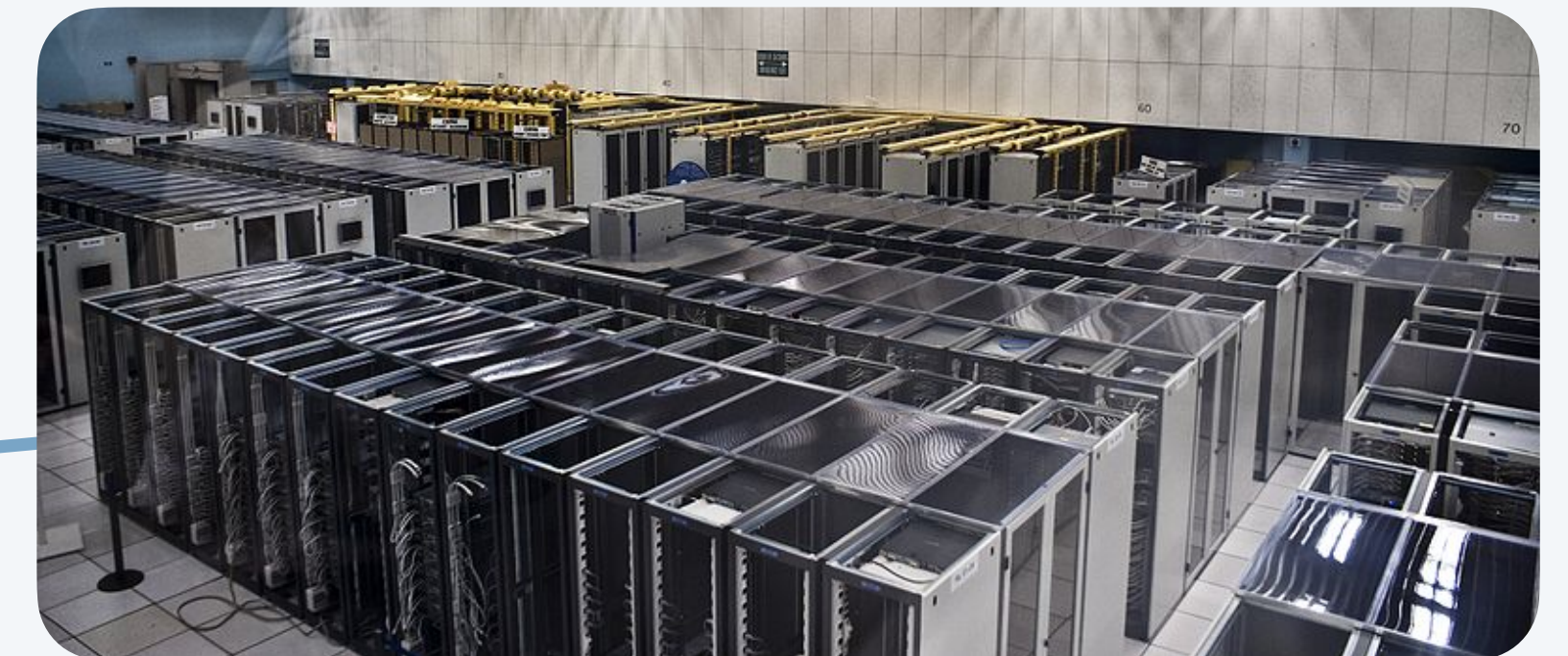
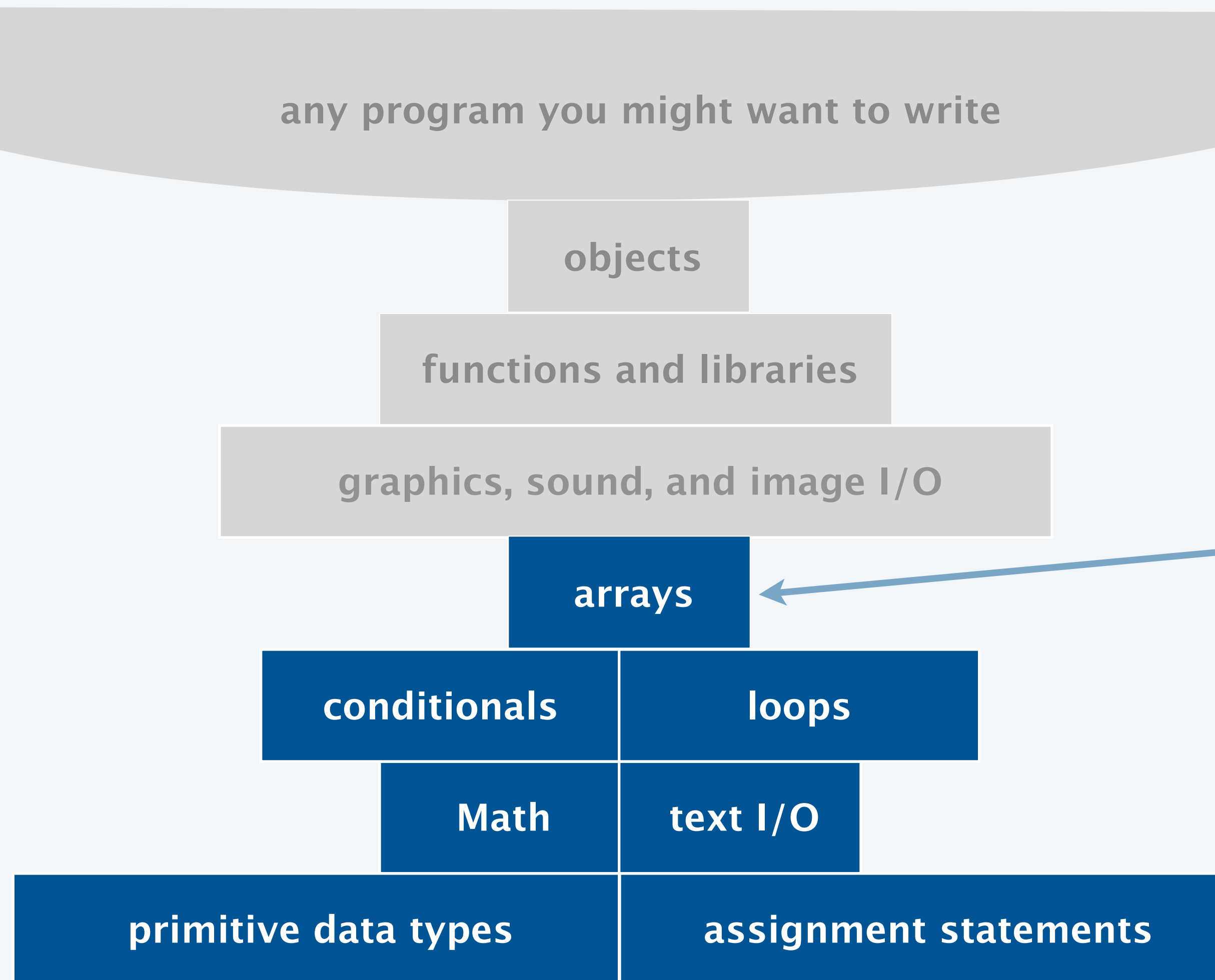
## 1.4 ARRAYS

---

- ▶ *basic concepts*
- ▶ *shuffling*
- ▶ *digital audio*
- ▶ *memory representation*
- ▶ *two-dimensional arrays*

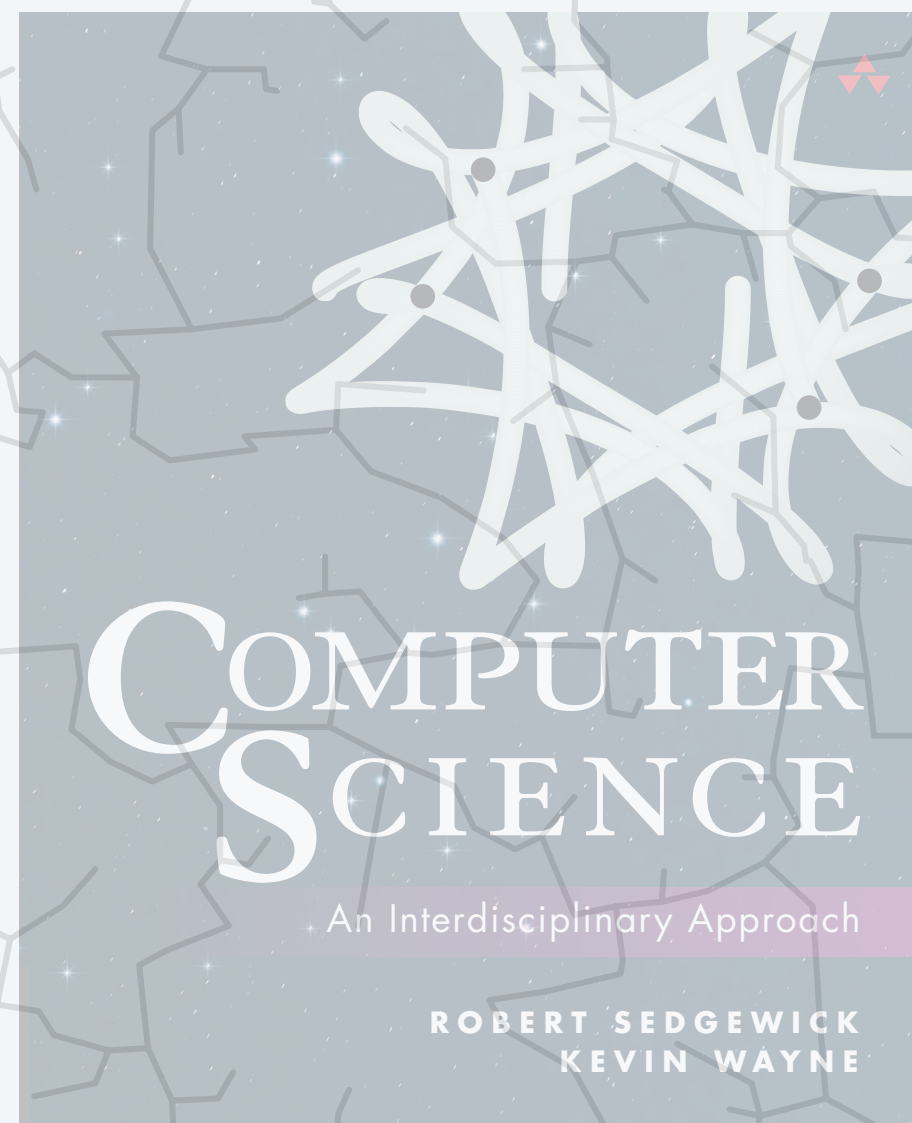
# Basic building blocks for programming

---



*store and process huge amounts of data*





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## 1.4 ARRAYS

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- ▶ *basic concepts*
- ▶ *shuffling*
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- ▶ *two-dimensional arrays*

# Your first data structure

---

An **array** is an *indexed sequence* of values of the same type.

