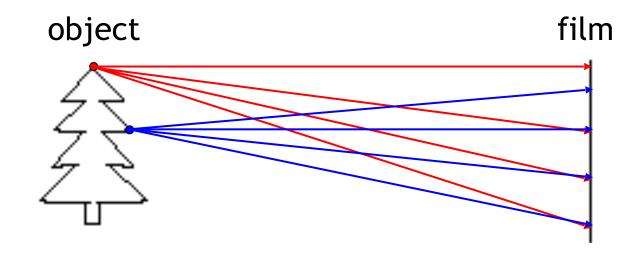
Lecture 2: Image formation and capture

COS 429: Computer Vision



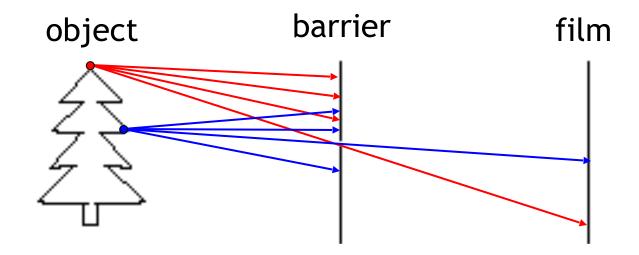
Pinhole camera: overview

Let's design a camera



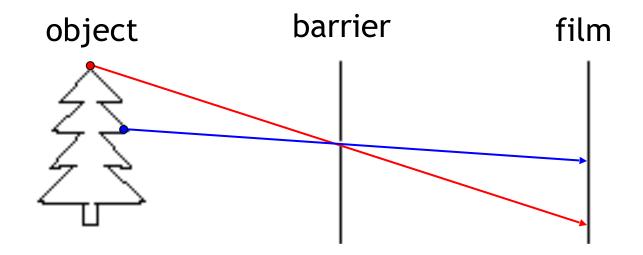
Idea 1: put a piece of film in front of an object Do we get a reasonable image?

Let's design a camera



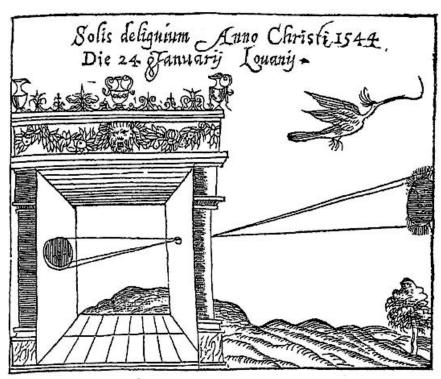
Add a barrier to block off most of the rays

Pinhole camera



- Captures pencil of rays all rays through a single point: aperture, center of projection, optical center, focal point, camera center
- The image is formed on the image plane

Camera obscura (Latin for "Dark Chamber")



Gemma Frisius, 1558

- Basic principle known to Mozi (470-390 BCE), Aristotle (384-322 BCE)
- Drawing aid for artists: described by Leonardo da Vinci (1452-1519)

Turning a room into a camera obscura



From Grand Images Through a Tiny Opening, Photo District News, February 2005

http://www.abelardomorell.net/project/camera-obscura/

Turning a room into a camera obscura

Hotel room, contrast enhanced



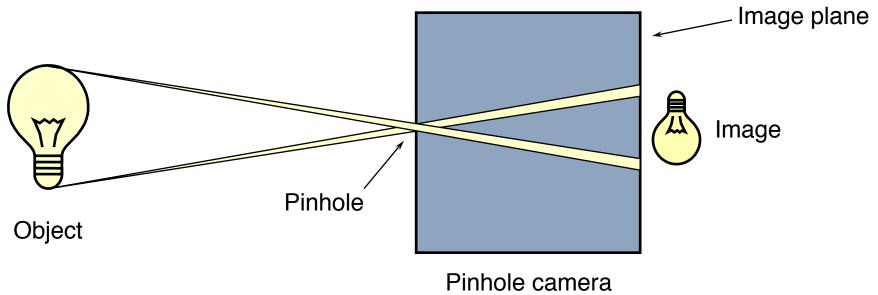
View from the window



Accidental pinholes produce images that are unnoticed or misinterpreted as shadows

Pinhole camera

 Each point on image plane illuminated by light from one direction

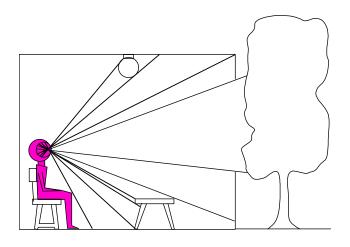


 Joseph Nicéphore Niépce: first recording onto pewter plate coated with bitumen (1826)



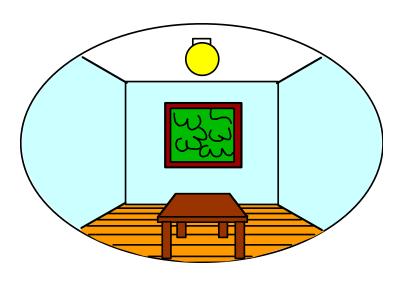
Dimensionality reduction: from 3D to 2D

3D world



Point of observation

2D image



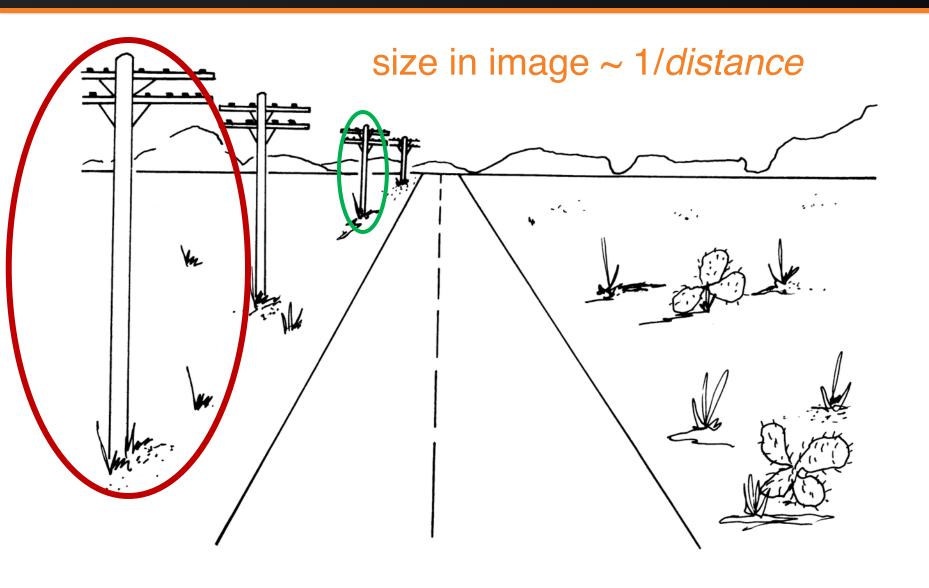
What properties of the world are preserved?

