OCaml Datatypes

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OCaml So Far

- We have seen a number of basic types:
 - int
 - float
 - char
 - string
 - bool
- We have seen a few structured types:
 - pairs
 - tuples
 - options
 - lists
- In this lecture, we will see some more general ways to define our own new types and data structures

• We have already seen some type abbreviations:

type point = float * float

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```
type point = float * float
```

• These abbreviations can be helpful documentation:

```
let distance (p1:point) (p2:point) : float =
    let square x = x *. x in
    let (x1,y1) = p1 in
    let (x2,y2) = p2 in
    sqrt (square (x2 -. x1) +. square (y2 -. y1))
```

But they add nothing of *substance* to the language
 they are equal in every way to an existing type

• We have already seen some type abbreviations:

```
type point = float * float
```

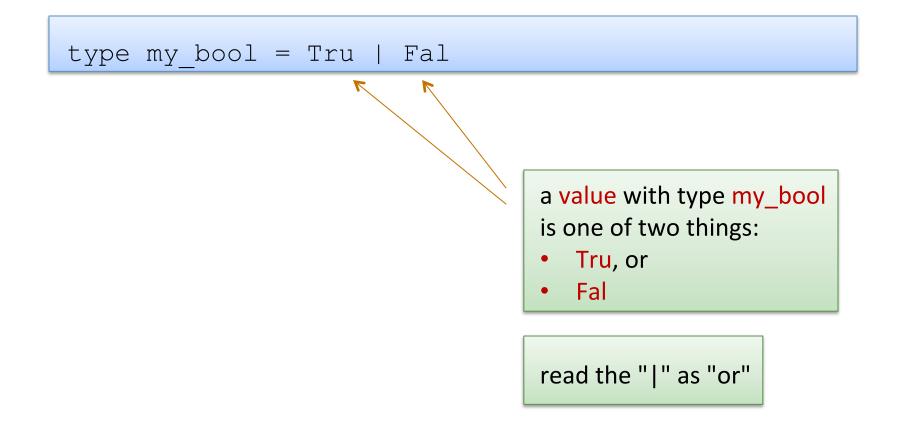
• As far as OCaml is concerned, you could have written:

```
let distance (p1:float*float)
        (p2:float*float) : float =
    let square x = x *. x in
    let (x1,y1) = p1 in
    let (x2,y2) = p2 in
    sqrt (square (x2 -. x1) +. square (y2 -. y1))
```

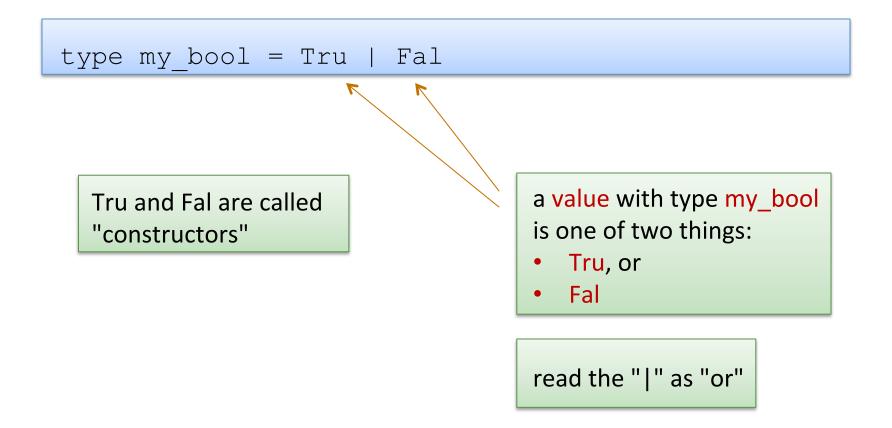
- Since the types are equal, you can *substitute* the definition for the name wherever you want
 - we have not added any new data structures

DATA TYPES

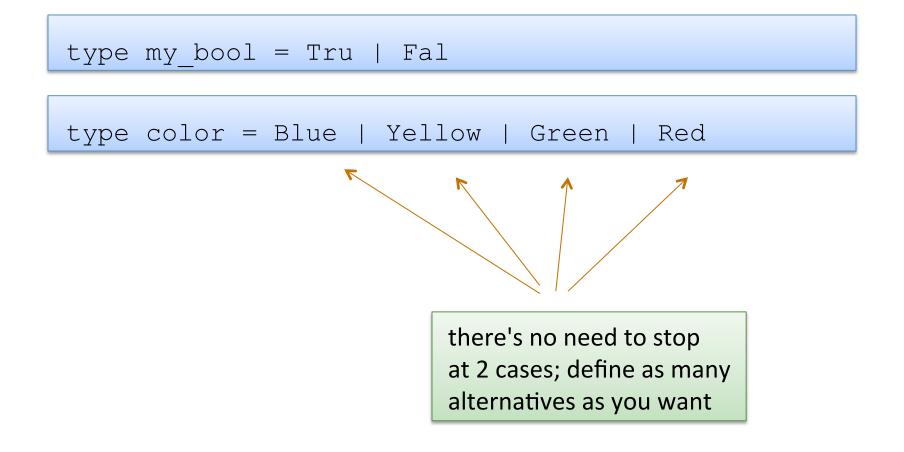
• OCaml provides a general mechanism called a data type for defining new data structures that consist of many alternatives



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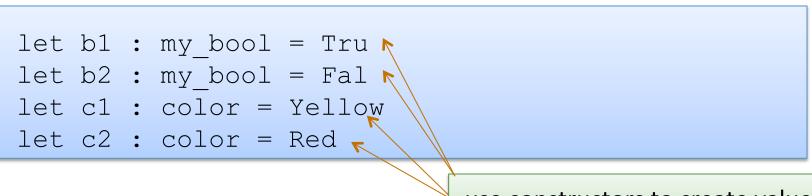


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 OCaml provides a general mechanism called a data type for defining new data structures that consist of many alternatives

• Creating values:



10