## Examples.

- 8 notes in a musical scale.
- 52 playing cards in a deck.
- 300 students in a COS class.
- 10 million audio samples in a song.
- 4 billion nucleotides in a DNA strand.
- 100 billion Google queries in a month.
- 1 trillion parameters in a large language model.
- ...

index	value
0	2♥
1	6♠
2	A♦
3	A♥
⋮	⋮
49	3♣
50	K♣
51	4♠



**Main purpose.** Facilitate storage and manipulation of data.



# Processing many values of the same type

## 10 values, without an array

```
double a0 = 0.0;
double a1 = 0.0;
double a2 = 0.0;
double a3 = 0.0;
double a4 = 0.0;
double a5 = 0.0;
double a6 = 0.0;
double a7 = 0.0;
double a8 = 0.0;
double a9 = 0.0;
...
a4 = 3.0;
...
a8 = 8.0;
...
double x = a4 + a8;
```

*tedious and error-prone code*

## 10 values, with an array

```
double[] a = new double[10];
...
a[4] = 3.0;
...
a[8] = 8.0;
...
double x = a[4] + a[8];
```

*an easy alternative*

## 1 million values, with an array

```
double[] a = new double[1000000];
...
a[234567] = 3.0;
...
a[876543] = 8.0;
...
double x = a[234567] + a[876543];
```

*scales to handle  
huge amounts of data*

# Arrays in Java

---

Create an array. Specify its type and length.

Access an array element. Use name of array, square brackets, and index.

operation	typical code
<i>declare an array</i>	<code>double[] a;</code>
<i>create an array of length n</i>	<code>a = new double[n];</code>
<i>declare, create, and initialize an array</i>	<code>double[] b = new double[n];</code> ← <i>all elements initialized to default value (zero for numeric types, false for boolean)</i>
<i>array initializer</i>	<code>double[] c = { 0.3, 0.6, 0.1 };</code>
<i>access an array element by index</i>	<code>a[i] = b[i-1] + c[i+1];</code> ← <i>index can be any expression of type int</i>
<i>length of array</i>	<code>a.length</code>



# Examples of programming with arrays

problem	code	
<i>print array elements, one per line</i>	<pre>for (int i = 0; i &lt; a.length; i++)     System.out.println(a[i]);</pre>	← <i>array indices go from 0 to a.length - 1</i>
<i>sum of array elements</i>	<pre>double sum = 0.0; for (int i = 0; i &lt; a.length; i++)     sum = sum + a[i];</pre>	← <i>array elements are variables (can be used in expressions)</i>
<i>create a new array containing n random numbers</i>	<pre>double[] a = new double[n]; for (int i = 0; i &lt; n; i++)     a[i] = Math.random();</pre>	← <i>array elements are variables (can be used as LHS of assignment statement)</i>
<i>command-line arguments</i>	<pre>int time = Integer.parseInt(args[0]); String folder = args[1] + "/";</pre>	← <i>args[] in main() is a String array</i>
<i>months in the year</i>	<pre>String[] months = {     "Jan", "Feb", "Mar", "Apr", "May", "Jun",     "Jul", "Aug", "Sep", "Oct", "Nov", "Dec", }</pre>	← <i>store predefined constants</i>



What are the contents of the array `a[]` after the loop terminates?



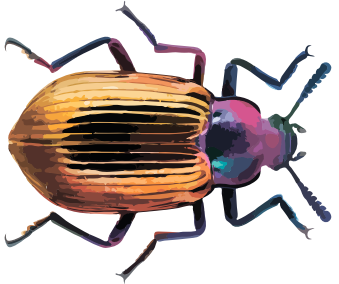
- A. A B C D E
- B. A B C B A
- C. E D C B A
- D. E D C D E

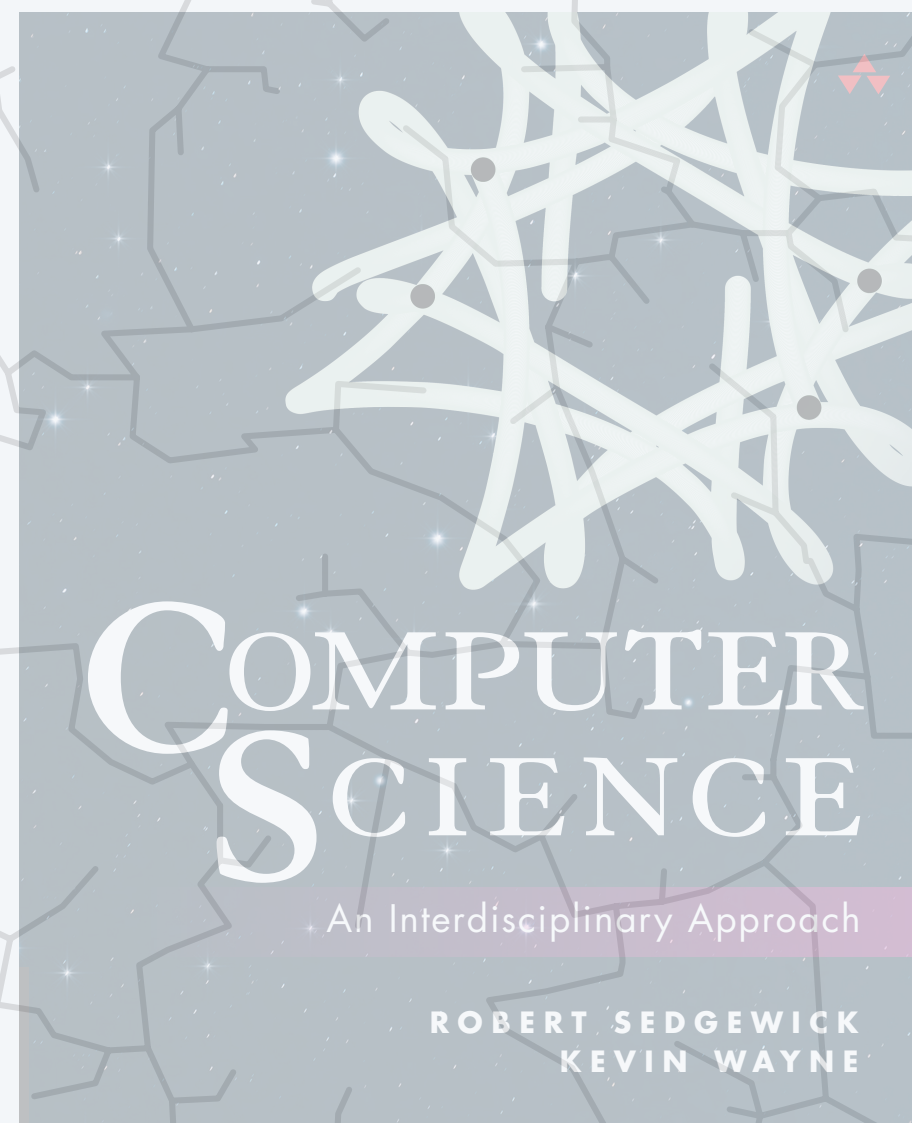
```
String[] a = { "A", "B", "C", "D", "E" };
int n = a.length;
for (int i = 0; i < n; i++) {
    String temp = a[i];
    a[i] = a[n-i-1];
    a[n-i-1] = temp;
}
```

← *swap idiom*



# Programming with arrays: common bugs

bug	buggy code	error	error message
	<pre>double[] a; for (int i = 0; i &lt; 10; i++)     a[i] = Math.random();</pre>	<p><i>uninitialized array</i> (compile-time error)</p>	<pre>~/cos126/arrays&gt; javac ArrayBug1.java ArrayBug1.java:5: error: variable a might not have been initialized     a[i] = Math.random();     ^ 1 error</pre>
	<pre>double[] a = new int[10]; for (int i = 0; i &lt; 10; i++)     a[i] = Math.random();</pre>	<p><i>type mismatch error</i> (compile-time error)</p>	<pre>~/cos126/arrays&gt; javac ArrayBug2.java ArrayBug2.java:3: error: incompatible types: int[] cannot be converted to double[]     double[] a = new int[10];                    ^ 1 error</pre>
	<pre>double[] a = new double[10]; for (int i = 1; i &lt;= 10; i++)     a[i] = Math.random();</pre>	<p><i>array index out of bounds</i> (run-time error)</p>	<pre>~/cos126/arrays&gt; javac ArrayBug3.java ~/cos126/arrays&gt; java ArrayBug3 Exception in thread "main" java.lang.ArrayIndexOutOfBoundsException: Index 10 out of bounds for length 10     at ArrayBug3.java:5)</pre>



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## 1.4 ARRAYS

---

- ▶ *basic concepts*
- ▶ *shuffling*
- ▶ *digital audio*
- ▶ *memory representation*
- ▶ *two-dimensional arrays*



# Create a deck of cards



## Define three arrays:

- Ranks. `String[] ranks = { "2", "3", "4", "5", "6", "7", "8", "9", "10", "J", "Q", "K", "A" };`
- Suits. `String[] suits = { "♣", "♦", "♥", "♠" };`
- Full deck. `String[] deck = new String[52];`



## Use nested for loops to put all cards in the deck.

```
for (int j = 0; j < 4; j++)  
    for (int i = 0; i < 13; i++)  
        deck[i + 13*j] = ranks[i] + suits[j];
```

		suits[]																					
		j																					
		0	1	2	3																		
		♣	♦	♥	♠																		
		ranks[]																					
		i																					
		0	1	2	3	4	5	6	7	8	9	10	11	12									
		2	3	4	5	6	7	8	9	10	J	Q	K	A									
deck[]	0	2♣	3♣	4♣	5♣	6♣	7♣	8♣	9♣	10♣	J♣	Q♣	K♣	A♣	2♦	3♦	4♦	5♦	6♦	7♦	8♦	9♦	...
	1																						
2																							
3																							
4																							
5																							
6																							
7																							
8																							
9																							
10																							
11																							
12																							
13																							
14																							
15																							
16																							
17																							
18																							
19																							
20																							
...																							