Straight lines, incidence

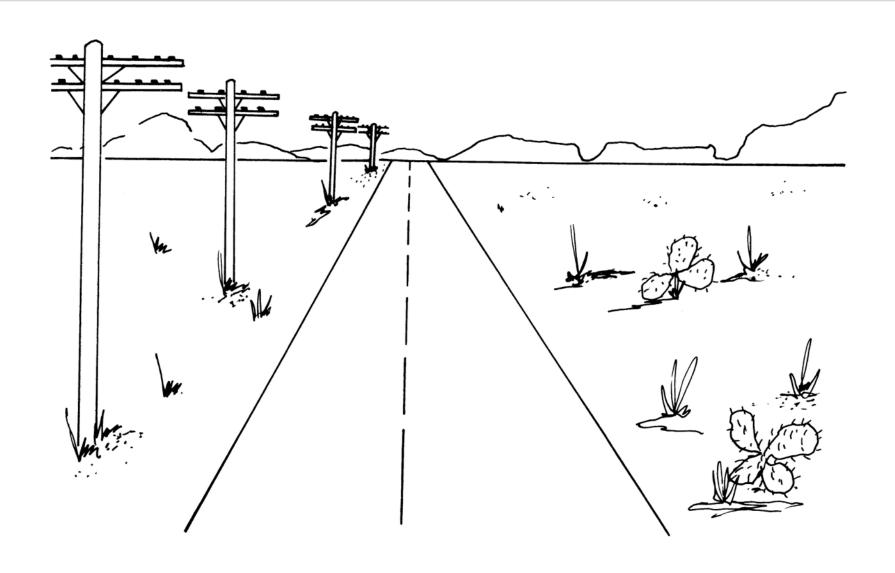
What properties are not preserved?

Angles, lengths

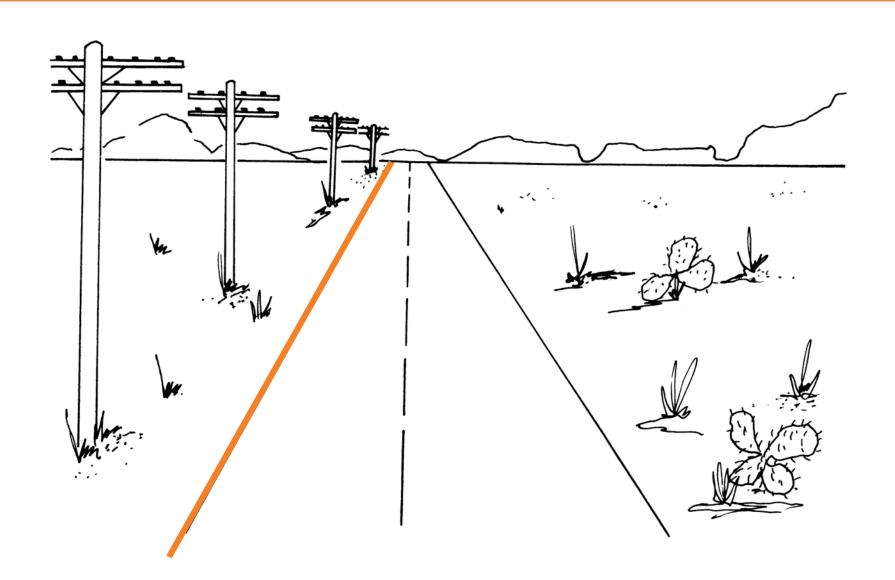
Nearer Objects Appear Bigger



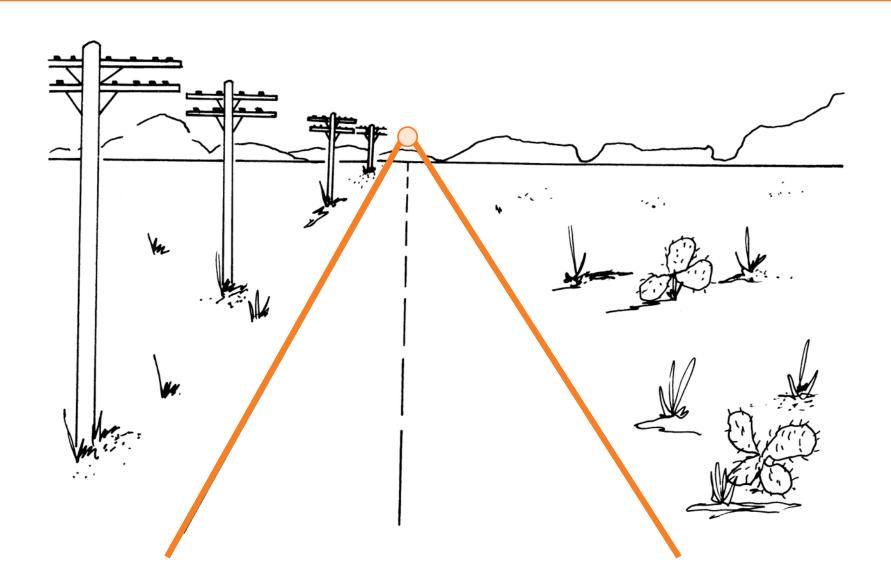
Perspective Projection Phenomena...



Straight Lines Remain Straight



Parallel Lines Converge at Vanishing Points



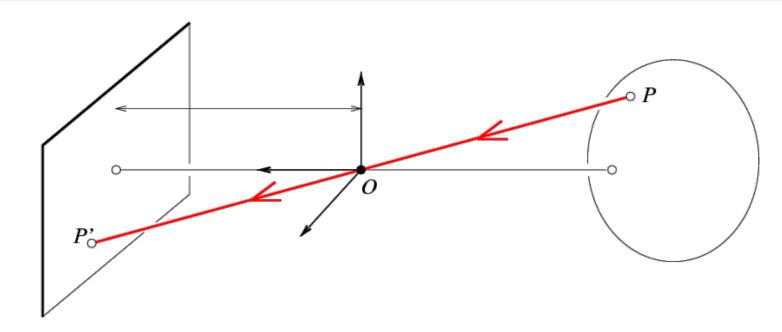
Parallel Lines Converge at Vanishing Points