```
type color = Blue | Yellow | Green | Red
let c1 : color = Yellow
let c2 : color = Red
```

• Using data type values:

```
let print_color (c:color) : unit =
  match c with
  | Blue ->
  | Yellow ->
  | Green ->
  | Red ->
```

use pattern matching to determine which color you have; act accordingly 11

```
type color = Blue | Yellow | Green | Red
let c1 : color = Yellow
let c2 : color = Red
```

• Using data type values:

```
let print_color (c:color) : unit =
  match c with
  | Blue -> print_string "blue"
  | Yellow -> print_string "yellow"
  | Green -> print_string "green"
  | Red -> print_string "red"
```

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type color = Blue | Yellow | Green | Red
let c1 : color = Yellow
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• Using data type values:

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let print_color (c:color) : unit =
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  | Blue -> print_string "blue"
  | Yellow -> print_string "yellow"
  | Green -> print_string "green"
  | Red -> print_string "red"
```

Why not just use strings to represent colors instead of defining a new type?

type color = Blue | Yellow | Green | Red

oops!:

```
let print_color (c:color) : unit =
  match c with
  | Blue -> print_string "blue"
  | Yellow -> print_string "yellow"
  | Red -> print_string "red"
```

Warning 8: this pattern-matching is not exhaustive. Here is an example of a value that is not matched: Green 14

type color = Blue | Yellow | Green | Red

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let print_color (c:color) : unit =
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Warning 8: this pattern-matching is not exhaustive. Here is an example of a value that is not matched: Green

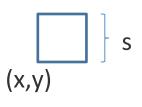
OCaml's datatype mechanism allow you to create types that contain *precisely* the values you want! 15

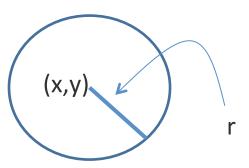
Data Types Can Carry Additional Values

• Data types are more than just enumerations of constants:

```
type point = float * float
type simple_shape =
  Circle of point * float
| Square of point * float
```

- Read as: a simple_shape is either:
 - a Circle, which contains a pair of a point and float, or
 - a Square, which contains a pair of a point and float





Data Types Can Carry Additional Values

• Data types are more than just enumerations of constants:

```
type point = float * float
type simple_shape =
  Circle of point * float
| Square of point * float
let origin : point = (0.0, 0.0)
let circ1 : simple_shape = Circle (origin, 1.0)
let circ2 : simple_shape = Circle ((1.0, 1.0), 5.0)
let square : simple_shape = Square (origin, 2.3)
```