# Create a deck of cards

```
public class Deck {
    public static void main(String[] args) {
        String[] ranks = { "2", "3", "4", "5", "6", "7", "8", "9", "10", "J", "Q", "K", "A" };
        String[] suits = { "♣", "♦", "♥", "♠" };

        String[] deck = new String[52];
        for (int j = 0; j < 4; j++)
            for (int i = 0; i < 13; i++)
                deck[i + 13*j] = ranks[i] + suits[j];

        for (int i = 0; i < 52; i++)
            System.out.print(deck[i] + " ");
        System.out.println();
    }
}
```

```
~/cos126/arrays> java Deck
```

```
2♣ 3♣ 4♣ 5♣ 6♣ 7♣ 8♣ 9♣ 10♣ J♣ Q♣ K♣ A♣ 2♦ 3♦ 4♦ 5♦ ... 2♠ 3♠ 4♠ 5♠ 6♠ 7♠ 8♠ 9♠ 10♠ J♠ Q♠ K♠ A♠
```

← *cards in order by suit*





Which code fragment puts the cards in the array in order by rank?

```
~/cos126/arrays> java Deck
```

```
2♣ 2♦ 2♥ 2♠ 3♣ 3♦ 3♥ 3♠ 4♣ 4♦ 4♥ 4♠ 5♣ 5♦ 5♥ 5♠ ... Q♣ Q♦ Q♥ Q♠ K♣ K♦ K♥ K♠ A♣ A♦ A♥
```

A. 

```
for (int i = 0; i < 13; i++)  
    for (int j = 0; j < 4; j++)  
        deck[i + 13*j] = rank[i] + suit[j];
```

B. 

```
for (int i = 0; i < 13; i++)  
    for (int j = 0; j < 4; j++)  
        deck[4*i + j] = rank[i] + suit[j];
```

C. Both A and B.

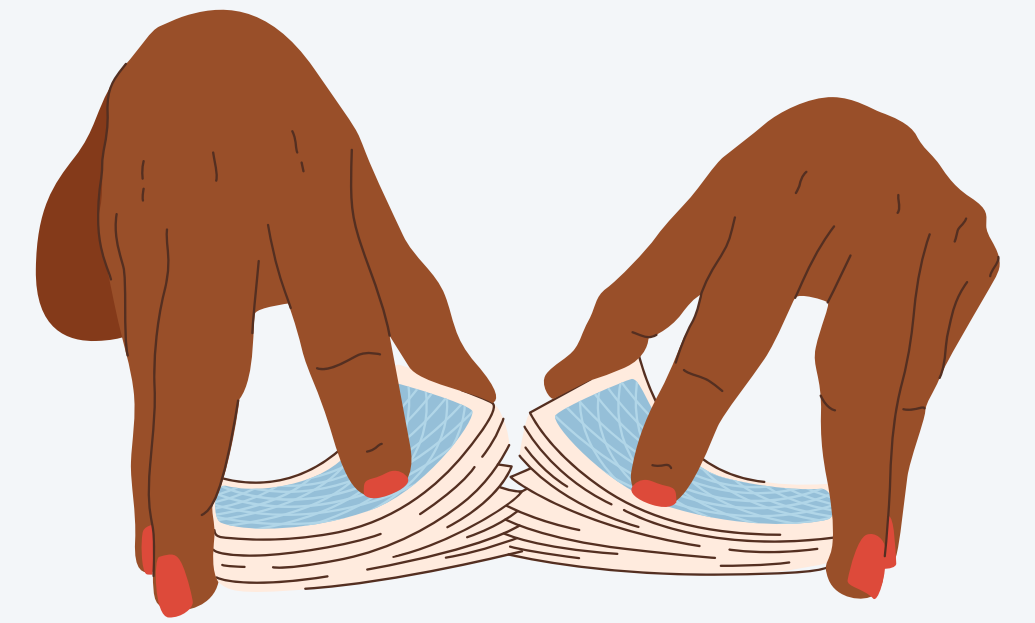
D. Neither A nor B.

# Shuffling

**Goal.** Rearrange deck of cards in uniformly random order.

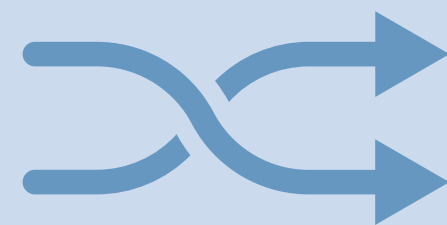
**Algorithm.** For each index  $i$  from 0 to 51 :

- Pick a uniformly random index  $r$  between 0 and  $i$ .
- Exchange `deck[i]` and `deck[r]`.

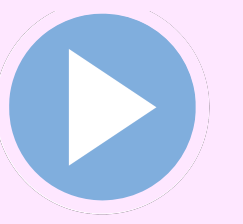


```
for (int i = 0; i < 52; i++) {  
    int r = (int) (Math.random() * (i+1));  
    String temp = deck[r];  
    deck[r] = deck[i];  
    deck[i] = temp;  
}
```

*between 0 and i  
(equally likely)*

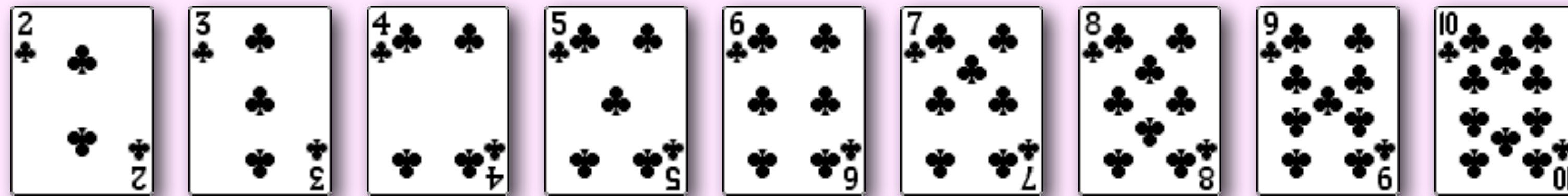


# Shuffling demo



**Algorithm.** For each index  $i$  from 0 to  $n-1$  :

- Pick a uniformly random index  $r$  between 0 and  $i$ .
- Exchange  $a[i]$  and  $a[r]$ .

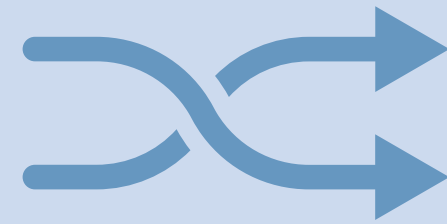




# Shuffling trace



```
for (int i = 0; i < 9; i++) {  
    int r = (int) (Math.random() * (i+1));  
    String temp = deck[r];  
    deck[r] = deck[i];  
    deck[i] = temp;  
}
```



i	r	deck[]								
		0	1	2	3	4	5	6	7	8
		2♣	3♣	4♣	5♣	6♣	7♣	8♣	9♣	10♣
0	0	2♣	3♣	4♣	5♣	6♣	7♣	8♣	9♣	10♣
1	0	3♣	2♣	4♣	5♣	6♣	7♣	8♣	9♣	10♣
2	0	4♣	2♣	3♣	5♣	6♣	7♣	8♣	9♣	10♣
3	2	4♣	2♣	5♣	3♣	6♣	7♣	8♣	9♣	10♣
4	1	4♣	6♣	5♣	3♣	2♣	7♣	8♣	9♣	10♣
5	0	7♣	6♣	5♣	3♣	2♣	4♣	8♣	9♣	10♣
6	4	7♣	6♣	5♣	3♣	8♣	4♣	2♣	9♣	10♣
7	7	7♣	6♣	5♣	3♣	8♣	4♣	2♣	9♣	10♣
8	1	7♣	10♣	5♣	3♣	8♣	4♣	2♣	9♣	6♣
		7♣	10♣	5♣	3♣	8♣	4♣	2♣	9♣	6♣

trace of variables (at end of each iteration)

# Shuffling a deck of cards: implementation

```
public class ShuffledDeck {  
    public static void main(String[] args) {  
        String[] ranks = { "2", "3", "4", "5", "6", "7", "8", "9", "10", "J", "Q", "K", "A" };  
        String[] suits = { "♣", "♦", "♥", "♠" };  
        int RANKS = ranks.length;  
        int SUITS = suits.length;  
        int n = RANKS * SUITS;
```