Each family of parallel lines has its own vanishing point

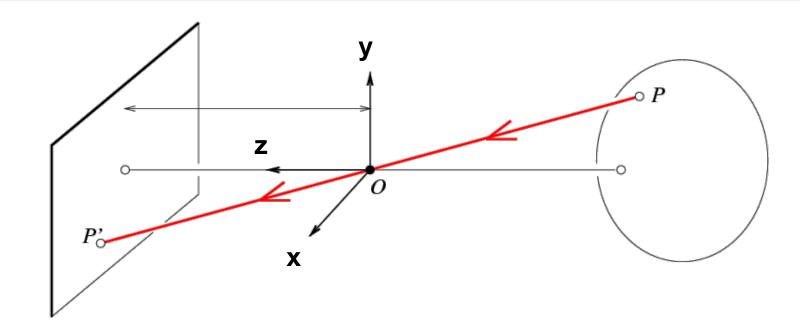
Pinhole camera: projection of a point

Modeling projection

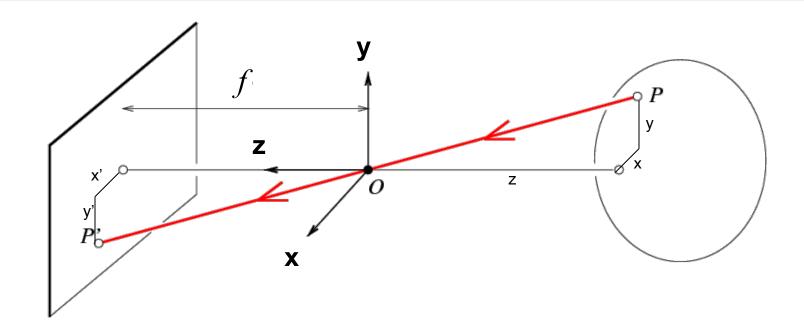


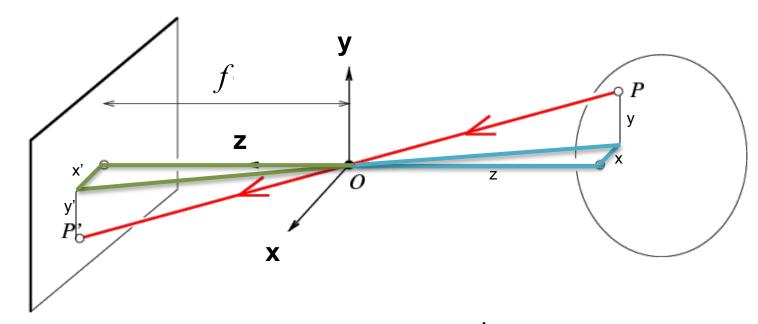
- To compute the projection P' of a scene point P, form the visual ray connecting P to the camera center O and find where it intersects the image plane
 - All scene points that lie on this visual ray have the same projection in the image
 - Are there scene points for which this projection is undefined?

The coordinate system



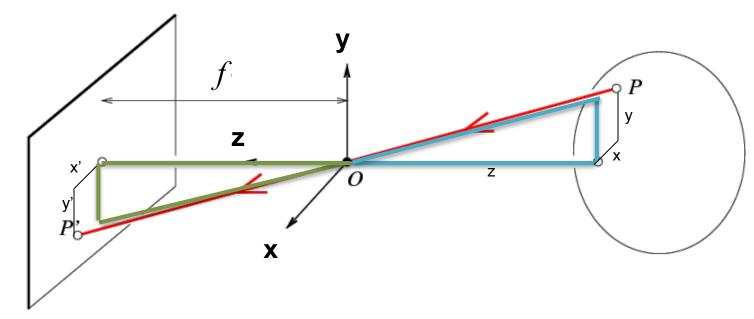
- The optical center (O) is at the origin
- The image plane is parallel to xy-plane or perpendicular to the z-axis, which is the *optical axis*



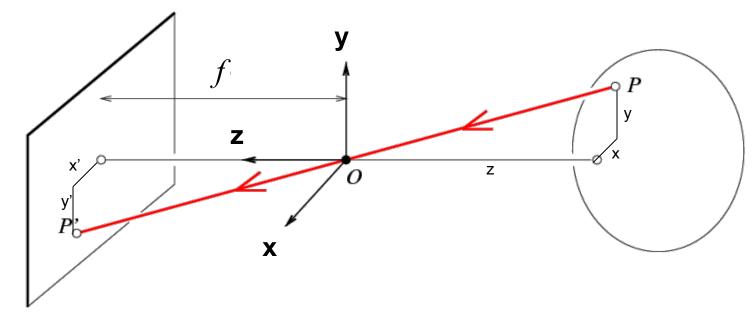


Using similar triangles:

$$\frac{x}{z} = \frac{x'}{f}$$



Using similar triangles:
$$\frac{x}{z} = \frac{x'}{f}$$
 $\frac{y}{z} = \frac{y'}{f}$



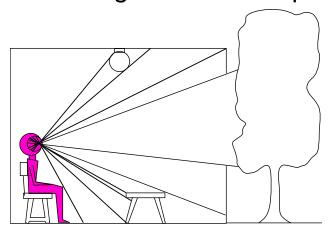
• Using similar triangles: $\frac{\tilde{z}}{z} =$

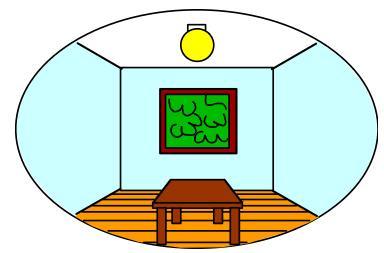
$$\frac{x}{z} = \frac{x'}{f} \qquad \frac{y}{z} = \frac{y'}{f}$$

• Thus: $(x, y, z) \rightarrow (f \frac{x}{z}, f \frac{y}{z})$

Fronto-parallel planes

- What happens to the projection of a pattern on a plane parallel to the image plane?
 - All points on that plane are at a fixed depth z
 - The pattern gets scaled by a factor of f / z, but angles and ratios of lengths/areas are preserved



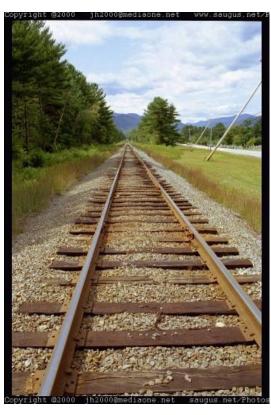


$$(x, y, z) \rightarrow (f \frac{x}{z}, f \frac{y}{z})$$

Pinhole camera: projection of a line

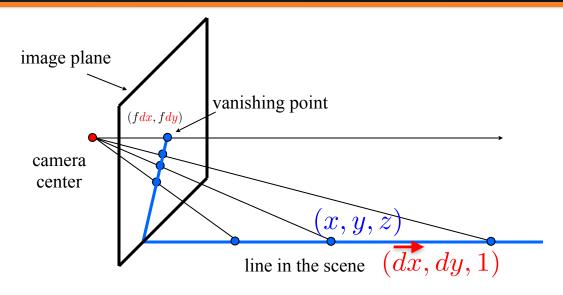
Vanishing points

- All parallel lines converge to a vanishing point
 - Each direction in space is associated with its own vanishing point
 - Exception: directions parallel to the image plane



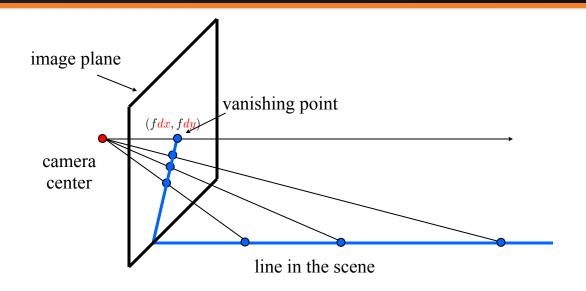


Constructing the vanishing point of a line



- Claim: Each direction in space is associated with one vanishing point
 - Any point on the line: $(x, y, z) + \alpha(dx, dy, 1)$
 - This point is projected to: $\left(f\frac{x+\alpha dx}{z+\alpha}, f\frac{y+\alpha dy}{z+\alpha}\right)$
 - The limit as $\alpha \to \inf: (f dx, f dy)$
 - Thus the vanishing point is independent of the location (x, y, z) and uniquely determined by the direction (dx, dy, 1)