Data Types Can Carry Additional Values

• Data types are more than just enumerations of constants:

```
type point = float * float
type simple_shape =
  Circle of point * float
! Square of point * float
let simple_area (s:simple_shape) : float =
  match s with
  | Circle (_, radius) -> 3.14 *. radius *. radius
  | Square (_, side) -> side *. side
```

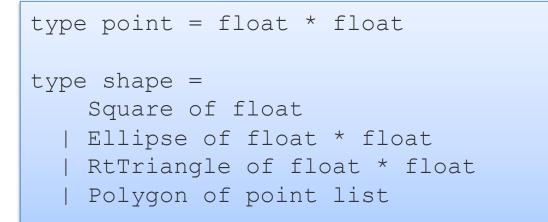
Compare

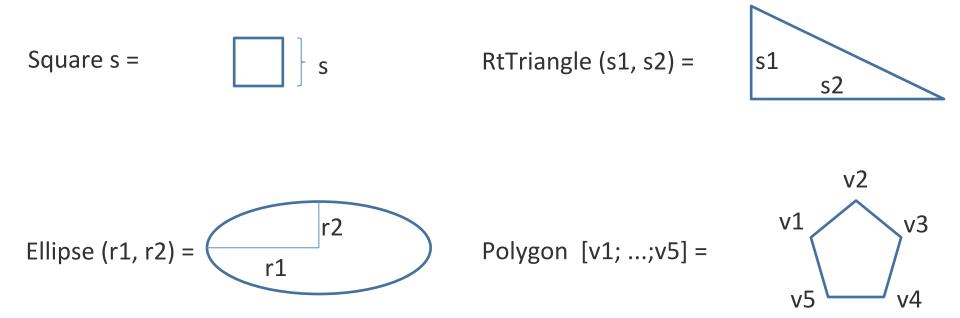
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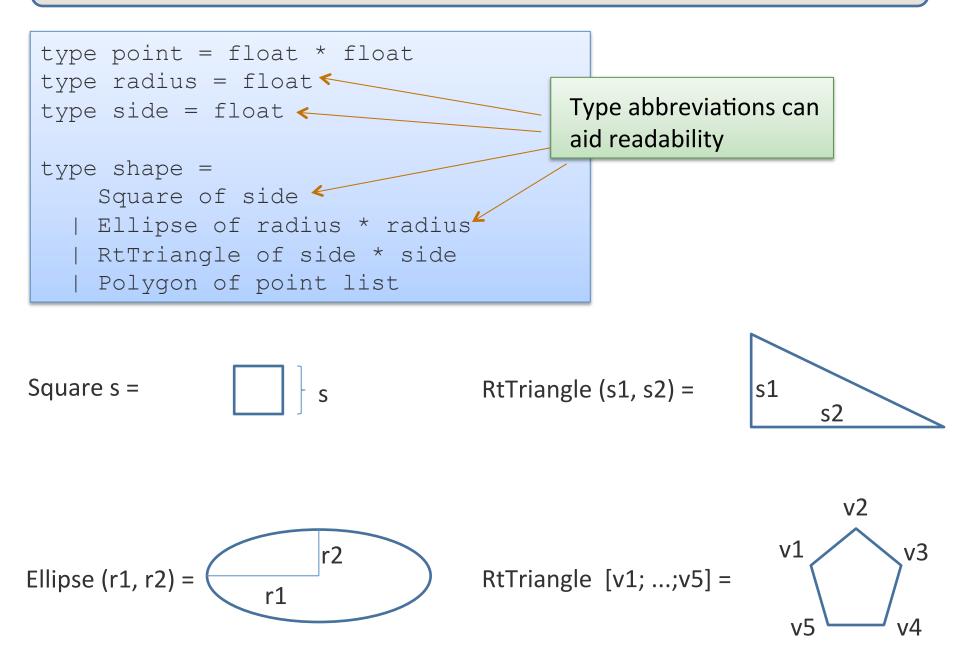
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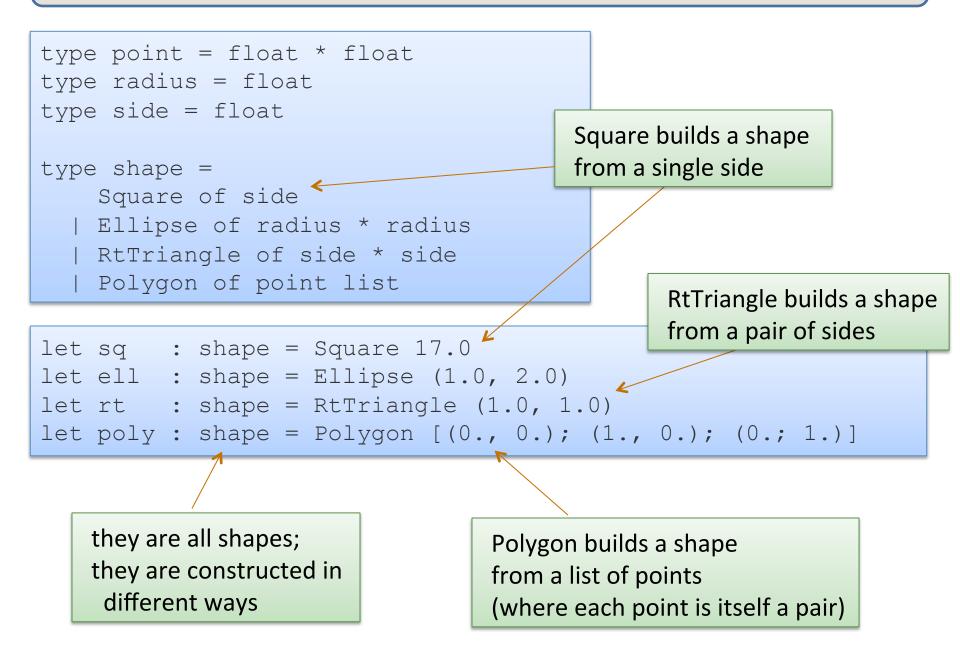
type my shape = point * float