← *avoid “magic constants”  
(such as 4, 13, and 52)*

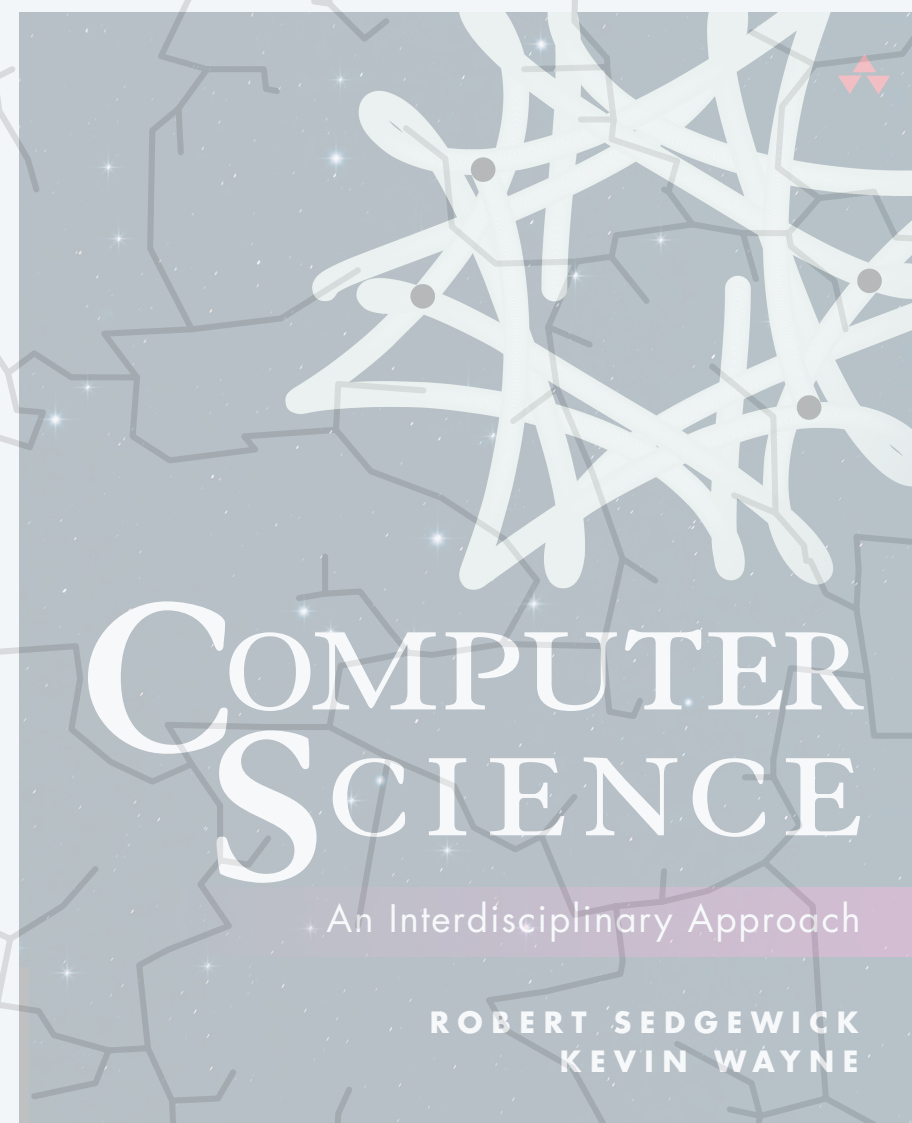
```
        String[] deck = new String[n];           create deck  
        for (int j = 0; j < SUITS; j++)  
            for (int i = 0; i < RANKS; i++)  
                deck[i + RANKS*j] = ranks[i] + suits[j];
```

```
        for (int i = 0; i < n; i++) {  
            int r = (int) (Math.random() * (i+1));  
            String temp = deck[r];  
            deck[r] = deck[i];           shuffle deck  
            deck[i] = temp;  
        }
```

```
        for (int i = 0; i < n; i++)           print deck  
            System.out.print(deck[i] + " ");
```

```
    }  
}
```

```
~/cos126/arrays> java ShuffledDeck  
8♠ A♦ A♥ 9♦ 6♥ 7♥ 9♠ Q♥ ... K♣ 2♣ 6♦ 2♦ 5♥  
  
~/cos126/arrays> java ShuffledDeck  
K♦ J♥ 7♦ 9♦ Q♦ 5♥ 6♥ 9♥ ... Q♥ K♠ 4♦ 6♠ 7♣
```



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## 1.4 ARRAYS

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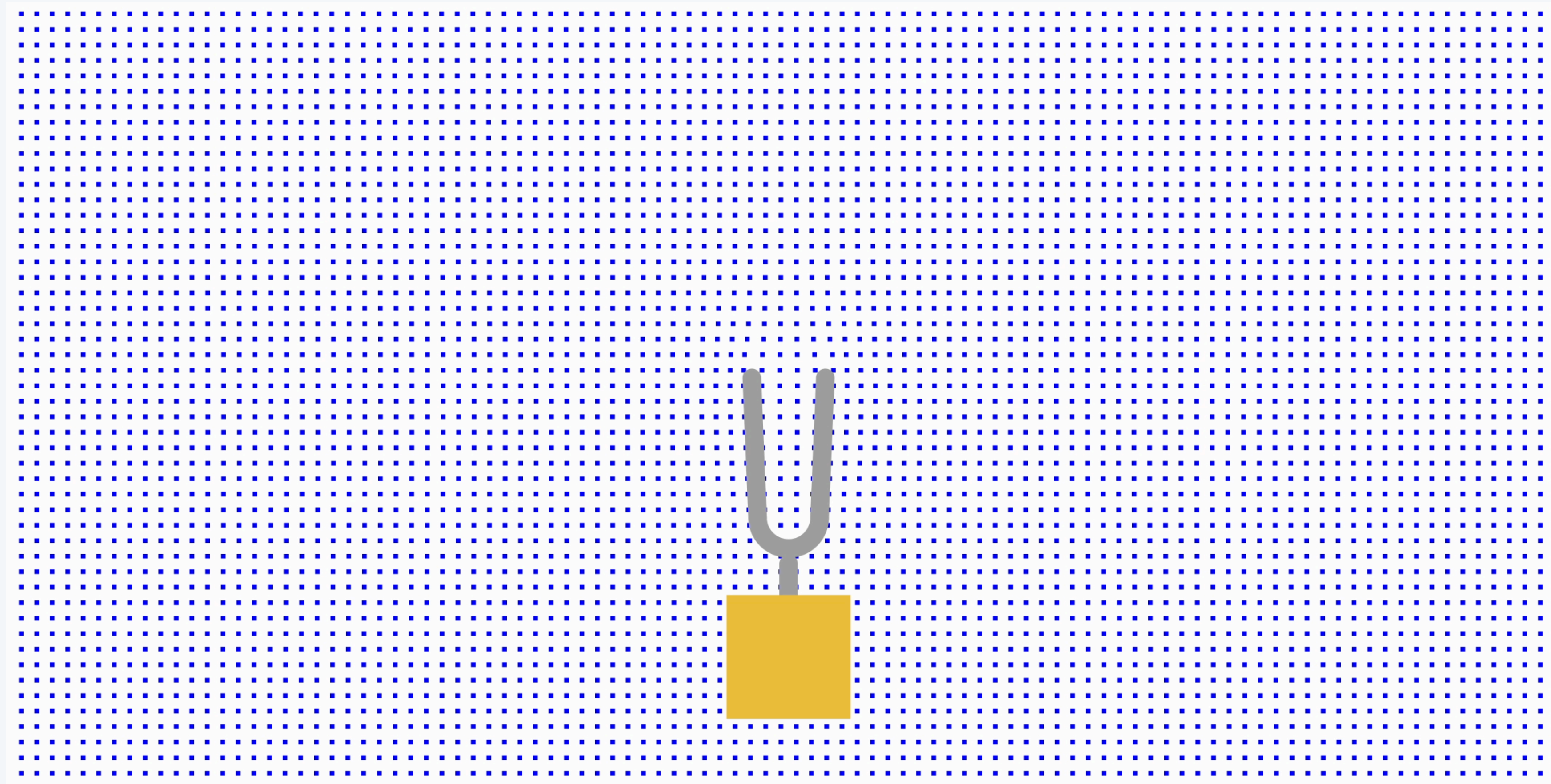
- ▶ *basic concepts*
- ▶ *shuffling*
- ▶ *digital audio*
- ▶ *memory representation*
- ▶ *two-dimensional arrays*







**Sound.** The perceptible vibration of air by the ear.







**Audio.** An analog or digital encoding of sound.

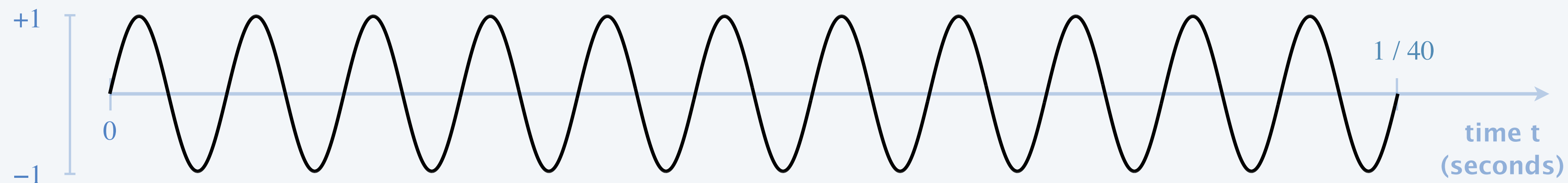
**Audio formats.** Vinyl, tape cassette, CD, WAV, MP3, AIFC, ...

**Audio signal.** Real-valued (between  $-1$  and  $+1$ ) function of time.  $\leftarrow$  *value (amplitude) relates to change in sound pressure*

- A loudspeaker converts an audio signal into sound.
- A microphone converts sound into an audio signal.