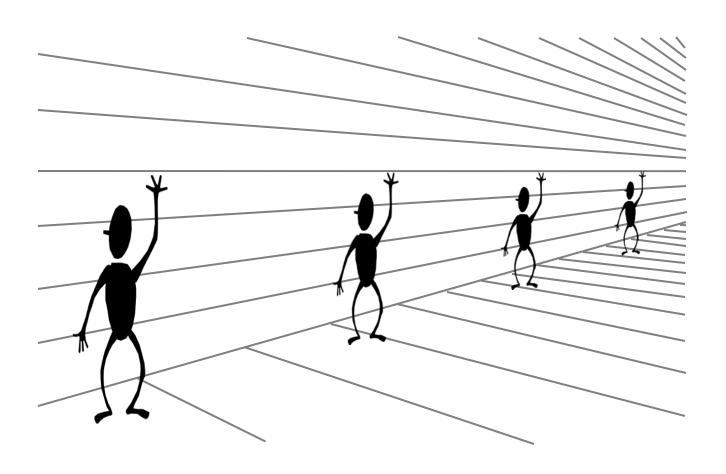
Constructing the vanishing point of a line



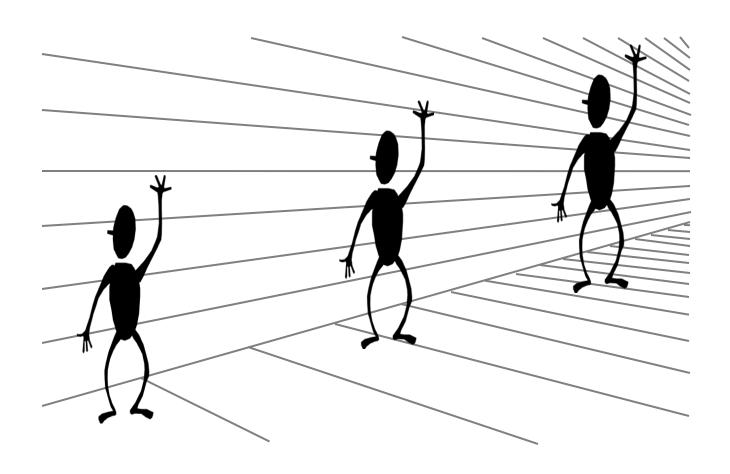
- To find the vanishing point, shoot a ray from camera center along the same direction. Find the intersection with the image plane.
- How does the vanishing point move if the camera is moved without rotation?