let simple_area (s:my_shape) : float =
 (3.14 *. radius *. radius) ?? or ?? (side *. side)





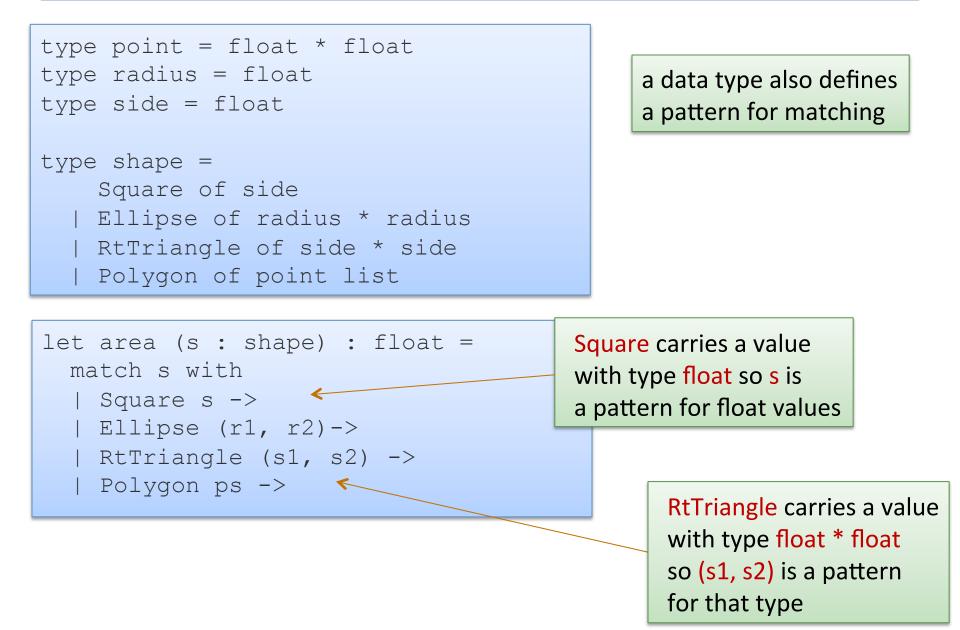




```
type point = float * float
type radius = float
type side = float
type shape =
    Square of side
    Ellipse of radius * radius
    RtTriangle of side * side
    Polygon of point list
```

```
let area (s : shape) : float =
  match s with
  | Square s ->
  | Ellipse (r1, r2)->
  | RtTriangle (s1, s2) ->
  | Polygon ps ->
```