amplitude  $y(t)$



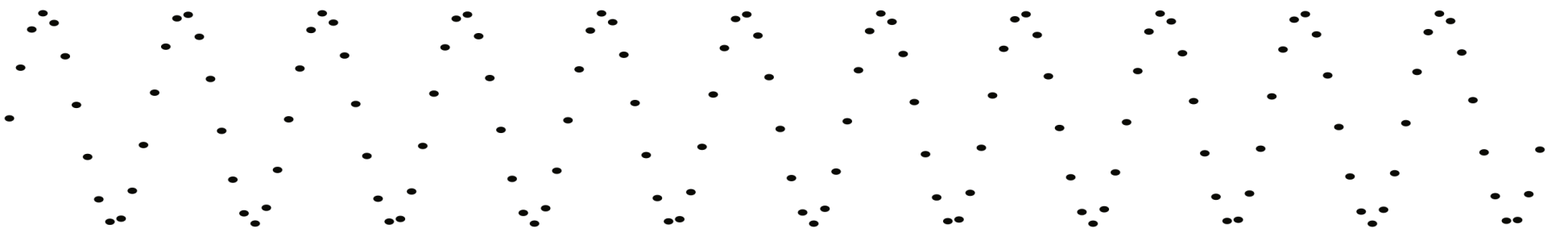
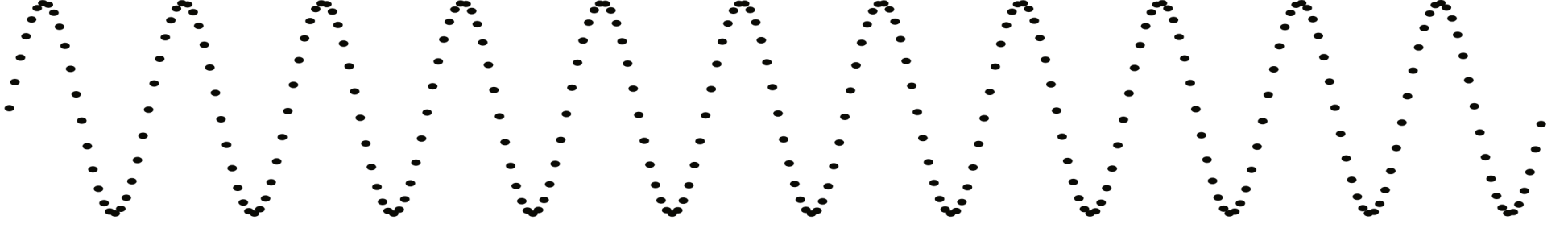
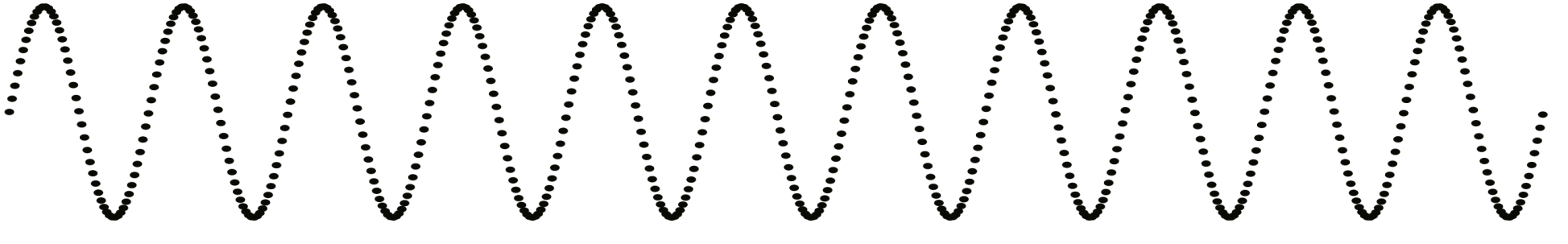
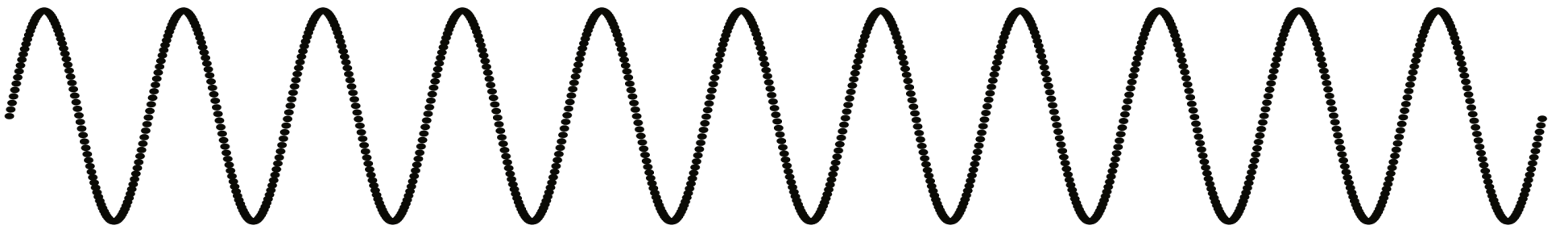
**1/40 second of concert A  
(sine wave with frequency 440 Hz)**

# Audio sampling

**Goal.** Convert a continuous-time signal into a discrete-time signal.

- A **sample** is a signal value at specific point in time.
- Take samples at **evenly spaced points**.

← *model sound with an array of  
real numbers between -1 and +1  
(using 44,100 samples per second)*

samples / second	samples	samples from a sine wave (440 Hz)
5,512	138	
11,025	276	
22,050	552	
44,100	1103	

← *a standard  
sampling rate*

1/40 second of concert A

*StdAudio*. Our library for playing, reading, and saving digital audio.

← available with `javac-introcs`  
and `java-introcs` commands

```
public class StdAudio
```

---

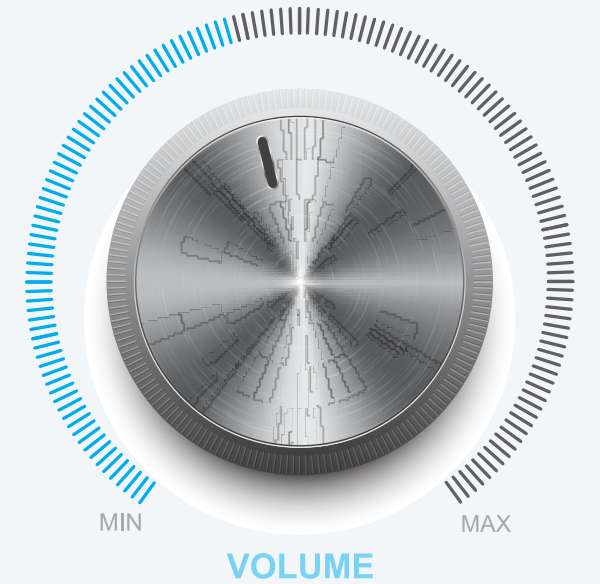
<code>static int</code>	<code>SAMPLE_RATE</code>	44,100 ( <i>CD quality audio</i> )	← 1 hour of audio comprises about 159 million samples
<code>static void</code>	<code>play(String filename)</code>	<i>play the audio file</i>	
<code>static void</code>	<code>playInBackground(String filename)</code>	<i>play the audio file in the background</i>	
<code>static void</code>	<code>play(double sample)</code>	<i>play the sample</i>	
<code>static void</code>	<code>play(double[] samples)</code>	<i>play the samples</i>	
<code>static double[]</code>	<code>read(String filename)</code>	<i>read the samples from an audio file</i>	← supported file formats: WAV, AU, AIFF, MIDI
<code>static void</code>	<code>save(String filename, double[] samples)</code>	<i>save the samples to an audio file</i>	
<code>static void</code>	<code>drain()</code>	<i>play any samples left in buffer</i>	
	<code>⋮</code>	<code>⋮</code>	



**Volume.** Perceived loudness of a sound.

**Audio gain.** Multiply all samples by the same constant  $\alpha$ .

- $|\alpha| > 1 \Rightarrow$  amplifies audio signal.
- $|\alpha| < 1 \Rightarrow$  attenuates audio signal.



```
public class Gain {
    public static void main(String[] args) {
        double[] samples = StdAudio.read(args[0]);
        double alpha = Double.parseDouble(args[1]);

        for (int i = 0; i < samples.length; i++) {
            samples[i] = samples[i] * alpha;
            if (samples[i] > +1.0) samples[i] = +1.0;
            if (samples[i] < -1.0) samples[i] = -1.0;
        }

        StdAudio.play(samples);
    }
}
```

↑  
“clipping”

```
~/cos126/arrays> java-introcs Gain Game.wav 1.0
```

🔊 [plays sound effect]

```
~/cos126/arrays> java-introcs Gain Game.wav 2.0
```

🔊 [plays louder version]

```
~/cos126/arrays> java-introcs Gain Game.wav 0.5
```

🔊 [plays quieter version]

```
~/cos126/arrays> java-introcs Gain Game.wav 0.0
```

🔊 [plays silence]

```
~/cos126/arrays> java-introcs Gain Game.wav -1.0
```

🔊 [plays inverted version]





What sound will the following command produce?

- A. Original audio.
- B. Silence.
- C. Static.
- D. Ear-shattering noise.
- E. None of the above.



```
~/cos126/arrays> java-introcs Gain HelloWorld.wav 9999.99  
🔊 [plays sound with ???]
```

```
double[] samples = StdAudio.read("HelloWorld.wav");  
for (int i = 0; i < samples.length; i++) {  
    if (samples[i] < 0.0) samples[i] = -1.0;  
    else if (samples[i] > 0.0) samples[i] = +1.0;  
}  
StdAudio.play(samples);
```

effectively equivalent to

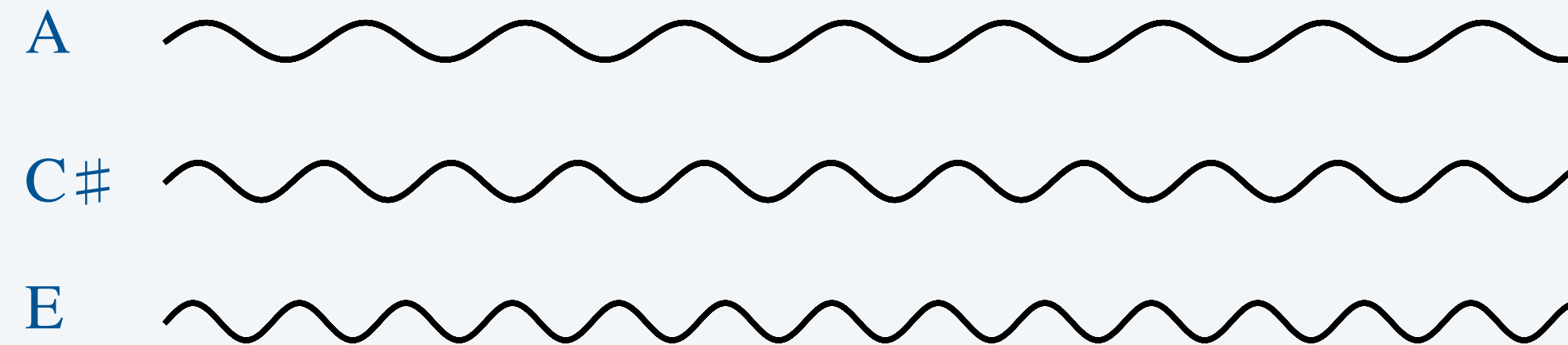
# Principle of superposition



**Superposition.** To combine two (or more) audio signals, **add** the corresponding samples.

*sound waves are mechanical waves*

**Ex 1.** Add audio signals of notes to produce a **chord**.



*A major chord*





**Superposition.** To combine two (or more) audio signals, **add** the corresponding samples.

Ex 1. Add audio signals of notes to produce a chord.

Ex 2. Add audio signals of parts, instruments, and voices to produce a **musical composition**.