Source: Steve Seitz

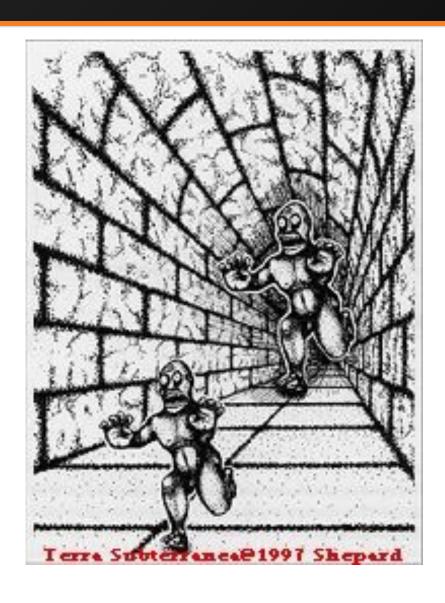
Perspective cues

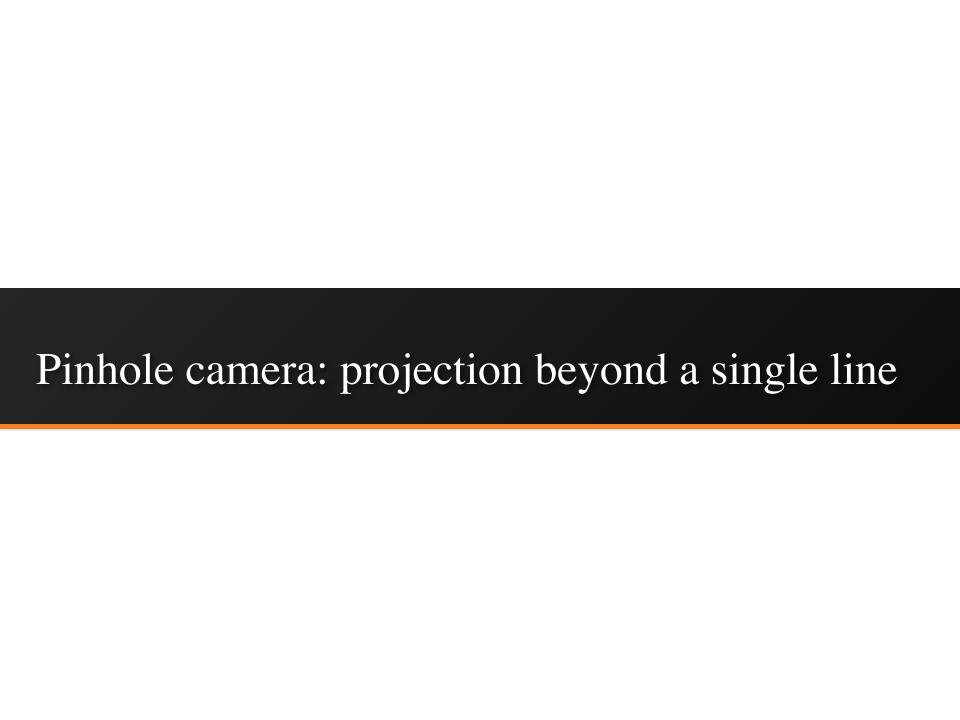


Perspective cues

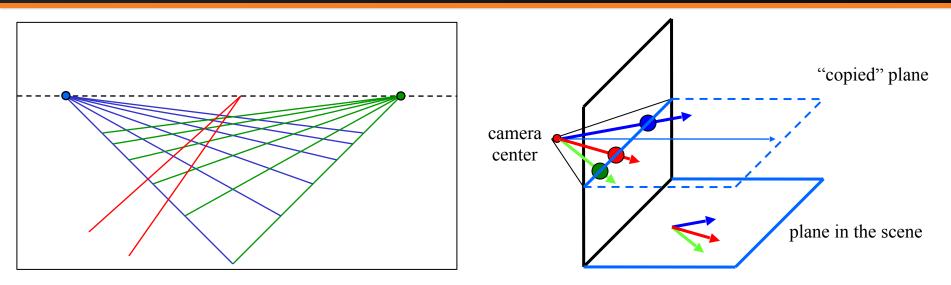


Perspective cues



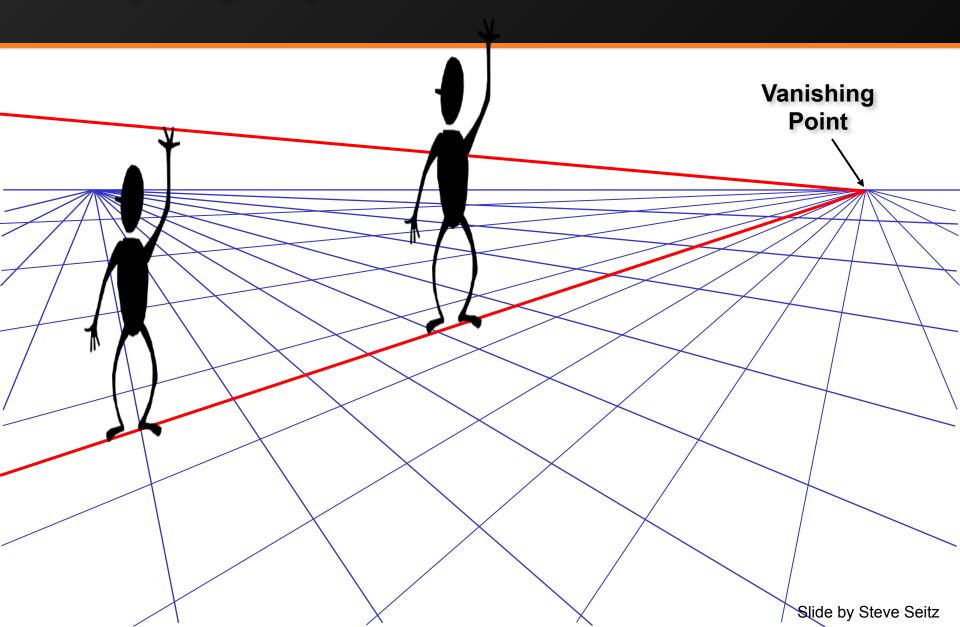


Vanishing lines of planes

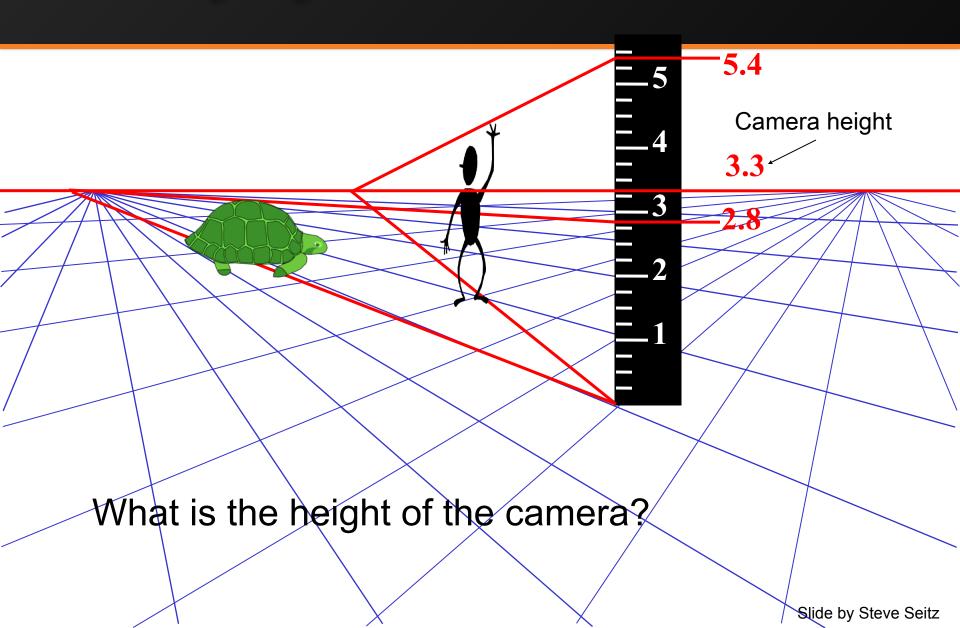


- Vanishing points of co-planar directions form a vanishing line (exercise for fun: show this algebraically)
- Horizon: vanishing line of the ground plane
 - All points at the same height as the camera project to the horizon
 - Points higher (resp. lower) than the camera project above (resp. below) the horizon
 - Provides way of comparing height of objects

Comparing heights



Measuring height



Quiz 1



Which is higher? The parachutist or the person taking the picture?

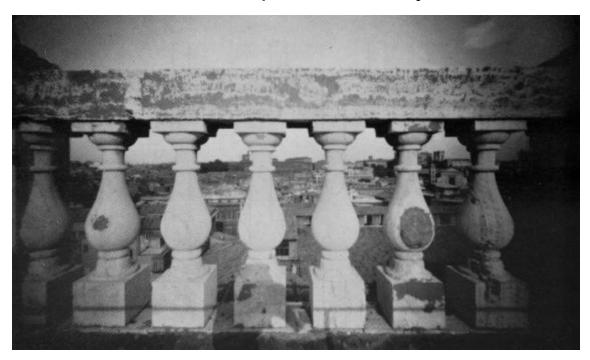
Quiz 2

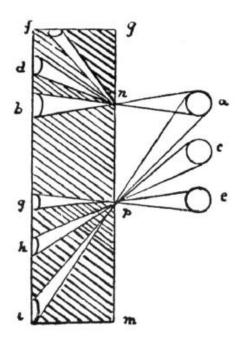


How does the location of the horizon change if the person taking the picture raise the camera but keep its orientation?

Perspective distortion

- Are the widths of the projected columns equal?
 - The exterior columns are wider
 - This is not an optical illusion, and is not due to lens flaws
 - Phenomenon pointed out by Da Vinci





Perspective distortion

What is the shape of the projection of a sphere?

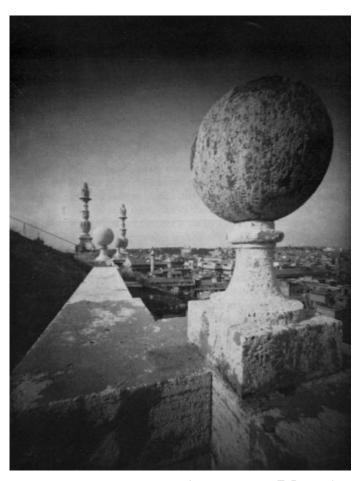
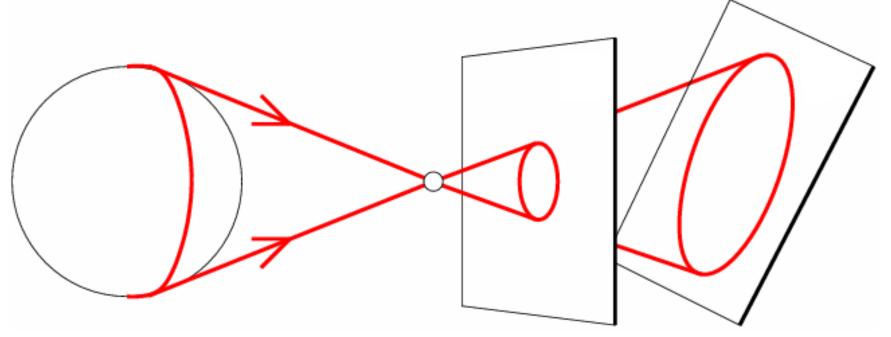