a data type also defines a pattern for matching

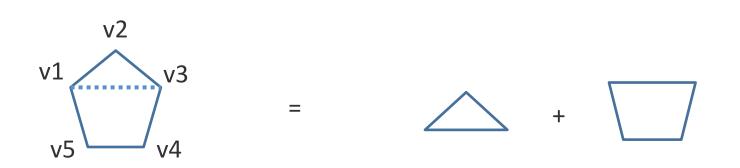


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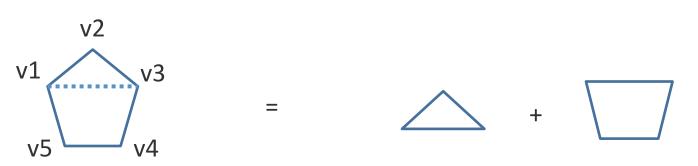
```
let area (s : shape) : float =
  match s with
   | Square s -> s *. s
   | Ellipse (r1, r2)-> pi *. r1 *. r2
   | RtTriangle (s1, s2) -> s1*.s2/.2.
   | Polygon ps -> ???
```

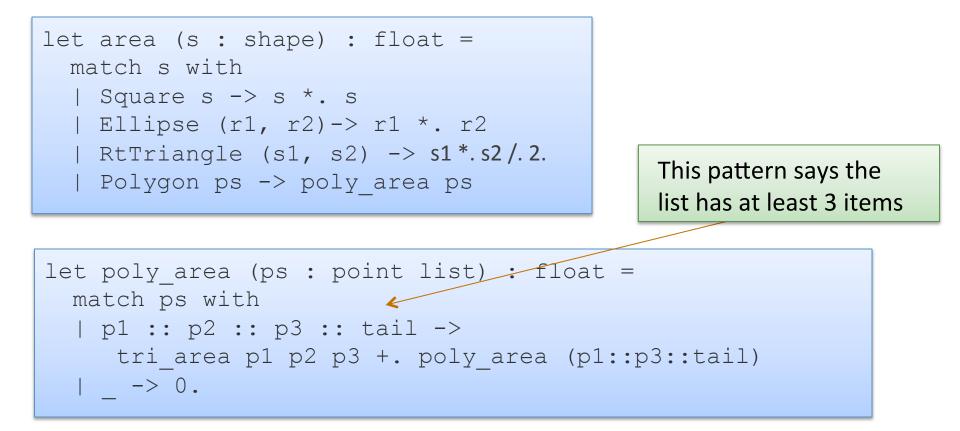
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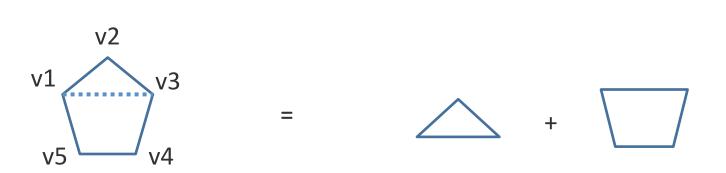
- How do we compute polygon area?
- For convex polygons:
 - Case: the polygon has fewer than 3 points:
 - it has 0 area! (it is a line or a point or nothing at all)
 - Case: the polygon has 3 or more points:
 - Compute the area of the triangle formed by the first 3 vertices
 - Delete the second vertex to form a new polygon
 - Sum the area of the triangle and the new polygon



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 - Compute the area of the triangle formed by the first 3 vertices
 - Delete the second vertex to form a new polygon
 - Sum the area of the triangle and the new polygon
- Note: This is a beautiful inductive algorithm:
 - the area of a polygon with n points is computed in terms of a smaller polygon with only n-1 points!







```
let tri_area (p1:point) (p2:point) (p3:point) : float =
    let a = distance p1 p2 in
    let b = distance p2 p3 in
    let c = distance p3 p1 in
    let s = 0.5 *. (a +. b +. c) in
    sqrt (s *. (s -. a) *. (s -. b) *. (s -. c))
```

```
let rec poly_area (ps : point list) : float =
  match ps with
  | p1 :: p2 :: p3 :: tail ->
     tri_area p1 p2 p3 +. poly_area (p1::p3::tail)
     | -> 0.
```