♩ = 120

melody

harmony

The image shows a musical score for the song "Twinkle, Twinkle, Little Star". It is written in 4/4 time with a tempo of 120 beats per minute. The score is divided into two parts: "melody" and "harmony". The melody is written on a treble clef staff and consists of a sequence of eighth and quarter notes. The harmony is written on a bass clef staff and consists of chords and single notes. The two parts are combined to form a complete musical composition.

“Twinkle, Twinkle, Little Star”  
(two parts)

# Principle of superposition

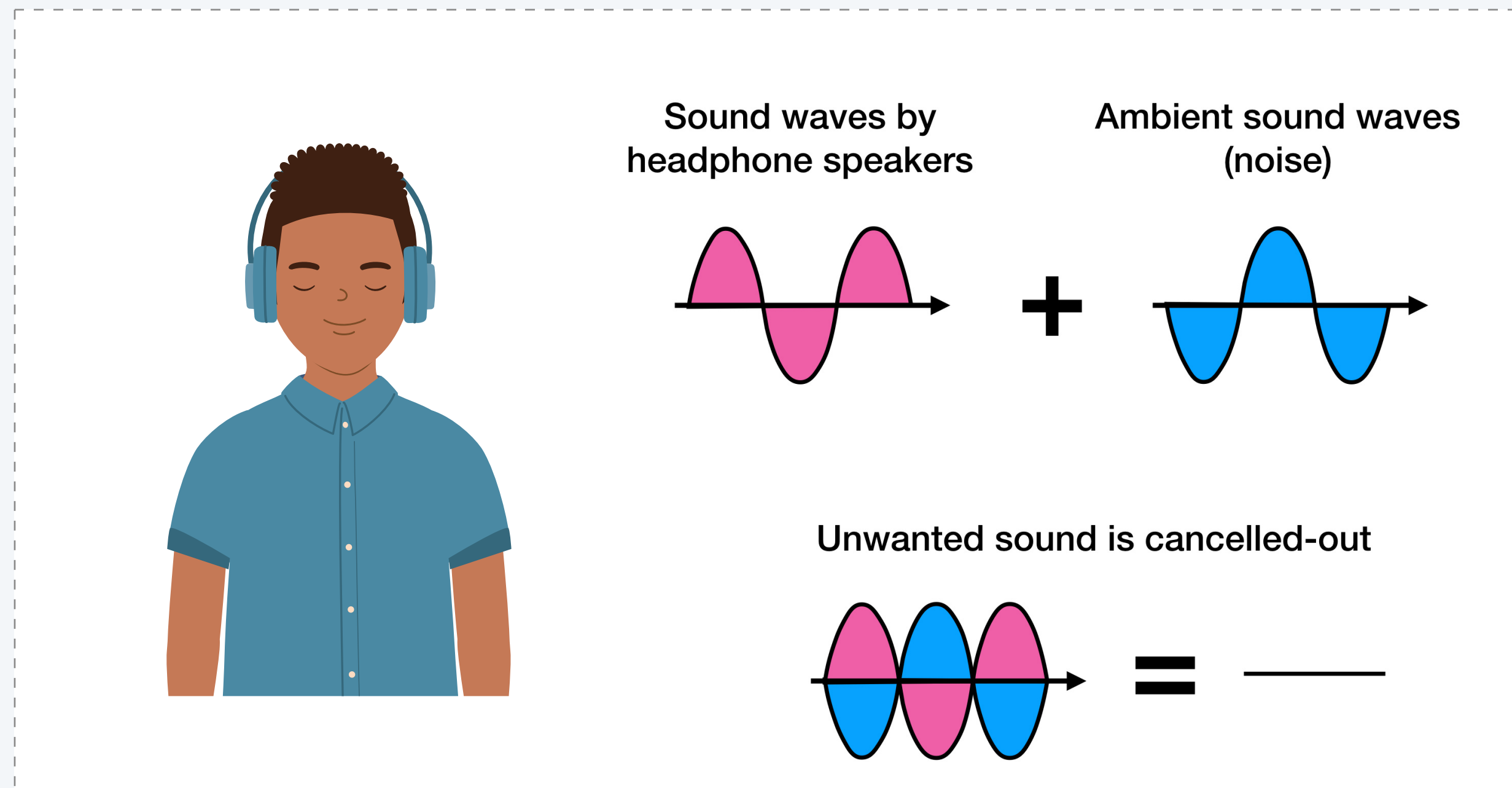
---

**Superposition.** To combine two (or more) audio signals, **add** the corresponding samples.

Ex 1. Add audio signals of notes to produce a chord.

Ex 2. Add audio signals of parts, instruments, and voices to produce a musical composition.

Ex 3. **Noise-cancelling** headphones.





# Superposition of audio files



```
public class Superpose {
    public static void main(String[] args) {
        double[] results = StdAudio.read(args[0]);
        for (int i = 1; i < args.length; i++) {
            double[] samples = StdAudio.read(args[i]);
            for (int j = 0; j < samples.length; j++) {
                results[j] = results[j] + samples[j];
            }
        }
        StdAudio.play(results);
    }
}
```

← args[] in main() is a String array

← use a loop to add the corresponding samples  
(assumes all arrays of same length)

← play the results

```
~/cos126/arrays> java-introcs Superpose PacManMelody.wav
```

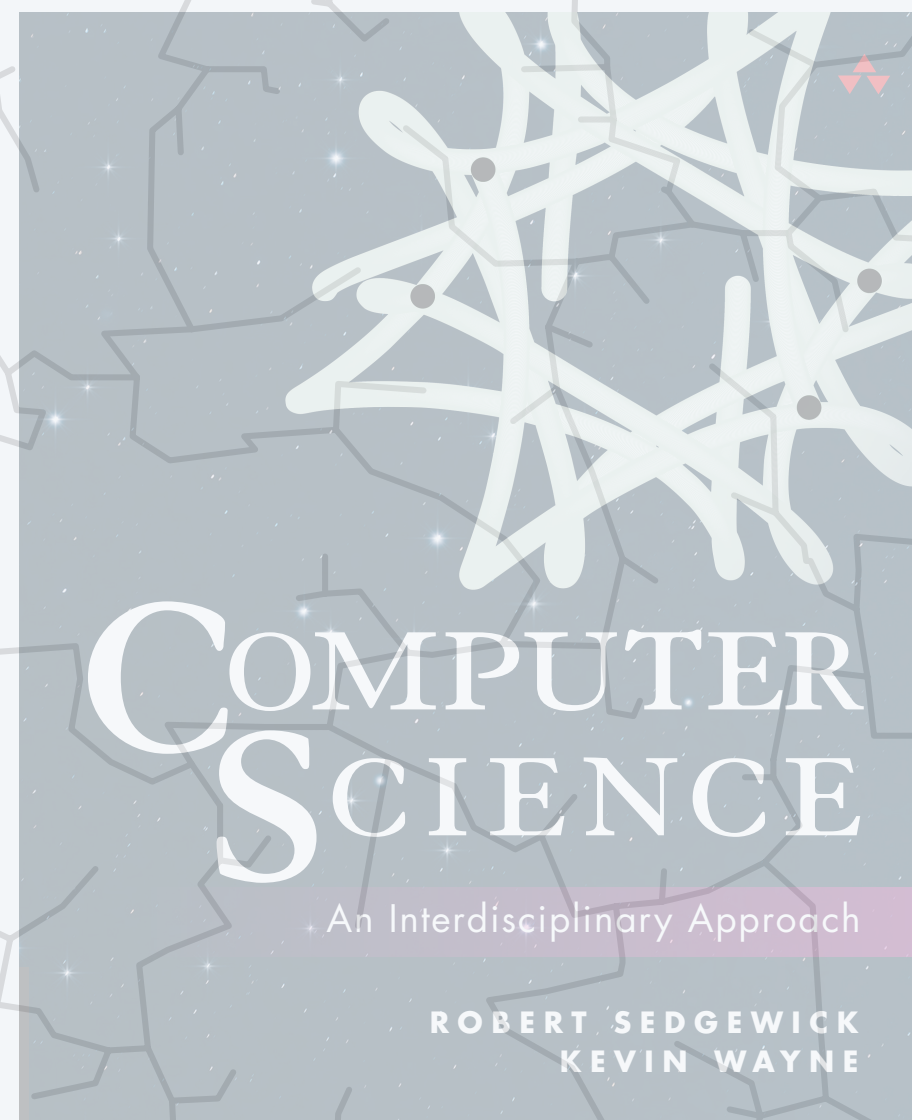
🔊 [plays Pac-Man startup melody]

```
~/cos126/arrays> java-introcs Superpose PacManHarmony.wav
```

🔊 [plays Pac-Man startup harmony]

```
~/cos126/arrays> java-introcs Superpose PacManMelody.wav PacManHarmony.wav
```

🔊 [plays Pac-Man startup melody and harmony]



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## 1.4 ARRAYS

---

- ▶ *basic concepts*
- ▶ *shuffling*
- ▶ *digital audio*
- ▶ ***memory representation***
- ▶ *two-dimensional arrays*

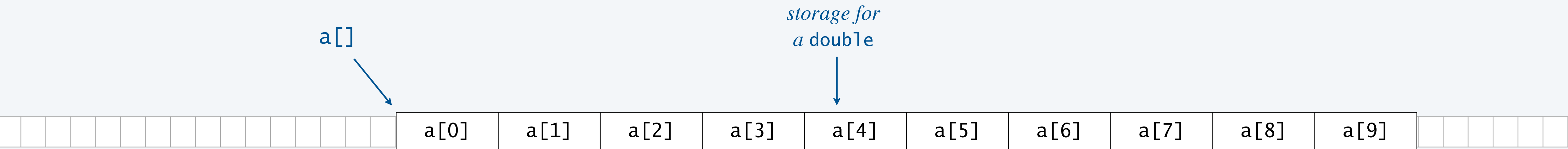
# Memory representation of an array

---

**Java array.** An array is an **indexed** sequence of values of the same type.

**Computer memory.** Your computer's memory is an **indexed** sequence of memory locations.

- Each *int*, *double*, or *boolean* occupies a fixed number of memory locations.
- Array elements are stored in contiguous memory locations.



## Key properties.

- Given index *i*, accessing *a[i]* is extremely efficient.
- Once you create an array, you can never change its type or length.
- Arrays are **reference types**, not primitive types.