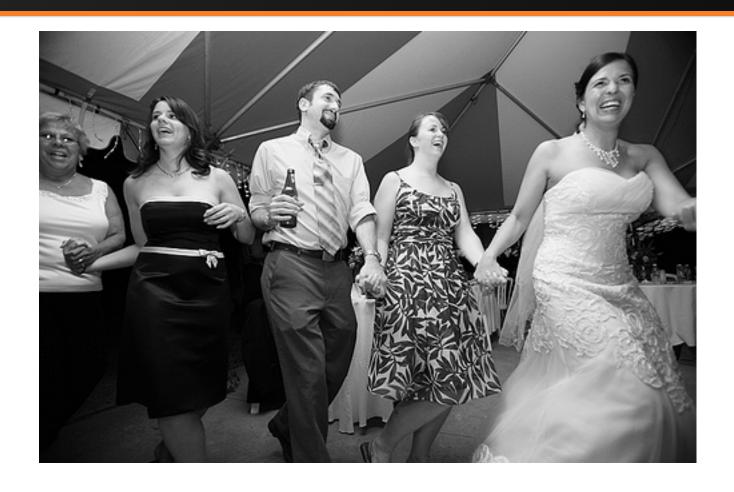
Image source: F. Durand

Perspective distortion

What is the shape of the projection of a sphere?



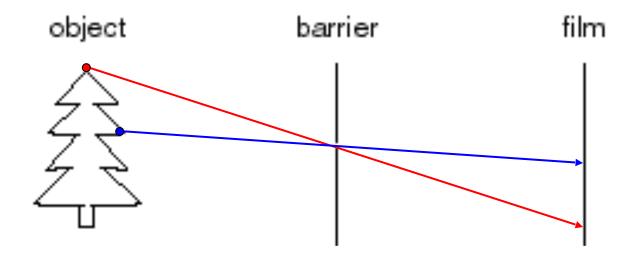
Perspective distortion: People



Building a real camera



Pinhole camera



Home-made pinhole camera



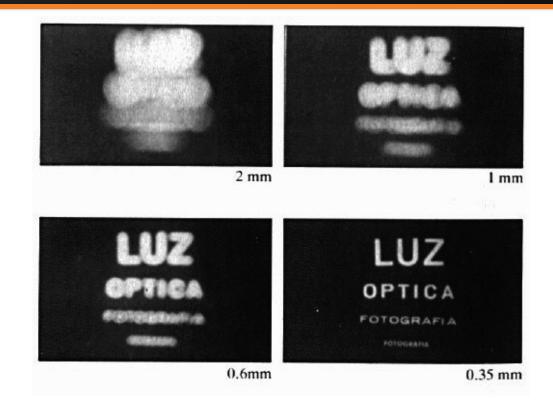
http://www.debevec.org/Pinhole/

Aperture

Controls amount of light



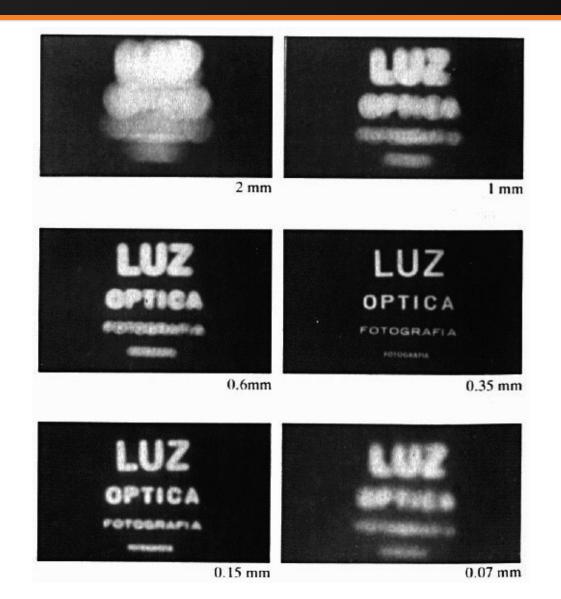
Shrinking the aperture



Why not make the aperture as small as possible?

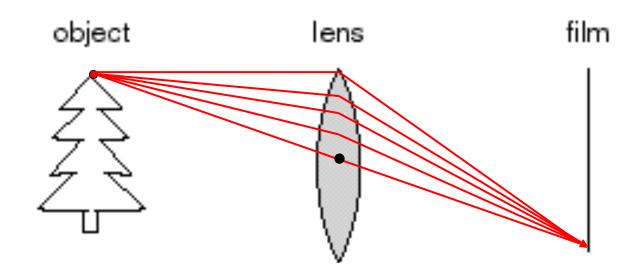
- Less light gets through
- Diffraction effects...

Shrinking the aperture



Slide by Steve Seitz

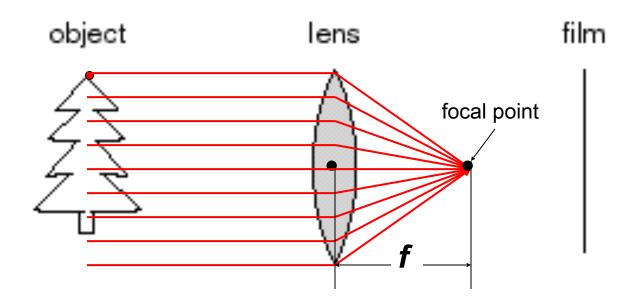
Adding a lens



A lens focuses light onto the film

- Thin lens model:
 - Rays passing through the center are not deviated (pinhole projection model still holds)

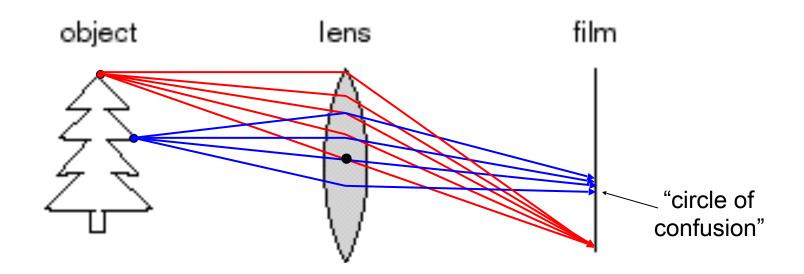
Adding a lens



A lens focuses light onto the film

- Thin lens model:
 - Rays passing through the center are not deviated (pinhole projection model still holds)
 - All parallel rays (along the principal axis) converge to one point on a plane located at the focal length f