INDUCTIVE DATA TYPES

- We can use data types to define inductive data
- A binary tree is:
 - a Leaf containing no data
 - a Node containing a key, a value, a left subtree and a right subtree

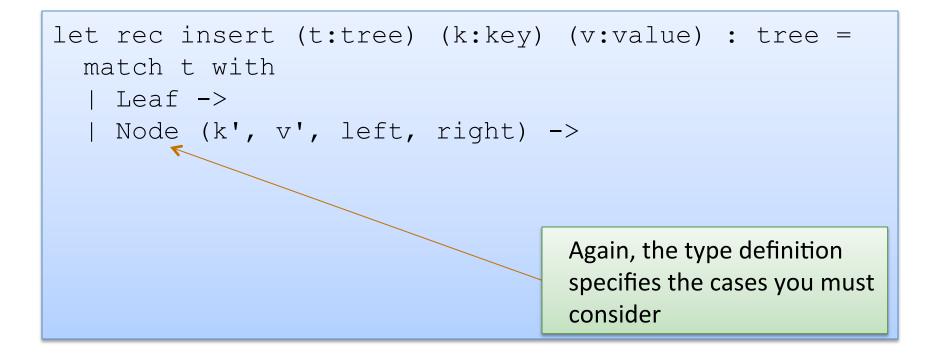
- We can use data types to define inductive data
- A binary tree is:
 - a Leaf containing no data
 - a Node containing a key, a value, a left subtree and a right subtree

```
type key = string
type value = int
type tree =
  Leaf
| Node of key * value * tree * tree
```

```
type key = int
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type tree =
  Leaf
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```

let rec insert (t:tree) (k:key) (v:value) : tree =

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type key = int
type value = string
type tree =
  Leaf
| Node of key * value * tree * tree
```



```
type key = int
type value = string
type tree =
  Leaf
| Node of key * value * tree * tree
```

```
let rec insert (t:tree) (k:key) (v:value) : tree =
match t with
    | Leaf -> Node (k, v, Leaf, Leaf)
    | Node (k', v', left, right) ->
```

```
type key = int
type value = string
type tree =
  Leaf
| Node of key * value * tree * tree
```

```
type key = int
type value = string
type tree =
  Leaf
| Node of key * value * tree * tree
```

```
type key = int
type value = string
type tree =
Leaf
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```

Inductive data types: Another Example

- Recall, we used the type "int" to represent natural numbers
 - but that was kind of broken: it also contained negative numbers
 - we had to use a dynamic test to guard entry to a function:

```
let double (n : int) : int =
   if n < 0 then
      raise (Failure "negative input!")
   else
      double_nat n</pre>
```

 it would be nice if there was a way to define the natural numbers exactly, and use OCaml's type system to guarantee no client ever attempts to double a negative number

- Recall, a natural number n is either:
 - zero, or
 - m + 1
- We use a data type to represent this definition exactly:

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 - zero, or
 - m + 1
- We use a data type to represent this definition exactly:

```
type nat = Zero | Succ of nat
let rec nat_to_int (n : nat) : int =
match n with
Zero -> 0
| Succ n -> 1 + nat_to_int n
```

- Recall, a natural number n is either:
 - zero, or
 - m + 1
- We use a data type to represent this definition exactly:

```
type nat = Zero | Succ of nat
let rec nat_to_int (n : nat) : int =
match n with
Zero -> 0
| Succ n -> 1 + nat_to_int n
let rec double_nat (n : nat) : nat =
match n with
| Zero -> Zero
| Succ m -> Succ (Succ(double_nat m))
```

Summary

- OCaml data types: a powerful mechanism for defining complex data structures:
 - They are precise
 - contain exactly the elements you want, not more elements
 - They are general
 - recursive, non-recursive (mutually recursive and polymorphic)
 - The type checker helps you detect errors
 - missing cases in your functions