*think of the variable a[] as storing the memory address of its first element*

# Assignment statements with arrays

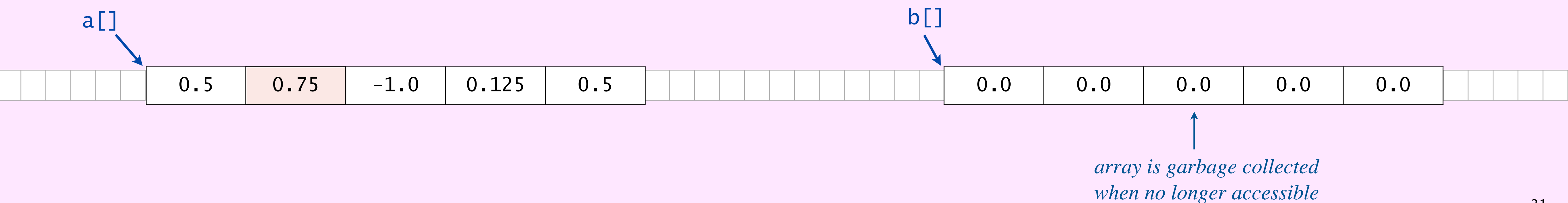


Consequence 1. The assignment statement  $b = a$  makes  $a$  and  $b$  refer to the **same array**.

Ex.

↑  
*it does not create a new,  
independent, array*

```
double[] a = { 0.5, 0.25, -1.0, 0.125, 0.5 };  
double[] b = new double[a.length];  
b = a;  
b[1] = 0.75;
```



# Checking arrays for equality

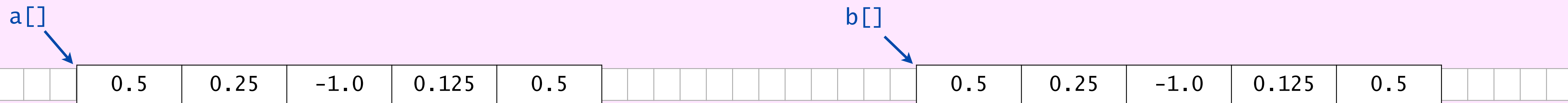


Consequence 2. The expression `a == b` checks whether `a` and `b` refer to the **same array**.

Ex.

```
double[] a = { 0.5, 0.25, -1.0, 0.125, 0.5 };  
double[] b = { 0.5, 0.25, -1.0, 0.125, 0.5 };  
System.out.println(a == b); // false
```

↑  
*not whether they store  
the same sequence of values*







# Copying an array and checking for equality

Q. How to copy an array and check for equality?

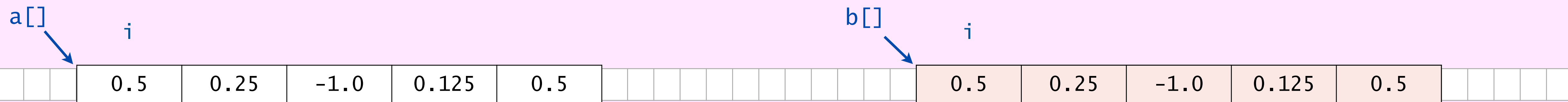
A. Use loops.

```
double[] a = { 0.5, 0.25, -1.0, 0.125, 0.5 };  
double[] b = new double[a.length];  
for (int i = 0; i < a.length; i++)  
    b[i] = a[i];
```

copying an array

```
boolean areEqual = true;  
for (int i = 0; i < a.length; i++) {  
    if (a[i] != b[i])  
        areEqual = false;  
}
```

checking two arrays (of same length) for equality

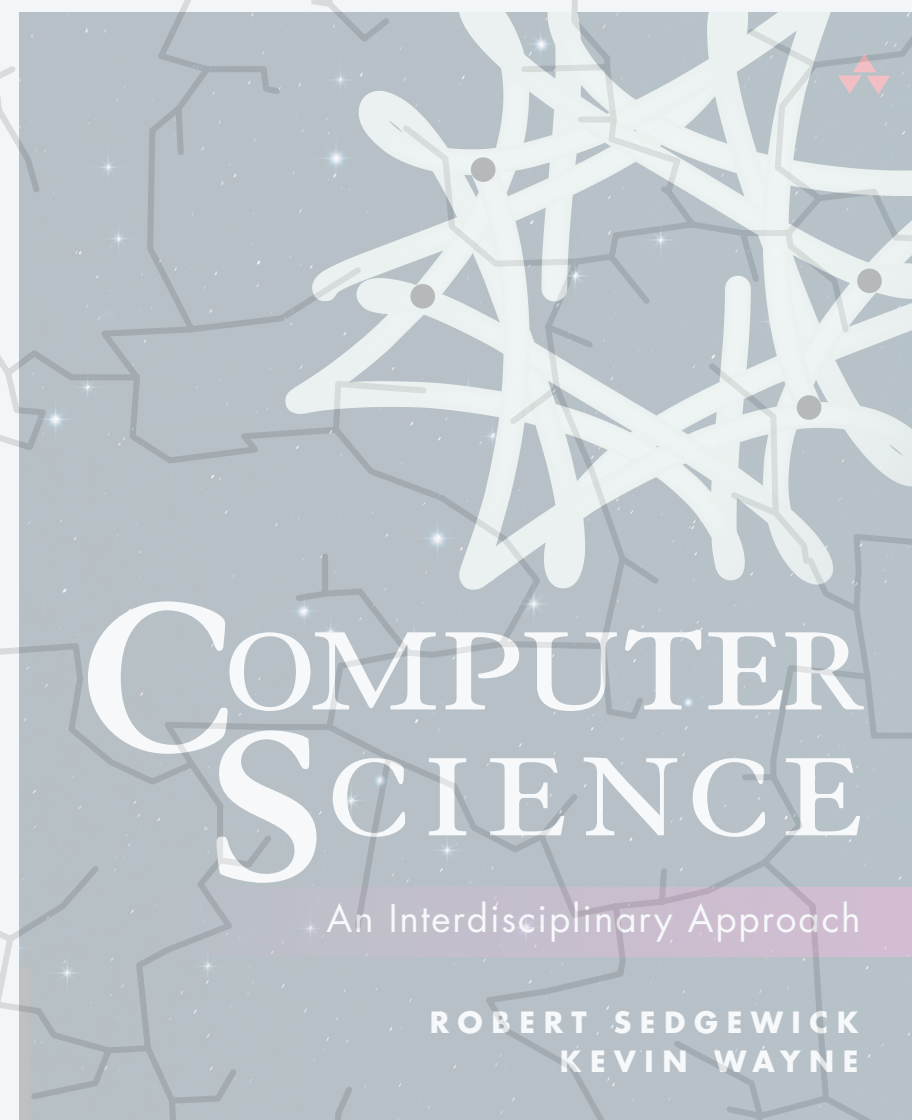




What does the following code fragment print?

- A. 0 1 2 0 1 2
- B. 0 1 2 1 2 6
- C. 1 2 6 0 1 2
- D. 1 2 6 1 2 6

```
int[] a = { 1, 2, 6 };  
int[] b = new int[a.length];  
  
b = a;  
for (int i = 0; i < b.length; i++)  
    b[i] = i;  
  
for (int i = 0; i < a.length; i++)  
    System.out.print(a[i] + " ");  
  
for (int i = 0; i < b.length; i++)  
    System.out.print(b[i] + " ");
```



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## 1.4 ARRAYS

---

- ▶ *basic concepts*
- ▶ *shuffling*
- ▶ *digital audio*
- ▶ *memory representation*
- ▶ *two-dimensional arrays*

# Two-dimensional arrays

A **two-dimensional array** is a *doubly-indexed* table of values of the same type.

## Examples.

- Grades for students in an online class.
- Outcomes of a scientific experiment.
- Customer transactions in a bank.
- Entries in a feature matrix.
- Pixels in a digital image.
- Cells in a spreadsheet.
- ...

	<i>grade</i>						
	0	1	2	3	4	5	...
<i>student ID</i>	0	A	A	C	B	A	C
1	B	B+	B	B-	A	A-	
2	C	D	D	B	C	A	
3	A	A+	A	A-	A	A+	
4	C	C	B+	C	B	B-	
⋮							



*column index*

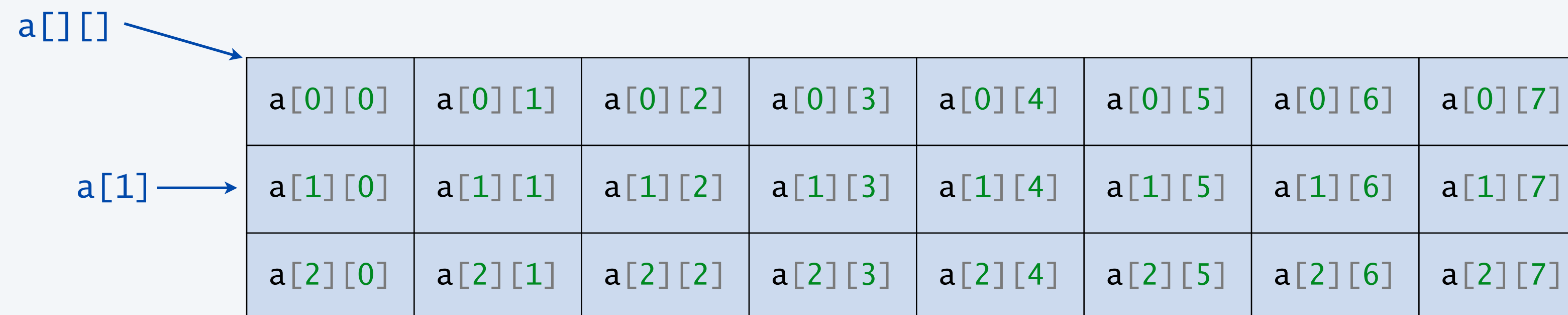


# Two-dimensional arrays in Java

operation	typical code
<i>declare a two-dimensional array</i>	<code>double[][] a;</code>
<i>create an m-by-n array</i>	<code>a = new double[m][n];</code>
<i>declare, create, and initialize in one statement</i>	<code>double[][] a = new double[m][n];</code>
<i>refer to an array element by index</i>	<code>a[i][j] = b[i][j] + c[j][k];</code>
<i>number of rows</i>	<code>a.length</code>
<i>number of columns</i>	<code>a[i].length</code>

*all elements initialized to default value  
(zero for numeric types, false for boolean)*

*can be different for each row  
("ragged" array)*



*same conventions  
as matrices*

**a 3-by-8 array**



# Vector and matrix calculations

Mathematical abstractions. Vectors and matrices.