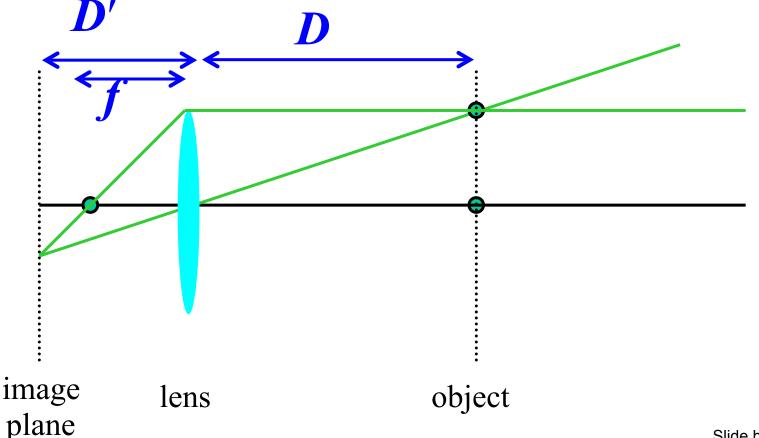
Adding a lens



A lens focuses light onto the film

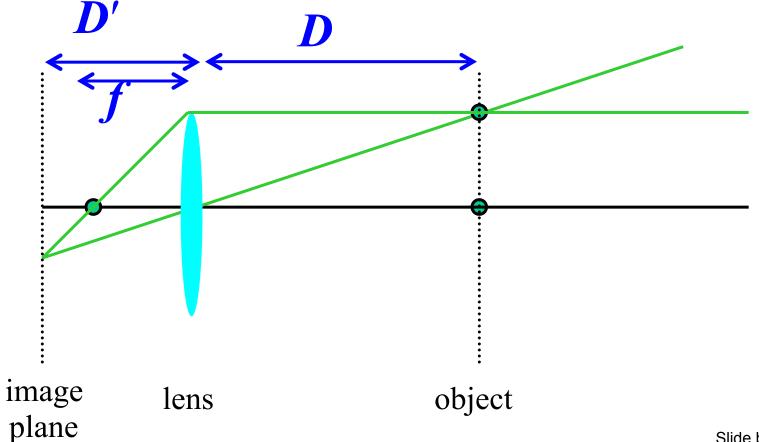
- There is a specific distance at which objects are "in focus"
 - Other points project to a "circle of confusion" in the image

• What is the relation between the focal length (f), the distance of the object from the optical center (D), and the distance at which the object will be in focus (D')?



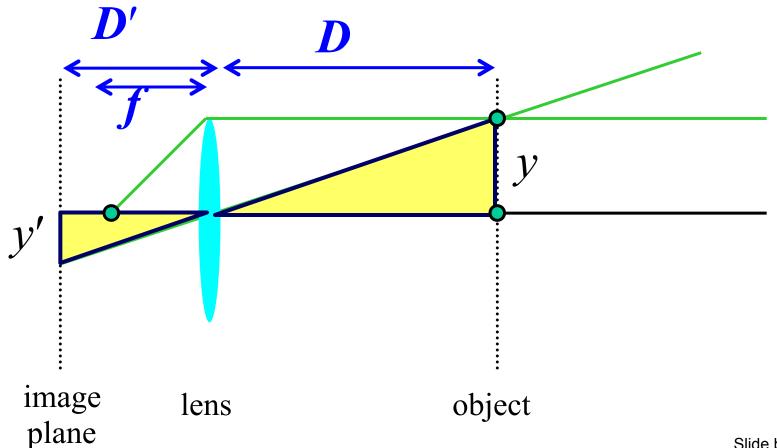
Slide by Frédo Durand

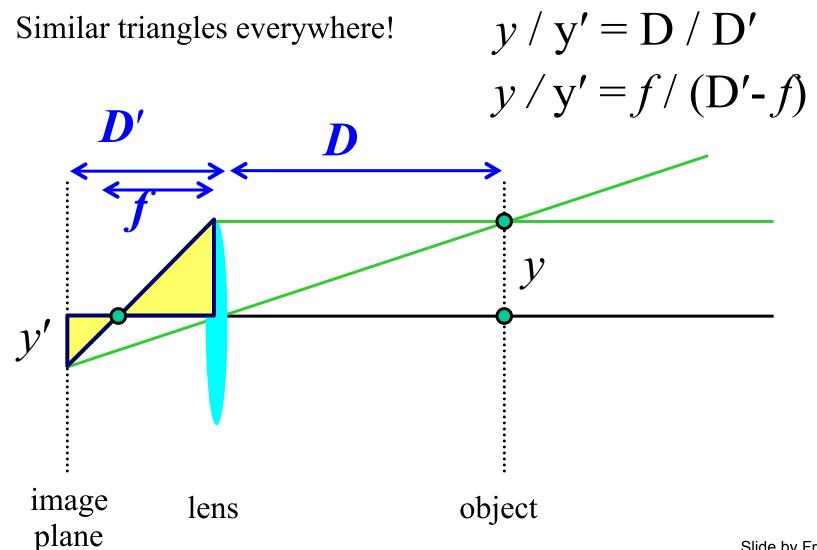
Similar triangles everywhere!

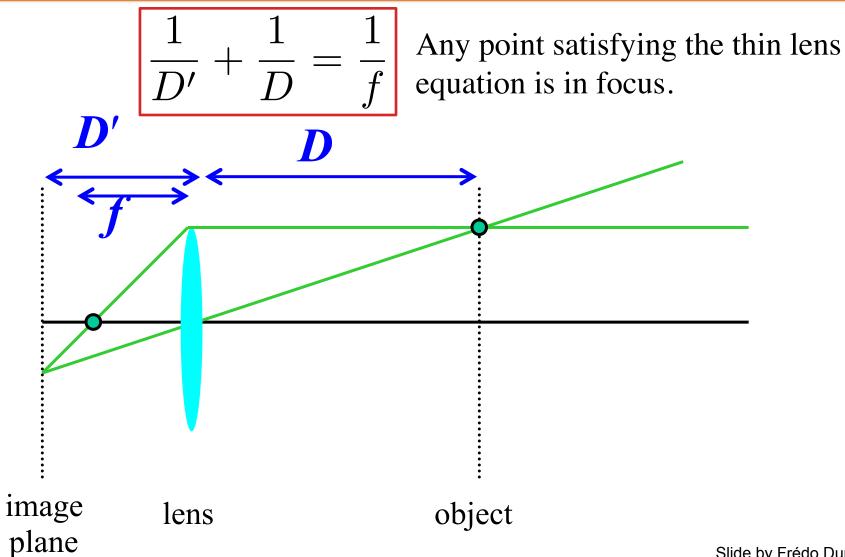


Similar triangles everywhere!

$$y / y' = D / D'$$

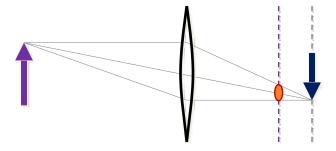






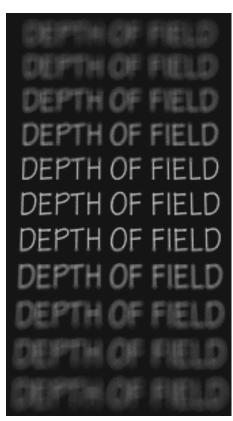
Focus and Depth of Field

- For a given D, "perfect" focus at only one D'
- In practice, OK for some range of depths
 - Circle of confusion smaller than a pixel



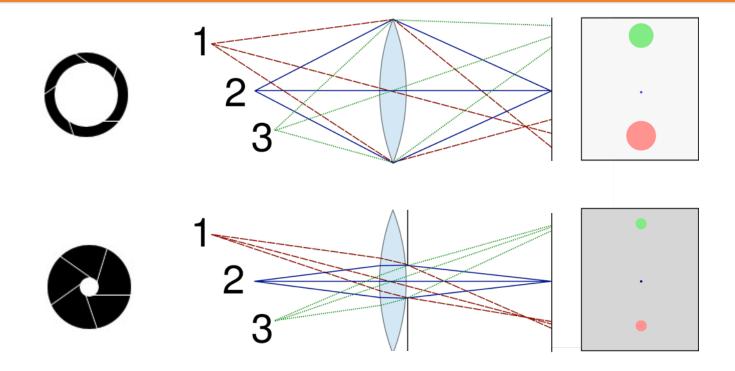
Depth of Field





http://www.cambridgeincolour.com/tutorials/depth-of-field.htm

Controlling depth of field



Changing the aperture size affects depth of field

- A smaller aperture increases the range in which the object is approximately in focus
- But small aperture reduces amount of light need to increase exposure

Varying the aperture



Large aperture = small DOF



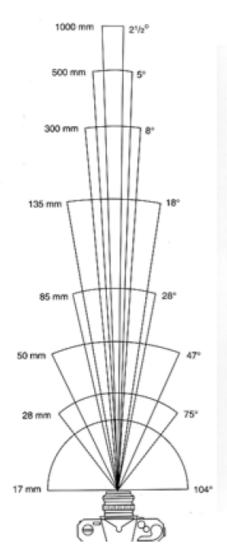
Small aperture = large DOF

Aperture |

- Aperture typically given as "f-number"
- What is *f*/4?
 - Aperture diameter is ¼ the focal length
- One "f-stop" equals change of f-number by √2
 - Equals change in aperture area by factor of 2
 - Equals change in amount of light by factor of 2
 - Example: $f/2 \rightarrow f/2.8 \rightarrow f/4$ (each one doubles light)

Building a real camera: field of view

Field of View







17mm

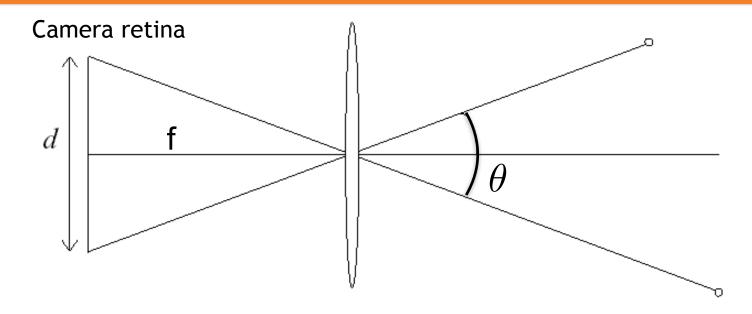






85mm

Field of View

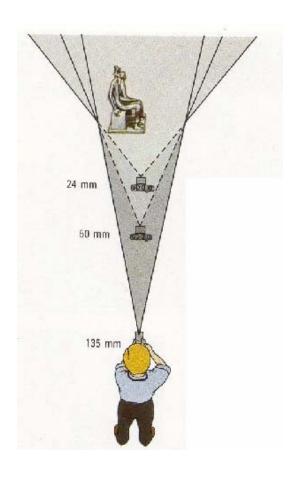


FOV depends on focal length and size of the camera retina

$$\theta = 2 \tan^{-1} \left(\frac{d}{2f} \right) \approx \frac{d}{f}$$

Larger focal length = smaller FOV

Field of View / Focal Length





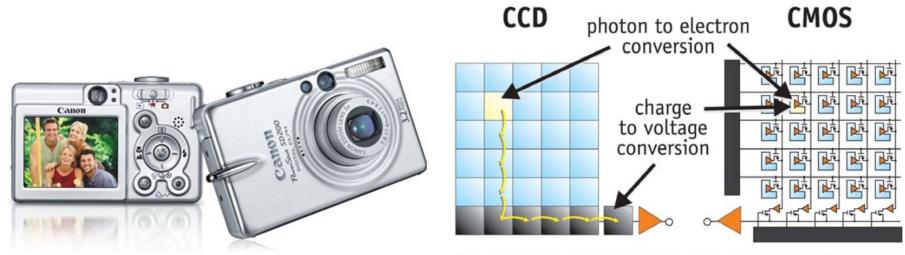
Large FOV, small *f* Camera close to car



Small FOV, large *f*Camera far from the car



Digital camera

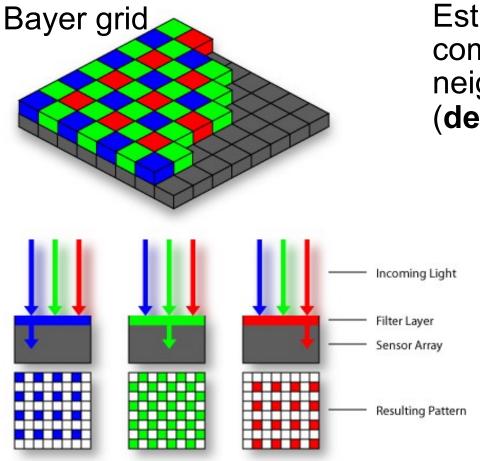


CCDs move photogenerated charge from pixel to pixel and convert it to voltage at an output node. CMOS imagers convert charge to voltage inside each pixel.

A digital camera replaces film with a sensor array

- Each cell in the array is light-sensitive diode that converts photons to electrons
- Two common types
 - Charge Coupled Device (CCD)
 - Complementary metal oxide semiconductor (CMOS)
- http://electronics.howstuffworks.com/digital-camera.htm

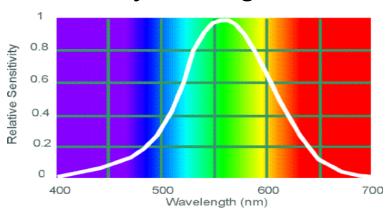
Color sensing: Color filter array



Estimate missing components from neighboring values (demosaicing)







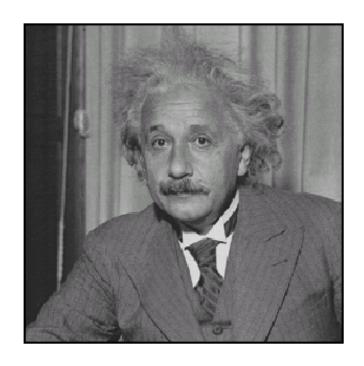
Human Luminance Sensitivity Function

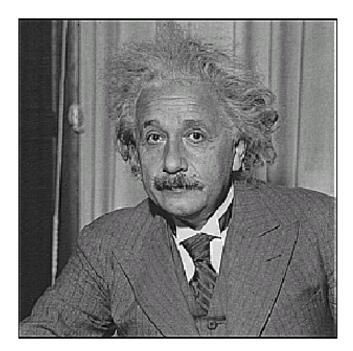
Source: Steve Seitz

COS 597C: Advances in Image Processing

- Taught by Prof. Rusinkiewicz this quarter
- Mon 1:30-4:20pm in CS 401
- "This seminar explores recent developments in image processing, manipulation, analysis, and synthesis, including data-driven and deeplearning-based methods."

Next class: convolution and filtering





before after