Java implementation. 1D arrays and 2D arrays.

Scalar	Vector	Matrix
1	$\begin{bmatrix} 1 \\ 2 \end{bmatrix}$	$\begin{bmatrix} 1 & 2 \\ 3 & 4 \end{bmatrix}$

## vector addition

```
double[] c = new double[n];  
for (int i = 0; i < n; i++)  
    c[i] = a[i] + b[i];
```

## matrix addition

```
double[][] c = new double[n][n];  
for (int i = 0; i < n; i++)  
    for (int j = 0; j < n; j++)  
        c[i][j] = a[i][j] + b[i][j];
```

$$\underline{\underline{\begin{pmatrix} 0.8 & 0.7 & 0.5 \end{pmatrix}}} = \underline{\underline{\begin{pmatrix} 0.3 & 0.6 & 0.1 \end{pmatrix}}} + \underline{\underline{\begin{pmatrix} 0.5 & 0.1 & 0.4 \end{pmatrix}}}$$

*c*                      *a*                      *b*

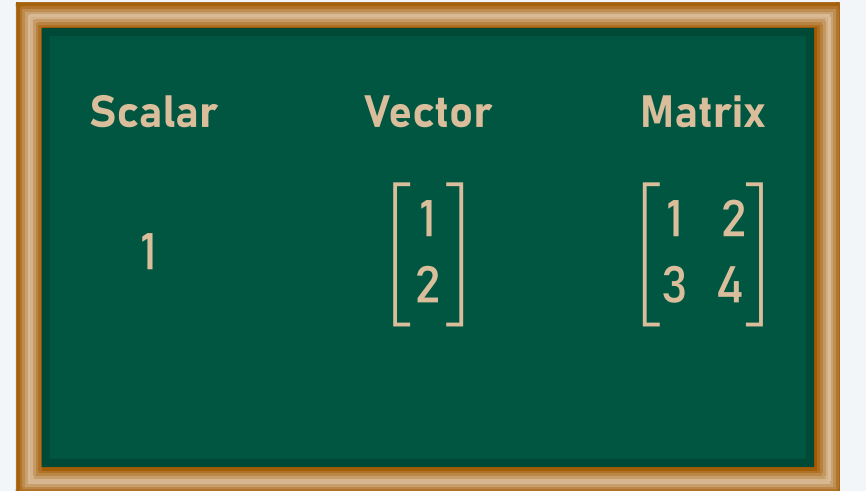
$$\underline{\underline{\begin{bmatrix} 1.5 & 0.5 & 0.6 \\ 0.4 & 1.0 & 0.2 \\ 0.6 & 0.4 & 0.8 \end{bmatrix}}} = \underline{\underline{\begin{bmatrix} 0.7 & 0.2 & 0.1 \\ 0.3 & 0.6 & 0.1 \\ 0.5 & 0.1 & 0.4 \end{bmatrix}}} + \underline{\underline{\begin{bmatrix} 0.8 & 0.3 & 0.5 \\ 0.1 & 0.4 & 0.1 \\ 0.1 & 0.3 & 0.4 \end{bmatrix}}}$$

*C*                      *A*                      *B*

# Vector and matrix calculations

Mathematical abstractions. Vectors and matrices.

Java implementation. 1D arrays and 2D arrays.



## vector dot product

```
double sum = 0.0;
for (int i = 0; i < n; i++)
    sum += a[i] * b[i];
```

$$0.25 = \underline{(0.3, 0.6, 0.1)} \cdot \underline{(0.5, 0.1, 0.4)}$$

*a*

*b*

<i>i</i>	<i>a</i> [ <i>i</i> ]	<i>b</i> [ <i>i</i> ]	<i>a</i> [ <i>i</i> ]* <i>b</i> [ <i>i</i> ]	sum
0	0.3	0.5	0.15	0.15
1	0.6	0.1	0.06	0.21
2	0.1	0.4	0.04	0.25

## matrix multiplication

```
double[][] c = new double[n][n];
for (int i = 0; i < n; i++)
    for (int j = 0; j < n; j++)
        for (int k = 0; k < n; k++)
            c[i][j] += a[i][k] * b[k][j];
```

$$\begin{bmatrix} 0.59 & 0.32 & 0.41 \\ 0.31 & 0.36 & 0.25 \\ 0.45 & 0.31 & 0.42 \end{bmatrix} = \begin{bmatrix} 0.7 & 0.2 & 0.1 \\ 0.3 & 0.6 & 0.1 \\ 0.5 & 0.1 & 0.4 \end{bmatrix} \times \begin{bmatrix} 0.8 & 0.3 & 0.5 \\ 0.1 & 0.4 & 0.1 \\ 0.1 & 0.3 & 0.4 \end{bmatrix}$$

*C*                      *A*                      *B*

# Summary

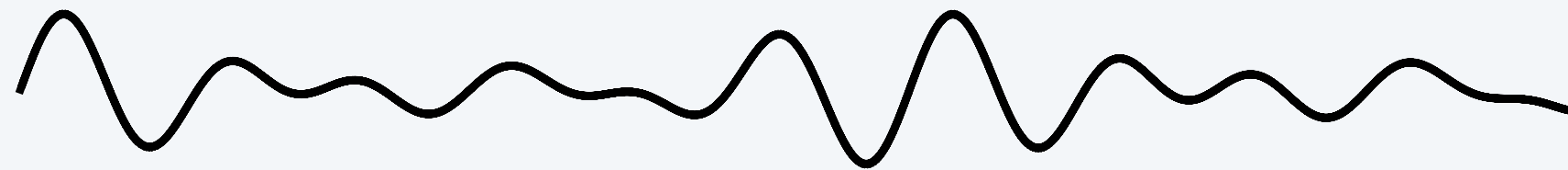
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An **array** is an *indexed sequence* of values of the same type.

- Serves as a basic building block in programming.
- Enables efficient manipulation of large amounts of data.

Some examples. [in this course]

digital audio signal



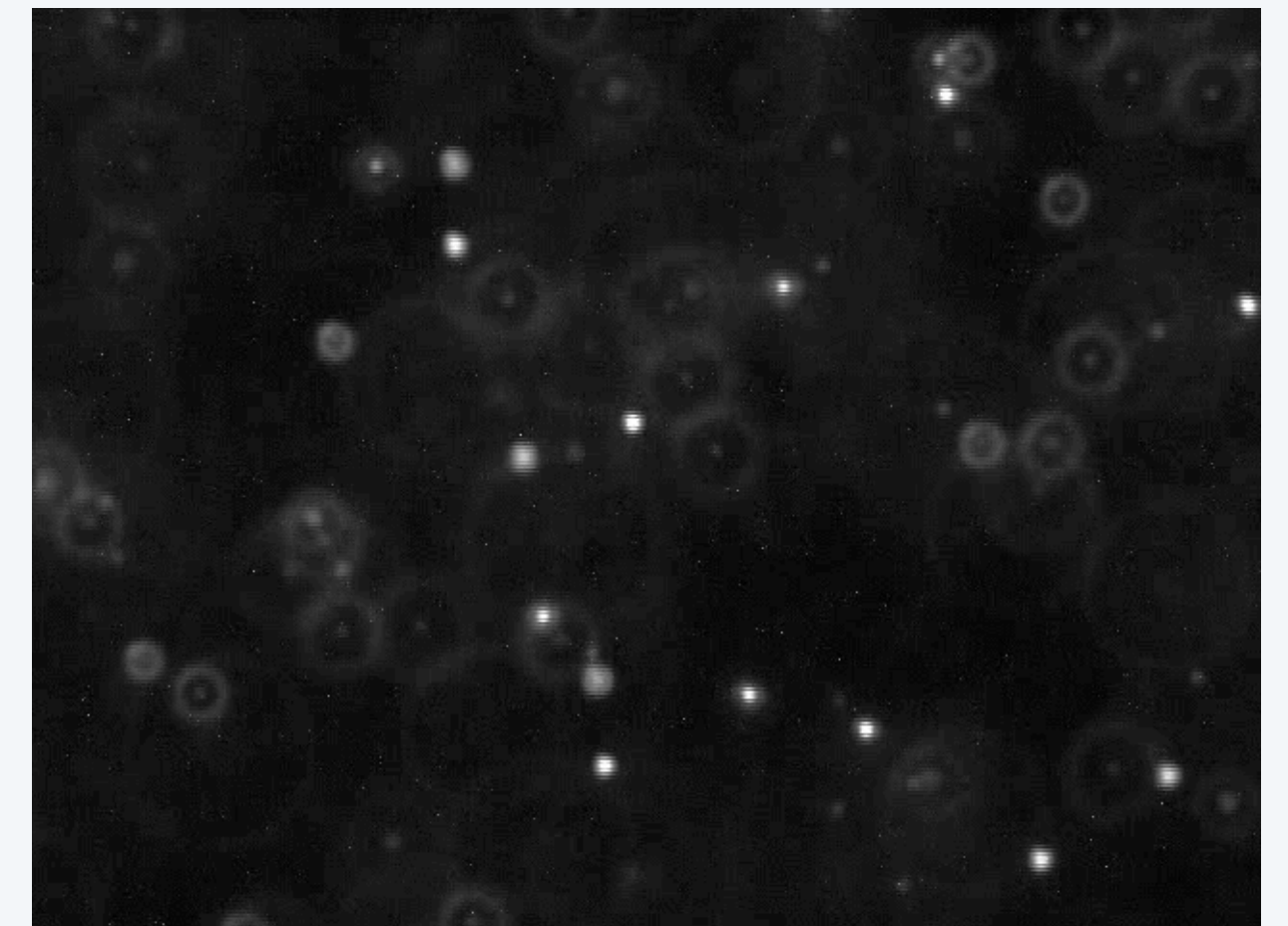
DNA string

T	A	G	A	T	G	T	G	C	T	A	G	C
---	---	---	---	---	---	---	---	---	---	---	---	---

digital image



digital video





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